



# Branch Target Buffer Energy Reduction Through Efficient Multiway Branch Translation Techniques

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Branch Target Buffer (BTB) plays an important role for pipelined processors in branch prediction during the execution of loops, if-then-else, call-return, and multiway branch statements. It has been observed that 20% of instructions in a program are related to branch. Access to BTB consumes 10% of total energy consumption of a program in execution. The present work introduces the use of  $K-d$  tree and pattern matcher to generate efficient code, i.e., lesser execution time, for multiway branch. However, instead of enhancing performance, Voltage Frequency Scaling (VFS) can be applied to achieve energy efficiency without degradation in performance. The present work is evaluated on a wide range benchmark programs. The BTB energy saving in the present work lies in the range 20% to 80% with small improvement performance as well. The total energy reduction is in the range 3–12%.

**Keywords:** Multiway Branch,  $K-d$  Tree, Pattern Matcher, Voltage Frequency Scaling, Branch Target Buffer, Energy, Performance.

## 1. INTRODUCTION

The present work introduces some techniques to reduce Branch Target Buffer (BTB) energy consumption through efficient translation of multiway branch. Low energy code generation is an important aspect of modern compilers.<sup>1</sup> It has been observed that 20% of instructions in a program are branch instructions.<sup>2</sup> BTB consumes 10% of total energy consumption of a program in execution.<sup>10,11</sup>

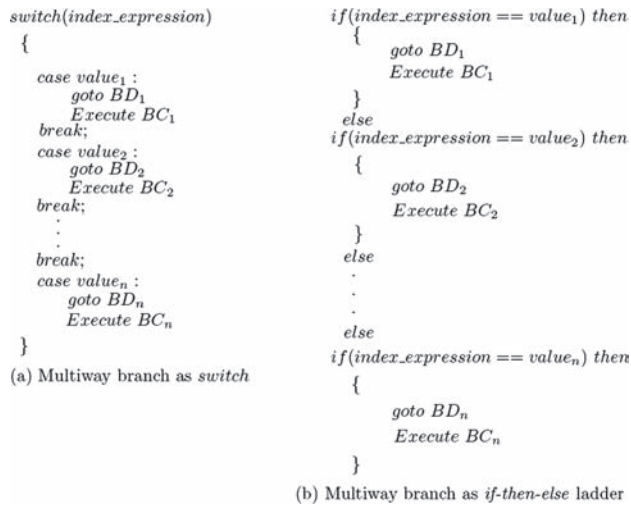
In most of the high-level languages, the construct ‘Multiway Branch’ ( $MB$ ) is widely used for the selection of one out of several possible blocks of code to be executed. For example, it is the *case* statement in Pascal, it is the *switch* statement in C and it is the *SELECT* statement in Fortran 90. Figures 1(a) and (b) shows the multiway branch as switch and *if-then-else* ladder, respectively, containing  $n$  branch destinations. Where,  $BC_j$  is the block of code at  $j$ th branch destination ( $BD_j$ ),  $1 \leq j \leq n$ . One or more index variables form an index expression. The index expression should match with the  $j$ th matching value ( $value_j$ ) to jump to  $BD_j$  and execute  $BC_j$ .

In modern processors Dynamic Branch Prediction is done and Branch Target Buffer (BTB) is commonly used to improve the performance of execution of branch

instructions. Dynamic Branch Prediction uses the information about taken or not taken branches gathered at run-time to predict the outcome of a branch. BTB is a small cache memory used to hold the branch history and the target addresses corresponding to different branch instructions.

There are three possible alternatives for the implementation of multiway branch. The three implementations are based on the way the index expression with  $value_j$  is searched to find out  $BD_j$ . These are linear search, binary search or hashing.<sup>3,4</sup> For a given  $MB$  the compiler implements either  $B_{linear}$ ,  $B_{binary}$ , or  $B_{hash}$  on the basis of value(s) of index expression(s).  $B_{linear}$ ,  $B_{binary}$ , and  $B_{hash}$  requires  $O(n)$ ,  $O(\log_2 n)$  and  $O(1)$  BTB accesses, respectively, to find out the target address of the  $BD_j$ . The first choice of the compiler is to implement a  $B_{hash}$ . The generation of  $B_{hash}$  depends on the possibility to find a hash function by analyzing the values matched by the index expression(s). This may not be possible for every  $MB$ . But it is always possible to generate a  $B_{binary}$ . However, the simplest implementation is the  $B_{linear}$ . In case of *if-then-else ladders*, most of the modern compilers generate  $B_{linear}$ , when multiway branch decision depends on more than one index expressions. The present work shows that it is possible to implement  $B_{hash}$  or  $B_{binary}$  for such *if-then-else ladders*. It introduces the utility of  $k-d$  tree<sup>6</sup> to generate  $B_{binary}$ . Many modern programming languages like C# and Ruby supports  $MB$  where the index expression values are strings.

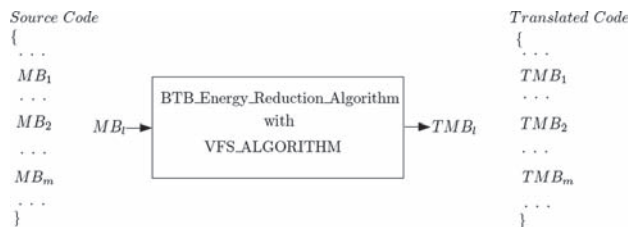
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**Fig. 1.** Equivalent forms of multiway branch.

The present work helps to generate efficient code called  $B_{pattern}$  for such  $MB$  using pattern matching. It considers a source code containing  $m$   $MB$ s and translates them to  $m$   $TMB$ s (Translated Multiway Branch) as shown in Figure 2. The  $MB_l$  is based on  $B_{linear}$ , on the other hand  $TMB_l$  utilizes either a  $B_{binary}$  or a  $B_{hash}$ .

As  $TMB_l$  utilizes either a  $B_{binary}$  or a  $B_{hash}$ , its execution time is smaller than that of  $B_{linear}$ . However, instead of enhancing performance, it is possible to reduce energy consumption by scaling down the voltage along with frequency, commonly known as Voltage and Frequency Scaling (VFS). However, the processor on which the code is executed should be a special type of processor that can operate at different voltages and frequencies, such as Strong ARM 1100. Here, we have used Intel's XScale processor, which works on nine different voltage–frequency ( $v, f$ ) pairs and supports VFS. Table I shows the ( $v, f$ ) pairs supported by XScale. The ( $v_1, f_1$ ) is the peak ( $v, f$ ) pair and ( $v_9, f_9$ ) is the least. The BTB Energy Reduction Algorithm with VFS Algorithm takes  $MB_l$  as input and generates  $TMB_l$  as output, for  $1 \leq l \leq m$ . The VFS Algorithm scales down the ( $v, f$ ) to minimize energy consumed by  $MB$  and the execution of  $TMB$  finishes within the *deadline*, i.e.,  $T_{translated} \leq \text{deadline}$ . Where, *deadline* =  $T_{linear}$  is execution time of  $MB$  which is a  $B_{linear}$ .  $T_{translated}$  is the execution time of  $TMB$  which is based on either  $B_{binary}$  or  $B_{hash}$ . It may be noted that the voltage–frequency



**Fig. 2.** Agenda of the present work.

**Table I.** Voltage–frequency pairs supported by XScale.

$i$	$v_i$ (Volt)	$f_i$ (MHz)
1	1.5	733
2	1.4	666
3	1.3	600
4	1.2	533
5	1.1	466
6	1.1	400
7	1.0	333
8	1.0	266
9	1.0	200

pairs supported XScale processor have limited number of discrete values. As a consequence, the chosen voltage–frequency pair for a particular  $TMB$  may not fully utilize the slack, i.e., the difference between ( $T_{linear} - T_{translated}$ ). This can be used to achieve small enhancement in performance of the  $TMB$  along with energy efficiency provided by the chosen voltage–frequency pair. This work is applicable to  $MB$  where the estimation of time taken and energy consumed to jump to  $BD_j$  and execute  $BC_j$  can be done at compile time.

The proposed scheme is simulated on XEEMU<sup>7,8</sup> which simulates Intel's XScale processor. The related works are discussed in Section 2. Section 3 illustrates the proposed scheme with illustrative examples and explains the application of VFS. Section 4 describes the experimental setup and evaluates the proposed scheme with benchmark programs. Section 5 concludes the present work with its future scopes.

## 2. RELATED WORKS

The past works on BTB energy/energy reduction were implemented either by hardware or by software. Both techniques concentrated on the reduction of BTB access.

### 2.1. Hardware Techniques

In Ref. [9] Deris et al. introduced Speculative BTB Access (SABA), to identify cycles where there is no control flow instruction among those fetched, at least one cycle in advance. By identifying such cycles and eliminating unnecessary BTB accesses BTB energy reduction varies between 6–15% with an average performance loss of 1.5%.

In Ref. [10] the non-necessary accesses to BTB are reduced by taking into account this fact that there exists distances between different consecutive branch instructions. This method decides the access to BTB by a constant value and a counter. After an instruction entrance, the BTB is accessed if the counter is zero, and if the instruction is a branch instruction and exists in the BTB the counter is reset. The approach achieves BTB energy saving by 25%.

In Ref. [11] the authors introduced the use of a static BTB that achieves the similar performance to the traditional branch target buffer but which eliminates most of

the state updates thus reducing the energy consumption of the BTB significantly. They also introduce a correlation based static prediction scheme into a dynamic branch predictor so that those branches that can be predicted statically or can be correlated to the previous ones will not go through normal prediction algorithm. This reduces the activities and conflicts in the branch history table. It saves 43.9% energy of the branch prediction unit without degradation of performance.

Hu et al. in Ref. [12] proposed two approaches to reduce BTB accesses. The first approach expects the distance of every two dynamic branch instructions to be a constant  $N$ , where  $N$  can be statically profiled, and forces BTB to response for  $N$  instructions after a BTB hit. The second approach dynamically predicts the address of the next branch instruction, and accesses BTB only on the predicted address. This reduces 22.033% of useless BTB access.

In Ref. [13] the authors studied two mechanisms that reduce dynamic energy dissipation. The first one is a serial-BTB configuration. The second mechanism is the filter-BTB, a combination of a low energy counting Bloom filter placed in front of a conventional BTB. They also studied the effect of placing a small 32 entry direct-mapped BTB, functioning as a bypass, in parallel with the first two mechanisms. The filter-BTB reduces the number of lookups relative to a conventional BTB and the dynamic energy dissipated. The serial-BTB variant only accesses the data array of the BTB upon a hit, therefore for most of the accesses the actual energy dissipated is only what is dissipated by accessing the tag array. The bypass is used in parallel to either the filter-BTB or the serial-BTB and reduces the performance cost by providing a low latency response in case of a hit. By integrating these mechanisms into a BTB design the scheme achieved an average reduction of 51% in the dynamic energy dissipation of the BTB. These benefits come at a small performance cost that is on average slightly less than 1.2%.

