LOGICAL DEDUCTION IN AI

PROPOSITIONAL LOGIC TO PREDICATE LOGIC



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Deduction Using Propositional Logic: Steps

- <u>Choice of Boolean Variables (a, b, c, d)</u>... which can take values true or <u>false</u>. \checkmark (\land (\land (\land)) \rightarrow (\land) \checkmark (\land) <u>Boolean Formulae developed</u> using well defined connectors \sim , \land , V, \rightarrow , etc, whose meaning (semantics) is given by their truth tables.
- <u>Codification of Sentences of the argument into Boolean Formulae.</u>
- Developing the <u>Deduction Process</u> as obtaining truth of a <u>Combined</u> Formula expressing the complete argument.

Determining the Truth or Validity of the formula and thereby proving or disproving the argument and Analyzing its truth under various, Interpretations.

Deduction Using Propositional Logic: Example 1

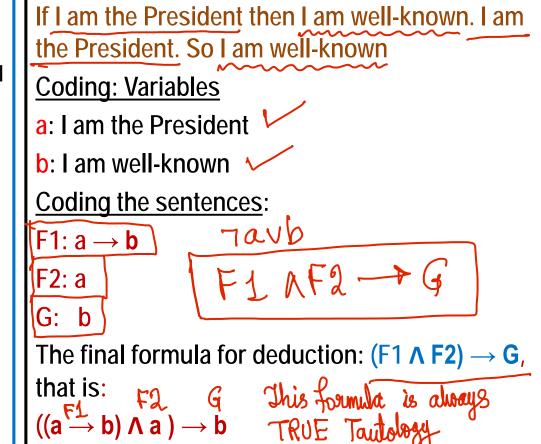
<u>Choice of Boolean Variables a, b, c, d,</u> ... which can take values <u>true</u> or <u>false</u>.

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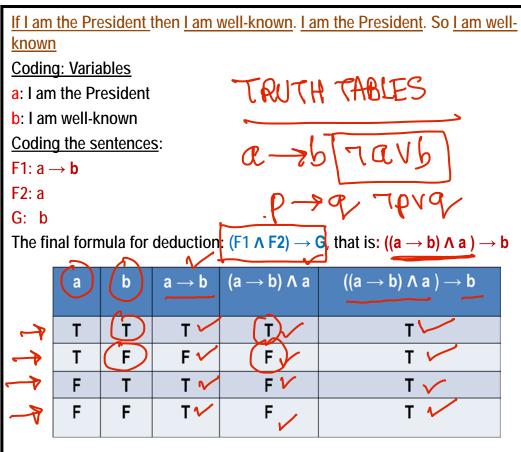
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Boolean formulae developed using well defined connectors \sim , \land , \lor , \rightarrow , etc, whose meaning (semantics) is given by their truth tables.

Codification of sentences of the argument into Boolean Formulae.

Developing the Deduction Process as obtaining truth of a combined formula expressing the complete argument.

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Deduction Using Propositional Logic: Example 2

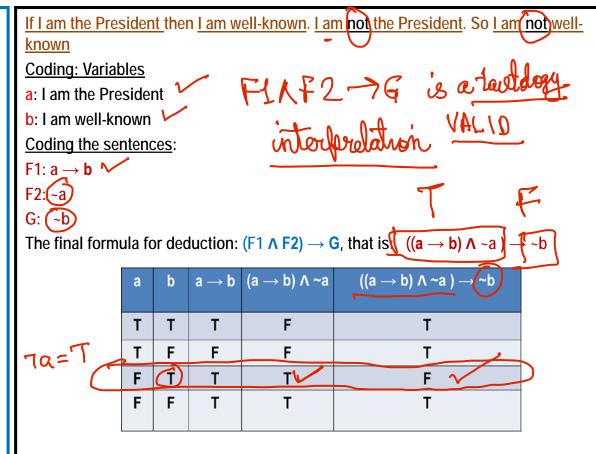
Boolean variables a, b, c, d, ... which can take values <u>true</u> or <u>false</u>.

Boolean formulae developed using well defined connectors \sim , \land , \lor , \rightarrow , etc, whose meaning (semantics) is given by their truth tables.

