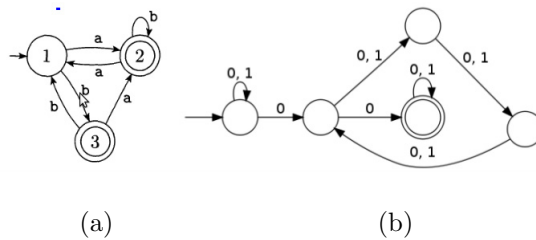


### CS21004, Tutorial 3

1. Design NFAs for the following regular expressions over  $\Sigma(ab)$

- a.  $(aa^* + aba^*b^*)^*$
- b.  $(ab(a + ab)^*(a + aa))$

2. Consider the following NFAs and write the equivalent regular expressions



3. Consider a language  $L = \{w \in \Sigma^* \mid w \text{ contains at least two 0s, or exactly two 1s}\}$ . Draw a NFA with six states that accepts this language.

4. Consider the regular expression  $R = (aa)^* + b^*$ .
- a. Draw an NFA of the above regular expression with not more than 4 states.
  - b. Draw the equivalent DFA.
  - c. Find  $R^c$  which recognizes the complement of language recognized by  $R$ .

5. Find an NFA that accepts  $((a + b)a^*) \cap (baa^*)$ .

6. Let  $\Sigma = \{1, \#\}$  and let  $Y = \{w \mid w = x_1\#x_2\#x_3\#\dots\#x_k \text{ for } k > 0, x_i \in 1^* \text{ and } x_i \neq x_j \text{ for } i \neq j\}$   
 Prove that  $Y$  is not regular.

7. Prove or disprove the following languages as regular

- (a)  $\{w \mid w \in \{0, 1\}^* \text{ is not a palindrome}\}$ .
- (b)  $\{w \mid w \text{ contains an equal number of occurrences of the substrings } 01 \text{ and } 10\}$ .