In Ref. [14] Kahn et al. investigated three architectural methods to reduce the leakage energy dissipated by the BTB data array. The first method (called here window) periodically places the entire BTB data array into drowsy mode. A drowsy entry is woken up by the first access in the time interval and remains active for the remainder of the interval (window). There is an associated performance loss which is related to the size of the window, since there is a delay when a specific line must be woken up. The second method, awake line buffer (ALB), limits the number of active BTB entries to a predetermined maximum. While this reduces energy dissipation it comes with a performance penalty that is relative to the size of the buffer. ALB, however, reduces the energy dissipation of the data array more than the window method. The third method, 2-level ALB (2L-ALB), uses a two level buffer with the identical number of combined entries as the previous method. This method exploits the fact that many branches operate numerous times in a fixed sequence.

By predicting the next BTB access, 2L-ALB achieves further reduction in leakage energy without incurring any further performance loss, compared to the ALB method.

Levison et al. in Ref. [15] proposed two BTB designs that fit the tight energy budgets of embedded processors. In the first design, the energy consumption of a single BTB access is reduced by reading only the lower part of the predicted target address bits. This design has energy savings of up to 25% dynamic energy, with effectively no performance degradation. In the second design, they avoid redundant BTB accesses to the same set by using a small buffer that holds the most recently accessed set. This design results in 75% dynamic energy savings at the cost of up to 0.64% system slowdown in a 2-way BTB, and 80% dynamic energy savings at the cost of up to 0.58% system slowdown in a 4-way BTB.

In Ref. [16] Baniyadi et al. introduced branch predictor prediction (BPP) which reduces branch prediction energy dissipation by selectively turning on and off two of the three tables used in the combined branch predictor BPP which relies on a small buffer that stores the addresses and the sub-predictors used by the most recent branches executed. They refer to this buffer to decide if any of the sub-predictors and the selector could be gated without harming performance. They show that on the average and for an 8-way processor, BPP can reduce branch prediction energy dissipation by 28% and 14% compared to non-banked and banked 32 k predictors respectively. This comes with a negligible impact on performance (1% max).

The authors in paper Ref. [17] proposed to use the loop cache to reduce static energy consumption as well as dynamic one. They combined it with CMOS circuits having sleep mode, and thus instruction cache can go to sleep mode when the loop cache is active. They also apply the technique to branch target buffer, and its static and dynamic energy consumption is reduced by up to 40.4% and 40.7%, respectively.

In Ref. [18] Tomas et al. analyzes at what extent tag and target address lengths could be reduced to benefit both dynamic and static energy consumption, silicon area, and access time, while sustaining performance. The tag length and the target address could be reduced by about a half and one byte, respectively with no performance losses. BTB energy savings can reach about 35%.

Levison et al. in Ref. [19] propose a novel micro-architectural method referred to as Shifted-Index BTB with a Set-Buffer, which reduces both dynamic and static energy. It achieves up to 80% reduction in dynamic energy is achieved at the cost of up to 0.64% system slowdown. 58% reduction in static energy is also achieved by applying low-leakage energy techniques that mesh well with the Set-Buffer design.

In Ref. [20] Deris et al. introduce Branchless Cycle Prediction (BLCP) which predicts cycles where there is no branch instruction among those fetched, at least one cycle in advance. They avoid accessing BTB during such cycles.

By using BLCP, it is possible to reduce BTB energy dissipation by 32% while paying a negligible performance cost (average: 0.2%).

The paper Ref. [21] proposes an energy-aware branch predictor by accessing the BTB selectively. To enable the selective access to the BTB, the PHT (Pattern History Table) in the proposed branch predictor is accessed one cycle earlier than the traditional PHT if the program is executed sequentially without branch instructions. As a side effect, two predictions from the PHT are obtained through one access to the PHT, resulting in more energy savings. In the proposed branch predictor, if the previous instruction was not a branch and the prediction from the PHT is untaken, the BTB is not accessed to reduce energy consumption. If the previous instruction was a branch, the BTB is always accessed, regardless of the prediction from the PHT, to prevent the additional delay/accuracy decrease. The proposed branch predictor reduces the energy consumption by 29–47% with little hardware overhead, not incurring additional delay and never harming prediction accuracy.

Briejer et al. in Ref. [22] proposed energy-efficient dynamic branch predictors for the Cell SPE, which normally depends on compiler-inserted hint instructions to predict branches. The prediction scheme predecodes instructions when they are fetched from the local store and accesses the BTB only for branch instructions, thereby saving energy compared to conventional dynamic predictors that access the BTB for every instruction. The authors also introduce branch warning instructions which initiate branch prediction before the actual branch instruction is fetched. This allows fetching the instructions starting at the branch target and thus completely removes the branch penalty for correctly predicted branches. For a 256-entry BTB, a speedup of up to 18.8% is achieved. The energy consumption of the branch prediction schemes is estimated at 1% or less of the total energy dissipation of the SPE and the average energy-delay product is reduced by up to 6.2%.

## 2.2. Software Techniques

Software techniques like loop unrolling and loop fusion reduce BTB access as well as BTB energy consumption. In Ref. [23] Yang et al. study the impact of loop optimizations such as loop unrolling and software pipelining in terms of performance and energy tradeoffs. Zhu et al. in Ref. [24] consider the effect of loop fusion on energy. Loop fusion combines corresponding iterations of different loops. It decreases program run time increasing instruction per cycle (IPC), by reducing loop overhead. The fusion-induced improvements in program energy are slightly smaller than improvements in program run time. If IPC is held constant, however, by reducing frequency and voltage—particularly on a processor with multiple clock domains then energy improvements may significantly exceed run time improvements. They demonstrate energy

savings ranging from 7–40%, with run times ranging from 1% slowdown to 17% speedup.

## 3. PRESENT WORK

The present work proposes BTB Energy Reduction Algorithm which takes  $MB_i$  as input and produces  $TMB_i$  as output. Figure 3(a) shows the format of an  $MB_i$ . Here  $MB_i$  is a  $B_{linear}$  enclosed in a loop, which executes  $p$  times, where  $p \geq 1$ .  $B_{linear}$  contains a multiway branch construct having  $n$  branch destinations. In other words,  $B_{linear}$  can be considered as an *if-then-else ladder* having  $n$  branch destinations. The proposed scheme applies VFS. The VFS\_Algorithm finds the opportunity to scale down  $(v, f)$  of  $TMB_i$ . Table II shows the two cases of VFS algorithm. These cases are based on the input dependency of  $p$ , where,  $p$  is the number of times the  $MB_i$  will execute. The value of  $p$  is input dependent means  $p$ 's value is obtained at runtime as an input. If  $p$  is input independent, then its value is always a constant. The proposed scheme considers two different forms of VFS algorithm. Figures 3(b) and (c) show the format of the  $TMB$  produced by different forms of VFS algorithm. The variable  $min\_vf\_pair$  ( $1 < min\_vf\_pair \leq 9$ ) in Figure 3(c) implies that execution of  $TMB$  at  $(v_{min\_vf\_pair}, f_{min\_vf\_pair})$  will minimize the energy consumed by it. In Figure 3(c)  $P[min\_vf\_pair]$ ,  $P[min\_vf\_pair-1]$ ,  $P[min\_vf\_pair-2], \dots, P[2]$  are the minimum values

```

for(x = 1; x ≤ p; x++)
{
  Blinear
}
(a) Format of MB code

setFrequency(min_vf_pair);
setVoltage(min_vf_pair);
for(x = 1; x ≤ p; x++)
{
  Btransformed
}
setVoltage(1);
setFrequency(1);
(b) Format of TMB code for case A

if(p ≥ P[min_vf_pair]) then
{
  setFrequency(min_vf_pair);
  setVoltage(min_vf_pair);
}
else
if(p ≥ P[min_vf_pair - 1]) then
{
  setFrequency(min_vf_pair - 1);
  setVoltage(min_vf_pair - 1);
}
else
if(p ≥ P[min_vf_pair - 2]) then
{
  setFrequency(min_vf_pair - 2);
  setVoltage(min_vf_pair - 2);
}
else
...
else
if(p ≥ P[2]) then
{
  setFrequency(2);
  setVoltage(2);
}
for(x = 1; x ≤ p; x++)
{
  Btransformed
}
if(p ≥ P[2]) then
{
  setVoltage(1);
  setFrequency(1);
}
(c) Format of TMB code for case B

```

Fig. 3. Format of the multiway branch (MB) and translated multiway branch (TMB) codes.

**Table II.** Input dependency.

Case	$p$	VFS_Algorithm
A	Input independent	VFS_Algorithm_A
B	Input dependent	VFS_Algorithm_B

of  $p$  required to execute  $TMB_i$  at voltage–frequency pairs  $(v_{min\_vf\_pair}, f_{min\_vf\_pair})$ ,  $(v_{min\_vf\_pair-1}, f_{min\_vf\_pair-1})$ ,  $(v_{min\_vf\_pair-2}, f_{min\_vf\_pair-2})$ ,  $\dots$ ,  $(v_2, f_2)$ , respectively. The subroutines *setVoltage* and *setFrequency* helps to scale up and scale down the  $(v, f)$  pair at runtime.

### 3.1. Illustrative Examples

To demonstrate the efficacy of the approach, three illustrative examples are provided in this section. In the illustrative example *EX1* the *MB* can be implemented as  $B_{linear}$ ,  $B_{hash}$ , or  $B_{binary}$ . For the illustrative example *EX2* compilers generate  $B_{linear}$ . It is hard to implement  $B_{hash}$  for *EX2*. In this case,  $k$ – $d$  tree<sup>6</sup> is used to implement  $B_{binary}$  for *EX2*. The illustrative example 3 *EX3* deals with an *MB* where the index variables and values are strings. The branching takes place on string matching. The compilers generate  $B_{linear}$  for such *MBs*. Here it introduces the use of pattern matcher to generate time and energy efficient  $B_{pattern}$  code for *EX3*. The assembly language used in this paper is based on the instruction set of XScale processor. The assembly language codes for  $B_{linear}$  and  $B_{hash}$  are generated by *xscale-gcc-elf* compiler. The  $B_{binary}$  and  $B_{pattern}$  codes are generated by traversal of  $k$ – $d$  tree and pattern matcher graph, respectively. The experimental values in Tables III–V are obtained by executing the possible  $B_{linear}$ ,  $B_{hash}$ ,  $B_{binary}$  and  $B_{pattern}$  implementations of the illustrative examples on XEEMU simulator. These tables use the

following metrics to compare the different energy and performance implementations of the illustrative examples:

(i) ‘Time’ is the total execution time taken of the program in seconds (sec),

(ii) ‘Total Energy’ is the energy consumed by the program in Joules (J),

(iii) ‘BTB Energy’ is the energy consumed by the BTB during the execution of the program micro Joules ( $\mu$ J).

The tables also show the performance and energy gained by  $B_{hash}$ ,  $B_{binary}$  and  $B_{pattern}$  implementations with respect to  $B_{linear}$  in percentage (%). The tables also compare the following BTB parameters:

(i) ‘Total branches’ is the total number of branch instructions executed in the program,

(ii) ‘Miss prediction taken’ is the total number wrong predictions taken by the Branch Prediction Unit (BPU) when a branch takes place,

(iii) ‘Miss prediction not taken’ is the total number wrong predictions taken by the BPU when no branch takes place,

(iv) ‘Non prediction taken’ is the total number of branches taken when no predictions are taken by the BPU because the BTB has no entry for the branch history and target addresses of the corresponding branch instructions.