Codification of sentences of the \checkmark argument into Boolean Formulae.

Developing the Deduction Process as obtaining truth of a combined formula expressing the complete argument.

Determining the Truth or Validity of the formula and thereby proving or disproving the argument and \sim Analyzing its truth under various interpretations.



Insufficiency of Propositional Logic

Wherever Mary goes, so does the lamb. Mary goes to school. So

the lamb goes to school.

all some no

No contractors are dependable. Some engineers are contractors. Therefore some engineers are not dependable.

All dancers are graceful. Ayesha is a student. Ayesha is a dancer. Therefore some student is graceful.

Every passenger is either in first class or second class. Each passenger is in second class if and only if he or she is not wealthy. Some passengers are wealthy. Not all passengers are wealthy. Therefore some passengers are in second class. Predicate Logic First order Logic

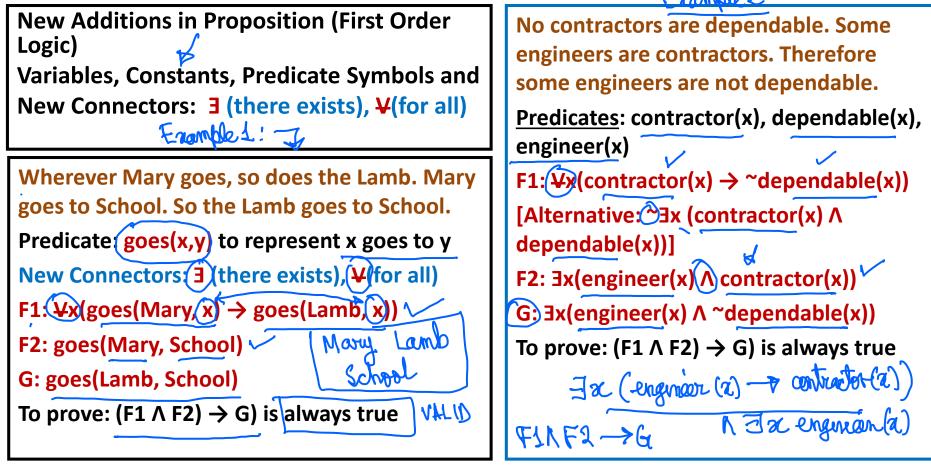
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Every passenger is either in first class or second class. Each passenger is in second class if and only if he or she is not wealthy. Some passengers are wealthy. Not all passengers are wealthy. Therefore some passengers are in second class. **New Additions in Proposition (First Order** Logic) - Function symbols Variables, Constants, Predicate Symbols and New Connectors: (3) (there exists), ¥(for all) Some orguments all x goes to y. a variables predicate symbol contractor (2) dependable (2)

Formulating Predicate Logic Statements



Example 3 ! -

More Examples Example: 4

All dancers are graceful. Ayesha is a student. Ayesha is a dancer. Therefore some student is graceful. graceful (x) student (x) doncer(x) Agesha F1: 42 2 dancor (x) -> gracefal (x) fancor (2) A grace student (Ayesha) F2: dancer (Ayesha) F3 : Fx J. student (x) N Gi graceful (2) 4 (F1KF2NF3) - G

Every passenger is either in first class or second class. Each passenger is in second class if and only if the passenger is not wealthy. Some passengers are wealthy. Not all passengers are wealthy. Therefore some passengers are in second class. p(x), f(x) s(x) w(x) - weally Ly passinger in first class - grand class + + + p(x) → (f(x) V 8(x)) 2 $\forall x \neq p(x) \rightarrow f(f(x) \land \neg s(x)) \lor \checkmark$ (7,f(x) & 8(x))} F2. $\forall x \neq p(x) \rightarrow ((3(x) \rightarrow \neg w(x)))$ $\exists sp(x) \land w(x) \rbrace (\neg w(x) \rightarrow s(x)) \rbrace$ - (42 2p(x)→w (2) 2) [F4: =>x2p(x) ~~w(x) 323 P(x) & S(2) 3 ((F1KF2KF3K