#### 3.1.1. Illustrative Example 1 (*EX1*)

*EX1* considers a simple *MB* which can implemented as *if-then-else* and *switch-case*, as shown in Figures 4(a) and (b), respectively. Here, ‘marks’ is the index variable that forms the index expression. The matching value set for index variable marks is *value* (marks) = {4, 5, 6, 7, 8, 9, 10}. The GCC compiler *xscale-gcc-elf* translates the source code in Figure 4(a) to  $B_{linear}$  code. For the source code in Figure 4(b) the *xscale-gcc-elf* generates  $B_{hash}$  code.

**Table III.** *EX1* results.

<i>EX1</i> code	Metric	Value	Gain (%)	BTB parameter	Value
$B_{linear}$ at $(v_1, f_1)$	Time (sec)	0.0832	–	Total branches	8999968
	Total energy (J)	0.0616	–	Miss predictions taken	56
	BTB energy ( $\mu$ J)	353.08	–	Miss predictions not taken	18
$B_{hash}$ at $(v_1, f_1)$	Time (sec)	0.0450	45.91	Non prediction taken	11
	Total energy (J)	0.0338	45.12	Total branches	3000116
	BTB energy ( $\mu$ J)	117.67	66.67	Miss predictions taken	36
$B_{hash}$ at $(v_5, f_5)$	Time (sec)	0.0707	15.02	Miss predictions not taken	4
	Total energy (J)	0.0169	72.56	Non prediction taken	81
	BTB energy ( $\mu$ J)	47.71	86.48	Total branches	3000116
$B_{binary}$ at $(v_1, f_1)$	Time (sec)	0.0477	42.66	Miss predictions taken	36
	Total energy (J)	0.0359	41.72	Miss predictions not taken	4
	BTB energy ( $\mu$ J)	274.62	22.22	Non prediction taken	81
$B_{binary}$ at $(v_5, f_5)$	Time (sec)	0.0750	9.85	Total branches	7000076
	Total energy (J)	0.0179	70.94	Miss predictions taken	49
	BTB energy ( $\mu$ J)	111.31	68.47	Miss predictions not taken	12
				Non prediction taken	11

**Table IV.** EX2 results.

EX2 code	Metric	Value	Gain (%)	BTB parameter	Value
$B_{linear}$ at $(v_1, f_1)$	Time (sec)	0.0560		Total branches	8008955
	Total energy (J)	0.0411	–	Miss predictions taken	1085
	BTB energy ( $\mu$ J)	314.225	–	Miss predictions not taken	56
				Non prediction taken	11
$B_{binary}$ at $(v_1, f_1)$	Time (sec)	0.0273	51.25	Total branches	5008198
	Total energy (J)	0.0213	48.17	Miss predictions taken	3071
	BTB energy ( $\mu$ J)	196.578	37.44	Miss predictions not taken	2040
				Non prediction taken	11
$B_{binary}$ at $(v_5, f_5)$	Time (sec)	0.0430	23.21	Total branches	5008198
	Total energy (J)	0.0106	74.20	Miss predictions taken	3071
	BTB energy ( $\mu$ J)	79.682	74.64	Miss predictions not taken	2040
				Non prediction taken	11

This depends on the ability of the compiler to find a possible hash function. Sometimes it is not possible to find a hash function. However, it is always possible to generate a  $B_{binary}$  code for a  $MB$ . The  $MB$  in EX1 can be translated to  $B_{binary}$  code as shown in Figure 19, in Appendix A. Figure 5 shows the binary search tree formed with all possible values to be matched with index variable.  $B_{binary}$  is generated by preorder traversal of the binary search tree. For a  $MB$  with  $n$  branch destinations belonging to the class of EX1,  $B_{linear}$  will take  $O(n)$  time to jump to a branch destination. While  $B_{hash}$  and  $B_{binary}$  will take  $O(1)$  and  $O(\log_2 n)$  time, respectively. The  $B_{linear}$ ,  $B_{hash}$ , and  $B_{binary}$  codes of EX1 are shown in the Appendix A. Table III compare the energy and performance of the different implementations of the EX1 and show the values of the BTB parameters. It also shows the energy and performance gained by  $B_{hash}$  and  $B_{binary}$  with respect to  $B_{linear}$ . The execution time of  $B_{linear}$  at  $(v_1, f_1)$  is considered as the *deadline* for  $B_{hash}$  and  $B_{binary}$  to finish execution. VFS is applied to  $B_{hash}$  and  $B_{binary}$  to minimize energy consumption.

### 3.1.2. Illustrative Example 2 (EX2)

The  $MB$  in Figure 6 is an *if-then-else ladder* which performs a two-dimensional range testing. The *if-then-else ladder* contains three branch destinations  $BD_1$ ,  $BD_2$  and  $BD_3$  for the blocks of code ‘ $z = 1$ ,’ ‘ $z = 2$ ’ and

‘ $z = 3$ ,’ respectively. When none of the conditions in the *if-then-else ladder* are satisfied, the control jumps to a branch destination NEXT. For such  $MB$  it is hard for a compiler to generate  $B_{hash}$  code. Compilers generate  $B_{linear}$  code for this type of  $MB$ , which is inefficient in terms of energy and performance. The present work introduces that it is possible to generate  $B_{binary}$  code for such  $MB$ s. This is done with the help of  $k-d$  tree.<sup>6</sup>  $k-d$  tree is a multidimensional binary search tree. The matching value set for index variable ‘ $x$ ’ is the  $value(x) = \{3, 5, 6, 12, 13, 16\}$ . The matching value set for index variable ‘ $y$ ’ is  $value(y) = \{1, 3, 4, 7, 8, 12\}$ . The ordered pair set or point set of matching values is  $value(x, y) = \{(3, 1), (3, 3), (5, 1), (5, 3), (6, 4), (6, 7), (12, 4), (12, 7), (13, 8), (13, 12), (16, 8), (16, 12)\}$ , as obtained from the source code in Figure 6. The  $k-d$  tree decomposition for the point set  $value(x, y)$  (as shown in Fig. 7) is done with the help of Bentley’s approach in Ref. [6]. The resulting  $k-d$  tree for the point set  $value(x, y)$  is shown in Figures 8. In Figure 7 lines  $l_3, l_7, l_{10}$  and  $l_{14}$  encloses the region related to  $BD_1$ . The lines  $l_9, l_6, l_{13}$  and  $l_1$  enclose the region related to  $BD_2$ . The lines  $l_8, l_{12}, l_2$  and  $l_4$  enclose the region related to  $BD_3$ . The rest of the regions are related to NEXT. Each non-leaf node of the  $k-d$  tree has left and right edges which connects it to its left and right subtrees, respectively.

**Table V.** EX3 results.

EX2 code	Metric	Value	Gain (%)	BTB parameter	Value
$B_{linear}$ at $(v_1, f_1)$	Time (sec)	0.7771	–	Total branches	71933373
	Total energy (J)	0.5909	–	Miss predictions taken	3866738
	BTB energy ( $\mu$ J)	2944.25	–	Miss predictions not taken	3666680
				Non prediction taken	8600003
$B_{pattern}$ at $(v_1, f_1)$	Time (sec)	0.6695	13.84	Total branches	33133409
	Total energy (J)	0.4969	15.90	Miss predictions taken	3466753
	BTB energy ( $\mu$ J)	1532.97	47.93	Miss predictions not taken	1066672
				Non prediction taken	7866669
$B_{pattern}$ at $(v_5, f_5)$	Time (sec)	0.7364	5.23	Total branches	33133409
	Total energy (J)	0.4246	28.14	Miss predictions taken	3466753
	BTB energy ( $\mu$ J)	1267.61	56.94	Miss predictions not taken	1066672
				Non prediction taken	7866669

```

int main()
{
  int s, marks;
  char grade;
  for(s=0; s<1000000; s++)
  {
    marks=s/10;
    if(marks==10)
      grade='X';
    else
    if(marks==9)
      grade='X';
    else
    if(marks==8)
      grade='A';
    else
    if(marks==7)
      grade='B';
    else
    if(marks==6)
      grade='C';
    else
    if(marks==5)
      grade='D';
    else
    if(marks==4)
      grade='P';
    else
      grade='F';
  }
  return 0;
}

```

(a) Source code of MX1 containing if-then-else ladder

```

int main()
{
  int s, marks;
  char grade;
  for(s=0; s<1000000; s++)
  {
    marks=s/10;
    switch(marks)
    {
      case 10: grade='X';
      break;
      case 9: grade='X';
      break;
      case 8: grade='A';
      break;
      case 7: grade='B';
      break;
      case 6: grade='C';
      break;
      case 5: grade='D';
      break;
      case 4: grade='P';
      break;
      default: grade='F';
    }
  }
  return 0;
}

```

(b) Source code of MX1 containing switch-case statement

Fig. 4. Two possible source codes of EX1.

The left edge is either labeled with the symbol ' $<$ ' or with ' $\leq$ '. The right edge is either labeled with the symbol ' $>$ ' or with ' $\geq$ '. The left and right edge symbols of a node depend on the source code. For example, the left edge symbol of the node  $l_1$  is ' $<$ ' and its right edge symbol is ' $\geq$ '. This is because in the source code in Figure 6 there is an expression ' $x \geq 6$ ' and  $l_1$  is the line representing ' $x = 6$ '. So for any node with ' $x \geq 6$ ' will be in the right subtree of  $l_1$ , while nodes with ' $x < 6$ ' will be in the left subtree of  $l_1$ . The leaf nodes of the  $k-d$  tree contain the branch destinations. The leaf nodes  $BD_1$ ,  $BD_2$ , and  $BD_3$  contain the branch destinations for the blocks of code ' $z = 1$ ', ' $z = 2$ ' and ' $z = 3$ ', respectively. The rest of the leaves contain NEXT as branch destination. There are

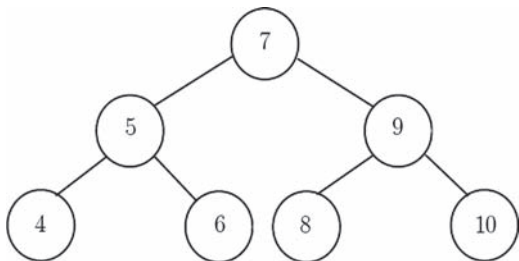


Fig. 5. Binary search tree for EX1.

two kinds of non-leaf  $k-d$  tree nodes considered in this work. The circular non-leaf nodes are the mandatory nodes required to form the  $k-d$  tree. The square non-leaf node ensures that a branch destination is enclosed within the desired region. For example in Figure 7 the lines  $l_{12}$ ,  $l_{13}$  and  $l_{14}$  provides enclosure for the regions related to  $BD_3$ ,  $BD_2$ , and  $BD_1$ , respectively. To jump to  $BD_3$ , the following

```

int main()
{
  int x, y, z;
  for(x=0; x<1000; x++)
  {
    for(y=0; y<1000; y++)
    {
      if((x>=13)&&(x<=16)&&(y>=8)&&(y<=12))
        z=1; // BD1
      else
      if((x>=6)&&(x<=12)&&(y>=4)&&(y<=7))
        z=2; // BD2
      else
      if((x>=3)&&(x<=5)&&(y>=1)&&(y<=3))
        z=3; // BD3
    }
  }
  return 0;
}

```

Fig. 6. Source code of EX2 as if-then-else ladder.

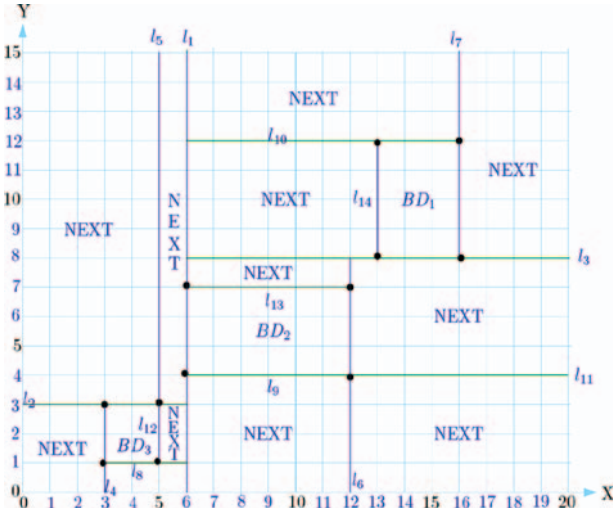


Fig. 7.  $k$ - $d$  tree decomposition for the point set  $value(x, y)$ .

sequences of conditions are to be satisfied, ‘ $x < 6$ ,’ ‘ $y < 3$ ,’ ‘ $x \geq 3$ ,’ ‘ $y \geq 1$ ’ and ‘ $x \leq 15$ ’. But, the conditions ‘ $x < 6$ ’ and ‘ $x \leq 5$ ’ are redundant because ‘ $x$ ’ is an integer variable. The node  $l_{12}$  can be deleted to obtain the modified  $k$ - $d$  tree in Figure 9. Similarly,  $l_{13}$  can also be deleted.

In Figure 8 all the leaves of the right subtrees of the nodes  $l_2$  and  $l_6$  contain NEXT. Each of these subtrees are pruned and replaced with a leaf node containing NEXT as

shown in Figure 9. Figure 10 shows two possible assembly language implementations of the *if-then-else ladder* in EX2. These assembly language code fragments are written using ARM instruction set.  $B_{linear}$  in Figure 10(a) is a brute-force implementation.  $B_{binary}$  in Figure 10(b) is obtained by a preorder traversal of the modified  $k$ - $d$  tree in Figure 9. The preorder traversal algorithm of the  $k$ - $d$  tree in Figure 9 is shown in Appendix C.

The detailed  $B_{linear}$  and  $B_{binary}$  implementations of EX2 are shown in Figures 20 and 21, respectively, in Appendix B. For a MB with  $n$  branch destinations belonging to the class of EX2 having  $d$  distinct index variables in each of the  $n$  index expressions,  $B_{linear}$  will take  $O(2 \times d \times n)$  time to jump to a branch destination. While  $B_{binary}$  will take  $O(\log_2 n + d + 1)$  time, where  $d$  is the dimension of the  $k$ - $d$  tree. In EX2  $d = 2$ . Table IV compares the energy and performance of the different implementations of EX2 and shows the values of BTB parameters. It also shows the gain achieved by  $B_{binary}$  with respect to  $B_{linear}$ . The execution time of  $B_{linear}$  at  $(v_1, f_1)$  is considered as the  $T_{linear}$ , which is the deadline for  $B_{binary}$  to finish execution. VFS is applied to  $B_{binary}$  to minimize energy consumption maintaining the constraint  $T_{binary} \leq T_{linear}$ . Table IV shows the maximum gain in BTB energy achieved by  $B_{binary}$  is 74.64% along with a performance gain of 23.21%, when  $B_{binary}$  is executed at  $(v_5, f_5)$ .

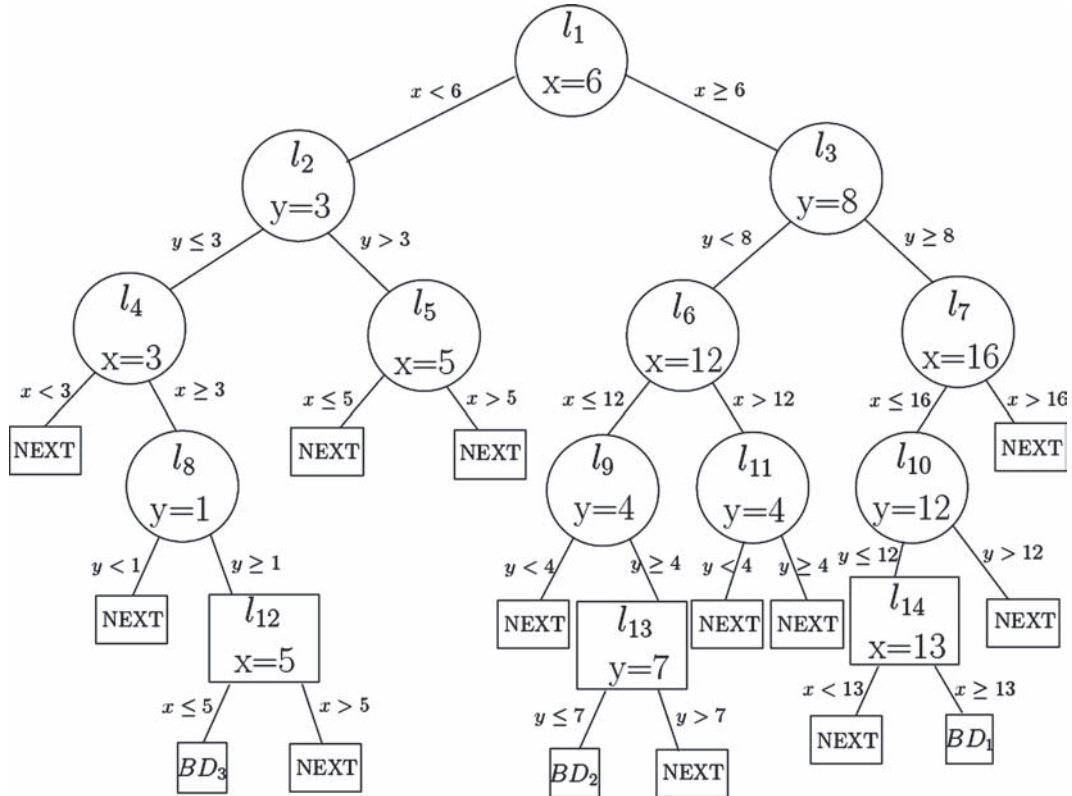


Fig. 8. The resulting  $k$ - $d$  tree for the point set  $value(x, y)$ .



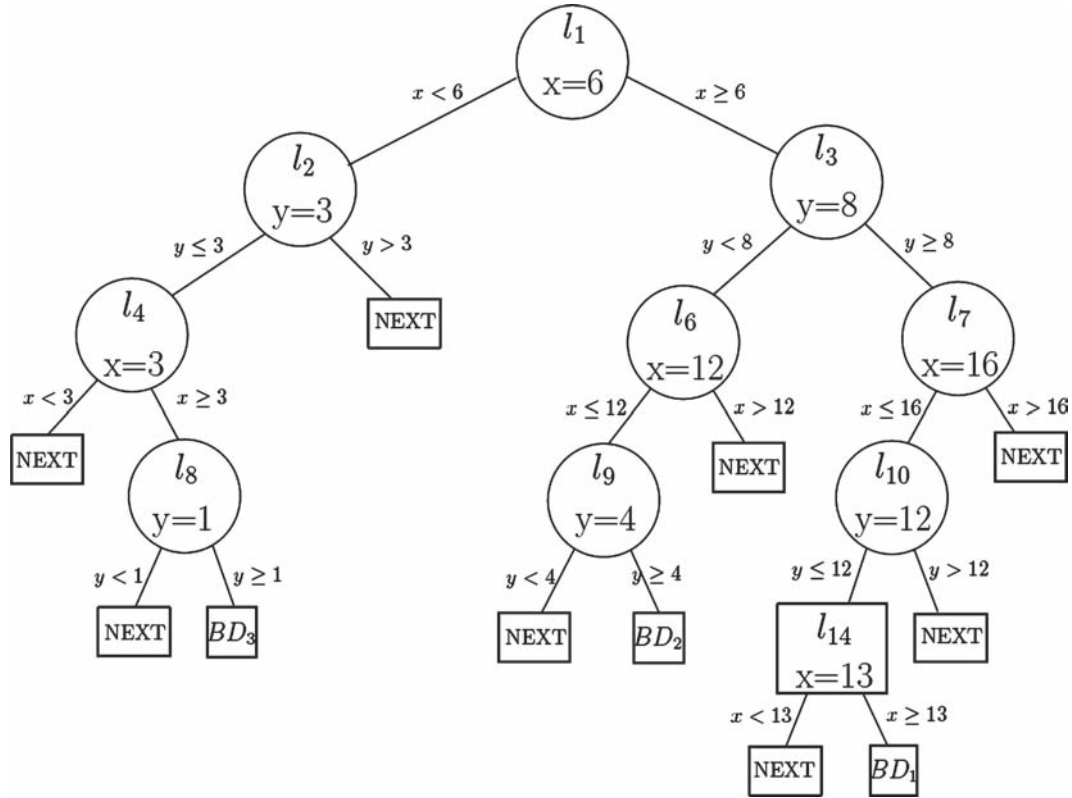


Fig. 9. Modified  $k$ - $d$  tree of the for the point set  $value(x, y)$ .

### 3.1.3. Illustrative Example 3 (EX3)

Programming languages like Ruby provides multiway branch with strings as shown in Figure 11.  $B_{linear}$  implementations of these multiway branches are inefficient in terms of time and energy. The pattern matcher in form of a finite state machine in Figure 11 can help to generate  $B_{pattern}$  which is both energy and time efficient. The matching value set for index variable ‘month’ is  $value(month) = \{“JANUARY,” “FEBRUARY,” “MARCH,” “APRIL,” “MAY,” “JUNE,” “JULY,” “AUGUST,” “SEPTEMBER,” “OCTOBER,” “NOVEMBER,” “DECEMBER”\}$ .  $B_{pattern}$  is generated by breadth first traversal of the pattern matcher graph.  $B_{pattern}$  makes use of a data structure called trie (or prefix-tree) to restrict the state transition time while pattern matching to  $O(1)$ . Table V shows the energy-performance gain, and the BTB parameters of the  $B_{linear}$  and  $B_{pattern}$ , respectively.  $B_{pattern}$  takes  $O(\psi)$  time to reach a  $BD$ , where  $\psi$  is the maximum external path length of the pattern matcher graph. The execution time of  $B_{linear}$  at  $(v_1, f_1)$  is considered as the *deadline* for  $B_{pattern}$  to finish execution.

## 3.2. BTB Energy Reduction Algorithm

This algorithm takes  $MB_l$  as input and produces  $TMB_l$  as output. The  $MB_l$  taken as input is considered to be implemented as  $B_{linear}$  code.  $B_{translated}$  code in  $TMB_l$  is either a  $B_{hash}$  code or a  $B_{binary}$  code or a  $B_{pattern}$  code. After

translating the code from  $B_{linear}$  code to  $B_{hash}$  or  $B_{binary}$  or  $B_{pattern}$ , the algorithm finds the possibility of VFS. On the basis of input dependency of  $p$  as shown in Table II the desired VFS algorithm is called. The VFS algorithm scales down the  $(v, f)$  to minimize the energy consumed by  $TMB_l$  such that  $T_{translated} \leq deadline$ .

### BTB\_Energy\_Reduction\_Algorithm

1. {
2. Given a  $B_{linear}$  as input;
3. if ( $B_{linear}$  can be translated to its equivalent  $B_{hash}$ )
4. then
5.  $B_{translated} := B_{hash}$ ;
6. else
7. if ( $B_{linear}$  can be translated to its equivalent  $B_{binary}$ )
8. then
9.  $B_{translated} := B_{binary}$ ;
10. else
11. if ( $B_{linear}$  can be translated to its equivalent  $B_{pattern}$ )
12. then
13.  $B_{translated} := B_{pattern}$ ;
14. else
15. goto 17;
16. if ( $p$  is input dependent) then
17. Call VFS\_Algorithm  $B(B_{linear}, B_{translated})$ ;
18. else
19. Call VFS\_Algorithm  $A(B_{linear}, B_{translated})$ ;
20. }

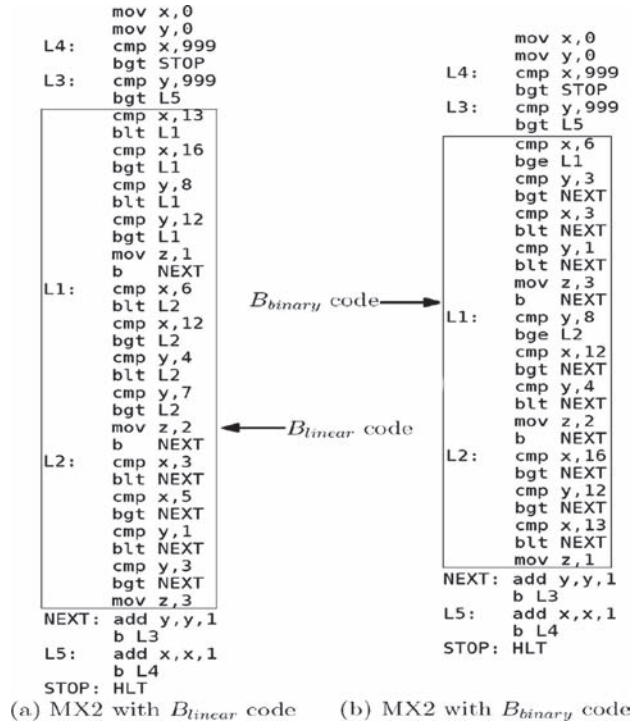


Fig. 10. Assembly language codes representing if-then-else ladder in EX2.

### 3.3. VFS\_Algorithm

This subsection explains the VFS algorithms in detail. The VFS algorithms find the value of  $min\_vf\_pair$ . The  $min\_vf\_pair$  is the  $(v, f)$  that minimizes the energy consumed by  $TMB_i$ . The VFS algorithms calculates the energy overhead ( $E_{overhead}$ ) and time overhead ( $t_{overhead}$ ) due to VFS. They are calculated using the following formulae.<sup>25</sup> Overheads when switching from  $(v_i, f_i)$  to  $(v_w, f_w)$

$$E_{overhead}(i, w) = (1 - \mu) \times C \times |V_i^2 - V_w^2| \quad (1)$$

$$t_{overhead}(i, w) = 2 \times \frac{C}{I_{MAX}} \times |V_i^2 - V_w^2| \quad (2)$$

where,  $\mu$  is the energy efficiency of the energy regulator which is considered as 90%,  $C$  is the voltage regulator's capacitance to be  $10 \mu\text{F}$ ,  $I_{MAX}$  is the maximum current allowed which is assumed to be 1 A and  $1 \leq w \leq 9$ . The VFS algorithms make use of a C library function *sprintf* which prints a formatted output to the string  $S$ . The subroutine generate code generates the assembly equivalent of the high-level code in  $S$  and inserts it to the target program file.

#### 3.3.1. VFS\_Algorithm\_A

VFS\_Algorithm\_A finds the possibility of VFS to save energy of  $TMB_i$  when  $p$  is input independent.

$VFS\_Algorithm\_A(B_{linear}, B_{translated})$

1. {
2. char  $S[50]$ ;
3.  $p := \text{constant value fixed in compile time}$ ;
4.  $T_{linear} := \frac{1}{n} \times \sum_{j=1}^n (t_{linear\_j} + t_{branch\_exe\_j}) \times p$ ;
5.  $E_{linear} := \frac{1}{n} \times \sum_{j=1}^n (e_{linear\_j} + e_{branch\_exe\_j}) \times p$ ;
6.  $deadline := T_{linear}$ ;
7.  $E_{min} := E_{linear}$ ;
8.  $min\_vf\_pair := 1$ ;
9. for( $i := 1$ ;  $i \leq 9$ ;  $i++$ )
10. {
11.  $T[i] := 2 \times t_{overhead}(1, i) \times \frac{1}{n}$   
 $\times \sum_{j=1}^n (t_{translated\_ij} + t_{branch\_exe\_ij}) \times p$ ;
12.  $E[i] := 2 \times E_{overhead}(1, i) \times \frac{1}{n}$   
 $\times \sum_{j=1}^n (e_{translated\_ij} + e_{branch\_exe\_ij}) \times p$ ;
13. if ( $T[i] \leq deadline$ ) then
14. {
15. if ( $E[i] < E_{min}$ ) then
16. {

```

names=["XYZ", "JANUARY", "FEBRUARY", "MARCH", "APRIL", "MAY", "JUNE", "123", "JULY",
"AUGUST", "SEPTEMBER", "OCTOBER", "NOVEMBER", "DECEMBER", "ABC"]
for s in 0..1000000
  month=names[s%15]
  case month
  when "DECEMBER", "JANUARY", "FEBRUARY"
    season=5 #BD1
  when "MARCH", "APRIL"
    season=1 #BD2
  when "MAY", "JUNE"
    season=2 #BD3
  when "JULY", "AUGUST", "SEPTEMBER"
    season=3 #BD4
  when "OCTOBER", "NOVEMBER"
    season=4 #BD5
  else
    season=0 #BD6
  end
end

```

Fig. 11. Multiway branch with strings.

```

17.          $E_{min} := E[i];$ 
18.          $min\_vf\_pair := i;$ 
19.     }
20. }
21. }
22. if ( $min\_vf\_pair > 1$ ) then
23. {
24.     sprintf( $S, "setFrequency(%d); setVoltage$ 
           ( $%d$ );",  $min\_vf\_pair, min\_vf\_pair$ );
25.     generate_code( $S$ );
26. }
27. generate_code( $B_{translated}$ );
28. if ( $min\_vf\_pair > 1$ ) then
29. {
30.     sprintf( $S, "setVoltage(1); setFrequency(1);"$ );
31.     generate_code( $S$ );
32. }
33. }

```

Here,  $t_{linear\_j}$  and  $t_{branch\_exe\_j}$  are time taken to jump to  $BD_j$  and execute  $BC_j$  of  $B_{linear}$ , respectively, at  $(v_1, f_1)$ .  $e_{linear\_j}$  and  $e_{branch\_exe\_j}$  are energy consumed to jump to  $BD_j$  and execute  $BC_j$  of  $B_{linear}$ , respectively, at  $(v_1, f_1)$ .  $t_{translated\_ij}$  and  $t_{branch\_exe\_ij}$  are time taken to jump to  $BD_j$  and execute  $BC_j$  of  $B_{translated}$ , respectively, at  $(v_i, f_i)$ .  $e_{translated\_ij}$  and  $e_{branch\_exe\_ij}$  are energy consumed to jump to  $BD_j$  and execute  $BC_j$  of  $B_{translated}$ , respectively at  $(v_i, f_i)$ . In steps 4 and 5,  $T_{linear}$  and  $E_{linear}$  are calculated as  $p$  times the average time taken and  $p$  times the average energy consumed to jump to  $BD_j$  and execute the block of code  $BC_j$  at  $(v_1, f_1)$ . Similarly, for  $B_{translated}$ ,  $T[i]$  and  $E[i]$  are

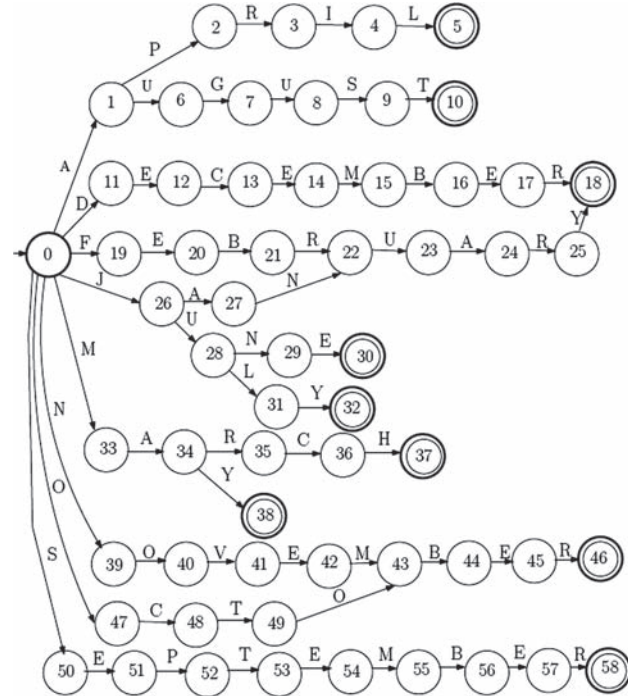


Fig. 12. Pattern matcher for multiway branch with strings (EX3).

calculated in steps 11 and 12. The algorithm finds the value of  $min\_vf\_pair$ , the  $(v, f)$  that will minimize energy consumed by  $TMB_i$  and allow the execution of the  $TMB_i$  to finish within the deadline.

### 3.3.2. VFS\_Algorithm\_B

VFS\_Algorithm\_B finds the possibility of VFS to save energy of  $TMB_i$  when  $p$  is dependent.  $T_{linear}$ ,  $E_{linear}$ ,  $T[i]$  and  $E[i]$  are calculated in a similar way as in VFS\_Algorithm\_A.

VFS\_Algorithm\_B( $B_{linear}$ ,  $B_{translated}$ )

```

1. {
2.   char  $S[50]$ ;
3.    $p := 10^6$ ;
4.   Linked_List linkedlist := null;
5.    $T_{linear} := \frac{1}{n} \times \sum_{j=1}^n (t_{linear\_j} + t_{branch\_exe\_j}) \times p$ ;
6.    $E_{linear} := \frac{1}{n} \times \sum_{j=1}^n (e_{linear\_j} + e_{branch\_exe\_j}) \times p$ ;
7.   deadline :=  $T_{linear}$ ;
8.    $t_{lin\_avg} := \frac{T_{linear}}{p}$ ;
9.    $E_{min} := E_{linear}$ ;
10.   $min\_vf\_pair := 1$ ;
11.  for( $i := 1$ ;  $i \leq 9$ ;  $i++$ )
12.  {
13.     $t_i := \frac{1}{n} \times \sum_{j=1}^n (t_{translated\_ij} + t_{branch\_exe\_ij})$ ;
14.     $T[i] := 2 \times t_{overhead}(1, i) + t_i \times p$ ;
15.     $E[i] := 2 \times E_{overhead}(1, i) \times \frac{1}{n}$ 
16.       $\times \sum_{j=1}^n (e_{translated\_ij} + e_{branch\_exe\_ij}) \times p$ ;
17.    if ( $t_{lin\_avg} > t_i$ ) then
18.    {
19.       $P[i] := \left\lceil \frac{2 \times t_{overhead}(1, i)}{t_{lin\_avg} - t_i} \right\rceil$ ;
20.    }
21.  }
22.  if ( $T[i] \leq \text{deadline}$ ) then
23.  {
24.    if ( $E[i] < E_{min}$ ) then
25.    {
26.       $E_{min} := E[i]$ ;
27.       $min\_vf\_pair := i$ ;
28.      if ( $i > 1$ ) then
29.      {
30.         $L := \text{create\_node}()$ ;
31.         $L \rightarrow vf\_pair := i$ ;
32.        linkedlist.addfirst( $L$ );
33.      }
34.    }
35.  }
36. }

```

```

37.  for(L := linkedlist.header_node();
    L ≠ null; L := L → next_node)
38.  {
39.  printf(S,"if (p ≥ %d){setFrequency(%d);
    setVoltage(%d); }," P[L → vf_pair],
    L → vf_pair, L → vf_pair);
40.  generate_code(S);
41.  if (L→next_node ≠ null) then
42.  {
43.  printf(S,"else");
44.  generate_code(S);
45.  }
46.  last_node := L;
47.  }
48.  generate_code(Btranslated);
49.  if (min_vf_pair > 1) then
50.  {
51.  printf(S,"if (p >= %d){setVoltage(1);
    setFrequency(1); }"; P[last_node→vf_pair]);
52.  generate_code(S);
53.  }
54. }

```

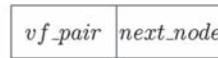
Since,  $p$  is input dependent; its value is not known at compile time. The value of  $p$  is assigned  $10^6$  in step 3. Apart from finding  $min\_vf\_pair$  the algorithm calculates  $P[i]$  for every  $(v_i, f_i)$ .  $P[i]$  is the minimum value of  $p$  required to execute  $TMB_i$  at  $(v_i, f_i)$ . The formula for  $P[i]$  is derived as follows. Let,  $t_{lin\_avg}$  be the average execution time of  $B_{linear}$ , executed once at  $(v_1, f_1)$ . Let,  $t_i$  be the average execution time of  $B_{translated}$ , executed once at  $(v_1, f_1)$ . Steps 8 and 15 of VFS\_Algorithm\_B calculates  $t_{lin\_avg}$  and  $t_i$ , respectively, when,  $t_{lin\_avg} > t_i$ . If  $B_{translated}$  is executed  $P[i]$  times at  $(v_i, f_i)$ , then the time taken to do this should be atmost that of  $P[i]$  time execution of  $B_{linear}$  at  $(v_1, f_1)$ . Considering the overhead of  $(v, f)$  scale up and scale down, this can be written as

$$\begin{aligned}
P[i] \times t_i + 2 \times t_{overhead}(1, i) &\leq P[i] \times t_{lin\_avg} \\
\Rightarrow P[i] \times (t_{lin\_avg} - t_i) &\geq 2 \times t_{overhead}(1, i) \\
\Rightarrow P[i] &\geq \frac{2 \times t_{overhead}(1, i)}{(t_{lin\_avg} - t_i)} \quad (3)
\end{aligned}$$

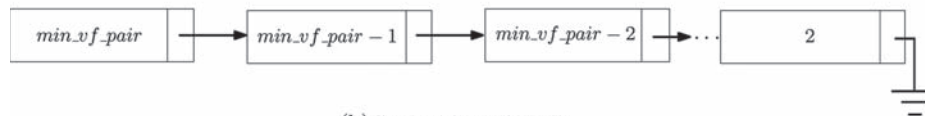
```

struct node
{
    int vf_pair;
    struct node *next_node;
} * L;

```



(a) Structure of node datatype



(b) Linked list of node

The obtained expression of  $P[i]$  is the minimum value of  $p$  required to execute  $TMB_i$  at  $(v_i, f_i)$ . In other words, if the value of  $p$  is obtained at runtime and  $p \geq P[i]$  then  $TMB_i$  can be executed at  $(v_i, f_i)$ . The algorithm also generates a linked list as shown in Figure 13(b). Each node of the linked list is an instance of a node type structure as shown in Figure 13(a). The  $vf\_pair$  field of the header node of the linked list contains the  $min\_vf\_pair$ . The nodes of the linked list are ordered by the value of  $vf\_pair$  field, as  $min\_vf\_pair, min\_vf\_pair-1, min\_vf\_pair-2, \dots$ , and 2, where,  $1 < min\_vf\_pair \leq 9$ . The linked list is arranged in such a manner because  $P[min\_vf\_pair] > P[min\_vf\_pair - 1] > P[min\_vf\_pair - 2] > \dots > P[2] \geq 1$ . The reason behind this is, as  $(v_i, f_i)$  decreases,  $P[i]$  increases. After the formation of the linked list the algorithm generates the  $TMB_i$  shown in Figure 3(b). The utility of the VFS\_Algorithm\_B is explained with the help of an  $MB$  and its equivalent  $TMB$ , as shown in Figure 14. Figure 14 considers  $MB$  and its equivalent  $TMB$ , where  $p$  is input dependent. The  $MB$  in Figure 14(a) contains an *if-then-else ladder* for which compiler generates  $B_{linear}$ .  $TMB$  in Figure 14(b) contains a *switch-case* for which compiler generates  $B_{hash}$ . For simplicity, the codes for  $MB$  and  $TMB$  in Figure 14 are shown in high level language. For the  $TMB$  in Figure 14 VFS\_Algorithm\_B generates the linked list shown in Figure 15. The linked list informs that the  $TMB$  can be run at four different  $(v, f)$  pairs other than  $(v_1, f_1)$ , depending on the value of  $p$ . The value of  $min\_vf\_pair$  is 5. The value of  $t_{lin\_avg}$  is  $0.0832 \mu\text{sec}$ . Table VI shows the values of  $t_i, T_{ov\_i}$  required to calculate  $P[i]$ .  $T_{ov\_i} (= 2 \times t_{overhead}(1, i))$  is the time taken to scale down from  $(v_1, f_1)$  to  $(v_i, f_i)$  and scale up from  $(v_i, f_i)$  to  $(v_1, f_1)$ . Table VI also shows the values of  $T_{MB(v_i, f_i, P[i])}, E_{MB(v_i, f_i, P[i])}, T_{TMB(v_i, f_i, P[i])}$ , and  $E_{TMB(v_i, f_i, P[i])}$ . These values are obtained for experimental verification of VFS\_Algorithm\_B.  $T_{MB(v_i, f_i, P[i])}$  and  $E_{MB(v_i, f_i, P[i])}$  are the time taken and energy consumed, respectively, by the  $MB$  in Figure 14(a), when it is executed at  $(v_i, f_i)$  and  $p = P[i]$ .  $T_{TMB(v_i, f_i, P[i])}$  and  $E_{TMB(v_i, f_i, P[i])}$  are time taken and energy consumed, respectively, by  $TMB$  in Figure 14(b), when it is executed at  $(v_i, f_i)$  and  $p = P[i]$ .  $T_{MB(v_i, f_i, P[i])}$

Fig. 13. Linked list created by VFS\_Algorithm\_B.

```

#include<stdio.h>
int main()
{
  int s,p,marks;
  char grade;
  scanf("%d",&p);
  for(s=0;s<p;s++)
  {
    marks=s/10;
    if(marks==10)
      grade='X';
    else
    if(marks==9)
      grade='X';
    else
    if(marks==8)
      grade='A';
    else
    if(marks==7)
      grade='B';
    else
    if(marks==6)
      grade='C';
    else
    if(marks==5)
      grade='D';
    else
    if(marks==4)
      grade='P';
    else
      grade='F';
  }
  return 0;
}
(a) MB with  $B_{linear}$ 

#include<stdio.h>
#include"dvfs.h"
int main()
{
  int s,p,marks;
  char grade;
  scanf("%d",&p);
  if(p>=4843)
  {
    setFrequency(5);
    setVoltage(5);
  }
  else
  if(p>=2840)
  {
    setFrequency(4);
    setVoltage(4);
  }
  else
  if(p>=2144)
  {
    setFrequency(3);
    setVoltage(3);
  }
  else
  if(p>=1795)
  {
    setFrequency(2);
    setVoltage(2);
  }
  }
  return 0;
}
(b) TMB with  $B_{hash}$ 

for(s=0;s<p;s++)
{
  marks=s/10;
  switch(marks)
  {
    case 10: grade='X';
    break;
    case 9: grade='X';
    break;
    case 8: grade='A';
    break;
    case 7: grade='B';
    break;
    case 6: grade='C';
    break;
    case 5: grade='D';
    break;
    case 4: grade='P';
    break;
    default: grade='F';
  }
}
return 0;

```

Fig. 14. High level representation of an *MB* and its equivalent *TMB*, where  $p$  is input dependent.

is the deadline for *TMB* in Figure 14(b). In Table VI  $T_{TMB(v_i, f_i, P[i])} \leq T_{MB(v_i, f_i, P[i])}$  for each  $i$  ( $2 \leq i \leq 5$ ). This ensures the utility of VFS\_Algorithm\_B. The VFS algorithms can save more energy, when the delays of blocks of code at all the branch destinations are equal and the blocks of code contain few branch instructions.

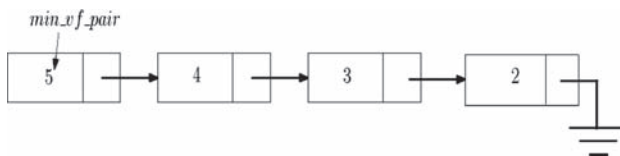


Fig. 15. Linked list created by VFS\_Algorithm\_B for the *TMB* in Figure 14(b).

Table VI. The time and energy values of *mb* and *tmb* in Figure 14.

$i$	$t_i$ ( $\mu\text{sec}$ )	$T_{ov_i}$ ( $\mu\text{sec}$ )	$P[i]$	$T_{MB(v_i, f_i, P[i])}$ ( $\mu\text{sec}$ )	$E_{MB(v_i, f_i, P[i])}$ ( $\mu\text{J}$ )	$T_{TMB(v_i, f_i, P[i])}$ ( $\mu\text{sec}$ )	$E_{TMB(v_i, f_i, P[i])}$ ( $\mu\text{J}$ )
2	0.0495	60.49	1795	158.51	115.11	156.69	58.11
3	0.0550	60.46	2144	186.63	136.34	185.27	60.38
4	0.0619	60.48	2840	242.90	178.67	242.24	65.57
5	0.0707	60.53	4843	406.21	300.50	405.15	86.87

## 4. EXPERIMENT AND RESULT

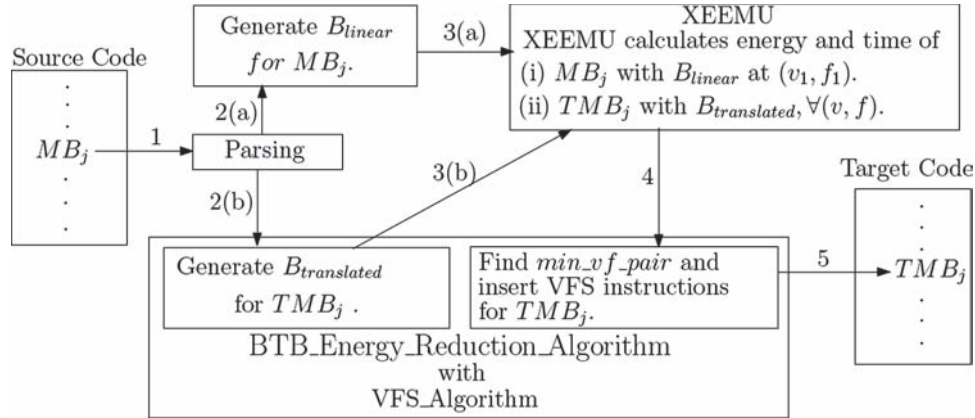
The proposed scheme is evaluated on eight benchmark programs on XEEMU simulator.<sup>7,8</sup> XEEMU simulates Intel's XScale processor. Since there does not exist standard benchmark programs involving *MB*, several representative examples in which *MB* are possible are considered as synthetic benchmarks. These synthetic benchmark programs impose the workload on the branch prediction unit causing BTB access, which implies their utility for testing the proposed work. This section explains the experimental procedure along with the analysis of the experimental results.

### 4.1. Experiment

The benchmark programs in Table VII contain one or more *MBs*. Each *MB* belongs to the class of the illustrative

**Table VII.** Benchmark programs.

Benchmark	Description	Source
PL	Evaluates proposition logic formula	cse.iitkgp.ac.in/~spyne/benchmarks
LR	A shift-reduce bottom up parser	cse.iitkgp.ac.in/~spyne/benchmarks
GUI	A GUI controller of a database system	cse.iitkgp.ac.in/~spyne/benchmarks
P'man	Pacman, a computer game	www.javaboutique.internet.com/PacMan
Chess	A computer game	www.caspercomsci.com/pages/javasource.htm
B'ship	Battleship, a computer game	www.caspercomsci.com/pages/javasource.htm
M'Conv	The mode converter, does base conversion of numbers	www.caspercomsci.com/pages/javasource.htm
B'Jack	The black Jack, a computer game	www.caspercomsci.com/pages/javasource.htm

**Fig. 16.** Experimental setup.

examples as discussed in Section 3.2. All the energy and performance values in this work are measured in XEEMU. The translated codes are written using ARM instruction set. All the programs are run on XEEMU which simulates

Intel's XScale processor. XScale has a 128-entry BTB.<sup>26</sup> Each entry contains the address of a branch instruction, the target address associated with the branch instruction, and a previous history of the branch being taken or not-taken.

**Table VIII.** Benchmark result.

Benchmark	Metric	Naïve code	Translated code	Gain (%)	Type of $k-d$ tree	# $k-d$ tree	Size range
PL	Time (sec)	1.7213	1.589	7.68	1D	16	5-11
	Total energy (J)	1.243	1.153	7.24	2D	-	-
	BTB energy ( $\mu$ J)	5746	1187	79.34	3D	-	-
LR	Time (sec)	1.1119	0.998	10.24	1D	10	3-11
	Total energy (J)	0.8368	0.7824	6.50	2D	-	-
	BTB energy ( $\mu$ J)	3380	989	70.73	3D	-	-
GUI	Time (sec)	1.1504	1.1297	1.79	1D	5	5-10
	Total energy (J)	1.8761	1.6572	11.66	2D	2	10-35
	BTB energy ( $\mu$ J)	3753	1023	72.74	3D	4	4-12
P'man	Time (sec)	2.175	1.962	9.79	1D	1	7
	Total energy (J)	1.875	1.1787	4.69	2D	1	4
	BTB energy ( $\mu$ J)	7054	2987	57.65	3D	-	-
Chess	Time (sec)	3.154	2.942	6.72	1D	-	-
	Total energy (J)	1.725	1.597	7.42	2D	3	3-8
	BTB energy ( $\mu$ J)	9432	4763	49.50	3D	-	-
B' Ship	Time (sec)	3.187	3.082	3.29	1D	-	-
	Total energy (J)	1.472	1.386	5.84	2D	1	3
	BTB energy ( $\mu$ J)	5087	3986	21.64	3D	2	2
M'Conv	Time (sec)	0.482	0.374	22.40	1D	2	26-32
	Total energy (J)	0.6427	0.6182	3.81	2D	-	-
	BTB energy ( $\mu$ J)	4876	1928	60.45	3D	-	-
B'Jack	Time (sec)	3.257	3.162	2.91	1D	3	3-13
	Total energy (J)	1.876	1.677	10.6	2D	1	14
	BTB energy ( $\mu$ J)	14872	6748	54.62	3D	-	-

The history is recorded as one of four states: strongly taken, weakly taken, weakly not-taken, or strongly not-taken. If the address of the branch instruction hits in the BTB and its history is strongly or weakly taken, the instruction at the branch target address is fetched; if its history is strongly or weakly not-taken, the next sequential instruction is fetched. In either case the history is updated. Each BTB access and update of its state causes energy consumption. The experimental setup in Figure 16 shows the proposed scheme in a sequence right from syntactical analysis (parsing) to translated multiway branch generation.

#### 4.2. Result

The Table VIII shows the comparison of energy, performance and the maximum gain achieved by the translated code. The metrics ‘Time,’ ‘Total Energy’ and ‘BTB Energy’ are same as in Tables III–V in Section 3.1. Naïve Code is the code generated by the compiler `xscale-elf-gcc`, which contains mainly  $B_{linear}$  implementations of  $MBs$ . Translated code contains possible  $B_{hash}$  and  $B_{linear}$  as  $TMBs$ . The performance gain lies within a range of 1 to 22%. The gain in total energy lies within a range of 3 to 12%. The gain in BTB energy lies within a range of 21 to 80%. The size of a  $k-d$  tree is the number of nodes in it. For a particular multiway branch, the size of a  $k-d$  tree depends on the number of branch destinations ( $n$ ) and the dimension ( $d$ ) of the  $k-d$  tree. For a multiway branch with  $n$  branch destinations and index expression values as  $d$ -dimensional discrete points, a  $k-d$  tree will have  $n$  nodes. For a multiway branch with  $n$  branch destinations and index expression values as  $d$ -dimensional ranges, a  $k-d$  tree will have  $2^d \times n$  nodes. The programs with more number of  $k-d$  trees with larger size achieve better energy and performance gain. Table VIII also keeps an account of the of the  $k-d$  trees formed during the code translation of the benchmark programs. It shows the number of  $k-d$  trees (# $k-d$  tree) belonging to different dimensions (Type of  $k-d$  tree) and the range of their size (Size range). Here, the ‘Type of  $k-d$  tree’ is either 1D (one-dimensional), 2D (two-dimensional) or 3D (three dimensional).

### 5. CONCLUSION AND FUTURE WORK

The present work reduces energy consumption for BTB access by translating multiway branch with VFS. The translated multiway branch also improves the performance of the program. It first transforms the multiway branch and then applies VFS to scale down the  $(v, f)$  to minimize energy consumed by  $MB$  under the execution time constraint. It introduces the use of  $k-d$  tree and pattern matcher to generate efficient code for multiway branch when hashing is not applicable. A wide range of illustrative examples and benchmark programs are used to highlight the efficacy of the approach. The energy savings

ranges from 21 to 80% with performance improvement ranging from 1 to 22%. The total energy is reduced within a range of 3 to 12%. As in the present work, the access to BTB is reduced; the future work will concentrate on reducing runtime leakage energy of BTB when it is not in use. We have restricted the index variables and matching values to integers and strings. The work may be extended to consider real numbers. There are *if-then-else ladders* where the index expressions are formed with several index variables, and the conditions are separated by several logical or conditional operators. The future work will also investigate on efficient translation of such  $MBs$ .

## APPENDIX

### A. $B_{linear}$ , $B_{hash}$ and $B_{binary}$ Implementations of $EX1$

The  $B_{linear}$  and  $B_{hash}$  codes of  $EX1$  are generated by `xscale-elf-gcc` compiler. Step 30 of  $B_{hash}$  code of  $EX1$  in Figure 18 shows the application of hashing. The  $B_{binary}$  code of  $EX1$  is generated by preorder traversal of the binary search tree in Figure 5.

### B. $B_{linear}$ and $B_{binary}$ Implementations of $EX2$

The  $B_{linear}$  code of  $EX2$  is generated by `xscale-elf-gcc` compiler. The  $B_{binary}$  code of  $EX2$  is generated by preorder traversal of the  $k-d$  tree in Figure 8. Appendix C illustrates the algorithm for preorder traversal of  $K-d$  tree.

### C. $B_{binary}$ Code Generation from $K-d$ Tree

#### C.1. Structure of the $K-d$ Tree Node

```
struct Kd_Tree_Node
{
    char variable_name[20];
    int value;
    char left_edge_symbol, right_edge_symbol;
    boolean left_tree_visited, right_tree_visited;
    Kd_Tree_Node *left_child, *right_child;
};
```

#### C.2. Code Generation

```
B_binary_code_generation_from_Kd_Tree(Kd_Tree_node
*root)
```

```
1. {
2.   for(all nodes q in the  $K-d$  tree)
3.   {
4.     q → left_tree_visited := false;
5.     q → right_tree_visited := false;
6.   }
7.   Preorder_Traversal_Kd_Tree(root,1);
8. }
```

```

1. .file "expl_linear.s"
2. .text
3. .align 2
4. .global main
5. .type main, %function
6. main:
7. @ args = 0, pretend = 0, frame =
   12
8. @ frame_needed = 1,
   uses_anonymous_args = 0
9. mov ip, sp
10. stmfd sp!, {fp, ip, lr, pc}
11. sub fp, ip, #4
12. sub sp, sp, #12
13. mov r3, #0
14. str r3, [fp, #-16]
15. .L2:
16. ldr r2, [fp, #-16]
17. ldr r3, .L19
18. cmp r2, r3
19. bgt .L3
20. ldr r1, [fp, #-16]
21. ldr r3, .L19+4
22. smull r2, r3, r1, r3
23. mov r2, r3, asr #2
24. mov r3, r1, asr #31
25. rsb r3, r3, r2
26. str r3, [fp, #-20]
27. ldr r3, [fp, #-20]
28. cmp r3, #10
29. bne .L5
30. mov r3, #88
31. strb r3, [fp, #-21]
32. b .L4
33. .L5:
34. ldr r3, [fp, #-20]
35. cmp r3, #9
36. bne .L7
37. mov r3, #88
38. strb r3, [fp, #-21]
39. b .L4
40. .L7:
41. ldr r3, [fp, #-20]
42. cmp r3, #8
43. bne .L9
44. mov r3, #65
45. strb r3, [fp, #-21]
46. b .L4
47. .L9:
48. ldr r3, [fp, #-20]
49. cmp r3, #7
50. bne .L11
51. mov r3, #66
52. strb r3, [fp, #-21]
53. b .L4
54. .L11:
55. ldr r3, [fp, #-20]
56. cmp r3, #6
57. bne .L13
58. mov r3, #67
59. strb r3, [fp, #-21]
60. b .L4
61. .L13:
62. ldr r3, [fp, #-20]
63. cmp r3, #5
64. bne .L15
65. mov r3, #68
66. strb r3, [fp, #-21]
67. b .L4
68. .L15:
69. ldr r3, [fp, #-20]
70. cmp r3, #4
71. bne .L17
72. mov r3, #80
73. strb r3, [fp, #-21]
74. b .L4
75. .L17:
76. mov r3, #70
77. strb r3, [fp, #-21]
78. .L4:
79. ldr r3, [fp, #-16]
80. add r3, r3, #1
81. str r3, [fp, #-16]
82. b .L2
83. .L3:
84. mov r3, #0
85. mov r0, r3
86. sub sp, fp, #12
87. ldmfd sp, {fp, sp, pc}
88. .L20:
89. .align 2
90. .L19:
91. .word 999999
92. .word 1717986919
93. .size main, .-main
94. .ident "GCC: (GNU) 3.4"

```

Fig. 17.  $B_{linear}$  code of EX1.

```

1. .file "expl_hash.s"
2. .text
3. .align 2
4. .global main
5. .type main, %function
6. main:
7. @ args = 0, pretend = 0,
   frame = 12
8. @ frame_needed = 1,
   uses_anonymous_args = 0
9. mov ip, sp
10. stmfd sp!, {fp, ip, lr, pc}
11. sub fp, ip, #4
12. sub sp, sp, #12
13. mov r3, #0
14. str r3, [fp, #-16]
15. .L2:
16. ldr r2, [fp, #-16]
17. ldr r3, .L15
18. cmp r2, r3
19. bgt .L3
20. ldr r1, [fp, #-16]
21. ldr r3, .L15+4
22. smull r2, r3, r1, r3
23. mov r2, r3, asr #2
24. mov r3, r1, asr #31
25. rsb r3, r3, r2
26. str r3, [fp, #-20]
27. ldr r3, [fp, #-20]
28. sub r3, r3, #4
29. cmp r3, #6
30. ldrls pc, [pc, r3, asl #2]
31. b .L13
32. .p2align 2
33. .L14:
34. .word .L12
35. .word .L11
36. .word .L10
37. .word .L9
38. .word .L8
39. .word .L7
40. .word .L6
41. .L6:
42. mov r3, #88
43. strb r3, [fp, #-21]
44. b .L4
45. .L7:
46. mov r3, #88
47. strb r3, [fp, #-21]
48. b .L4
49. .L8:
50. mov r3, #65
51. strb r3, [fp, #-21]
52. b .L4
53. .L9:
54. mov r3, #66
55. strb r3, [fp, #-21]
56. b .L4
57. .L10:
58. mov r3, #67
59. strb r3, [fp, #-21]
60. b .L4
61. .L11:
62. mov r3, #68
63. strb r3, [fp, #-21]
64. b .L4
65. .L12:
66. mov r3, #80
67. strb r3, [fp, #-21]
68. b .L4
69. .L13:
70. mov r3, #70
71. strb r3, [fp, #-21]
72. .L4:
73. ldr r3, [fp, #-16]
74. add r3, r3, #1
75. str r3, [fp, #-16]
76. b .L2
77. .L3:
78. mov r3, #0
79. mov r0, r3
80. sub sp, fp, #12
81. ldmfd sp, {fp, sp, pc}
82. .L16:
83. .align 2
84. .L15:
85. .word 999999
86. .word 1717986919
87. .size main, .-main
88. .ident "GCC: (GNU) 3.4.3"

```

Fig. 18.  $B_{hash}$  code of EX1.



```

1. .file "expl_binary.s"
2. .text
3. .align 2
4. .global main
5. .type main,%function
6. main:
7. @ args = 0, pretend = 0, frame =
   12
8. @ frame_needed = 1,
   uses_anonymous_args = 0
9. mov ip, sp
10. stmfd sp!, {fp, ip, lr, pc}
11. sub fp, ip, #4
12. sub sp, sp, #12
13. mov r3, #0
14. str r3, [fp, #-16]
15. .L2:
16. ldr r2, [fp, #-16]
17. ldr r3, .L19
18. cmp r2, r3
19. bgt .L3
20. ldr r1, [fp, #-16]
21. ldr r3, .L19+4
22. smull r2, r3, r1, r3
23. mov r2, r3, asr #2
24. mov r3, r1, asr #31
25. rsb r3, r3, r2
26. str r3, [fp, #-20]
27. ldr r3, [fp, #-20]
28. cmp r3, #7
29. blt .L5
30. bgt .L6
31. b .L12
32. .L5:
33. cmp r3, #5
34. blt .L7
35. bgt .L8
36. b .L13
37. .L7:
38. cmp r3, #4
39. blt .L9
40. bgt .L4
41. b .L14
42. .L8:
43. cmp r3, #6
44. bne .L4
45. b .L15
46. .L6:
47. cmp r3, #9
48. blt .L10
49. bgt .L11
50. b .L16
51. .L10:
52. cmp r3, #8
53. bne .L4
54. b .L17
55. .L11:
56. cmp r3, #10
57. bne .L4
58. b .L16
59. .L12:
60. mov r3, #66
61. strb r3, [fp, #-21]
62. b .L4
63. .L13:
64. mov r3, #68
65. strb r3, [fp, #-21]
66. b .L4
67. .L14:
68. mov r3, #80
69. strb r3, [fp, #-21]
70. b .L4
71. .L15:
72. mov r3, #67
73. strb r3, [fp, #-21]
74. b .L4
75. .L16:
76. mov r3, #88
77. strb r3, [fp, #-21]
78. b .L4
79. .L17:
80. mov r3, #65
81. strb r3, [fp, #-21]
82. b .L4
83. .L9:
84. mov r3, #70
85. strb r3, [fp, #-21]
86. .L4:
87. ldr r3, [fp, #-16]
88. add r3, r3, #1
89. str r3, [fp, #-16]
90. b .L2
91. .L3:
92. mov r3, #0
93. mov r0, r3
94. sub sp, fp, #12
95. ldmfd sp, {fp, sp, pc}
96. .L20:
97. align 2
98. .L19:
99. .word 999999
100. .word 1717986919
101. .size main, .-main
102. .ident "GCC: (GNU) 3.4.3"

```

Fig. 19.  $B_{binary}$  code of EX1.

```

1. .file "exp5_linear.s"
2. .text
3. .align 2
4. .global main
5. .type main,%function
6. main:
7. @ args = 0, pretend = 0, frame = 12
8. @ frame_needed = 1,
   uses_anonymous_args = 0
9. mov ip, sp
10. stmfd sp!, {fp, ip, lr, pc}
11. sub fp, ip, #4
12. sub sp, sp, #12
13. mov r3, #0
14. str r3, [fp, #-16]
15. .L2:
16. ldr r2, [fp, #-16]
17. mov r3, #996
18. add r3, r3, #3
19. cmp r2, r3
20. bgt .L3
21. mov r3, #0
22. str r3, [fp, #-20]
23. .L5:
24. ldr r2, [fp, #-20]
25. mov r3, #996
26. add r3, r3, #3
27. cmp r2, r3
28. bgt .L4
29. ldr r3, [fp, #-16]
30. cmp r3, #12
31. ble .L8
32. ldr r3, [fp, #-16]
33. cmp r3, #16
34. bgt .L8
35. ldr r3, [fp, #-20]
36. cmp r3, #7
37. ble .L8
38. ldr r3, [fp, #-20]
39. cmp r3, #12
40. bgt .L8
41. mov r3, #1
42. str r3, [fp, #-24]
43. b .L7
44. .L8:
45. ldr r3, [fp, #-16]
46. cmp r3, #5
47. ble .L10
48. ldr r3, [fp, #-16]
49. cmp r3, #12
50. bgt .L10
51. ldr r3, [fp, #-20]
52. cmp r3, #3
53. ble .L10
54. ldr r3, [fp, #-20]
55. cmp r3, #7
56. bgt .L10
57. mov r3, #2
58. str r3, [fp, #-24]
59. b .L7
60. .L10:
61. ldr r3, [fp, #-16]
62. cmp r3, #2
63. ble .L7
64. ldr r3, [fp, #-16]
65. cmp r3, #5
66. bgt .L7
67. ldr r3, [fp, #-20]
68. cmp r3, #0
69. ble .L7
70. ldr r3, [fp, #-20]
71. cmp r3, #3
72. bgt .L7
73. mov r3, #3
74. str r3, [fp, #-24]
75. .L7:
76. ldr r3, [fp, #-20]
77. add r3, r3, #1
78. str r3, [fp, #-20]
79. b .L5
80. .L4:
81. ldr r3, [fp, #-16]
82. add r3, r3, #1
83. str r3, [fp, #-16]
84. b .L2
85. .L3:
86. mov r3, #0
87. mov r0, r3
88. sub sp, fp, #12
89. ldmfd sp, {fp, sp, pc}
90. .size main, .-main
91. .ident "GCC: (GNU) 3.4.3"

```

Fig. 20.  $B_{linear}$  code of EX2.

```

1. .file "exp5_binary.s"
2. .text
3. .align 2
4. .global main
5. .type main, %function
6. main:
7. @ args = 0, pretend = 0, frame = 12
8. @ frame_needed = 1,
   uses_anonymous_args = 0
9. mov ip, sp
10. stmfid sp!, {fp, ip, lr, pc}
11. sub fp, ip, #4
12. sub sp, sp, #12
13. mov r3, #0
14. str r3, [fp, #-16]
15. .L2:
16. ldr r2, [fp, #-16]
17. mov r3, #996
18. add r3, r3, #3
19. cmp r2, r3
20. bgt .L3
21. mov r3, #0
22. str r3, [fp, #-20]
23. .L5:
24. ldr r2, [fp, #-20]
25. mov r3, #996
26. add r3, r3, #3
27. cmp r2, r3
28. bgt .L4
29. ldr r2, [fp, #-16]
30. ldr r3, [fp, #-20]
31. cmp r2, #6
32. bge .L9
33. .L8:
34. cmp r3, #3
35. bgt .L7
36. .L10:
37. cmp r2, #3
38. blt .L7
39. .L11:
40. cmp r3, #1
41. blt .L7
42. mov r3, #3
43. str r3, [fp, #-24]
44. b .L7
45. .L9:
46. cmp r3, #8
47. bge .L13
48. .L12:
49. cmp r2, #12
50. bgt .L7
51. .L14:
52. cmp r3, #4
53. blt .L7
54. mov r3, #2
55. str r3, [fp, #-24]
56. b .L7
57. .L13:
58. cmp r2, #16
59. bat .L7
60. .L15:
61. cmp r3, #12
62. bgt .L7
63. cmp r2, #13
64. blt .L7
65. mov r3, #1
66. str r3, [fp, #-24]
67. .L7:
68. ldr r3, [fp, #-20]
69. add r3, r3, #1
70. str r3, [fp, #-20]
71. b .L5
72. .L4:
73. ldr r3, [fp, #-16]
74. add r3, r3, #1
75. str r3, [fp, #-16]
76. b .L2
77. .L3:
78. mov r3, #0
79. mov r0, r3
80. sub sp, fp, #12
81. ldmfd sp, {fp, sp, pc}
82. .size main, .-main
83. .ident "GCC: (GNU) 3.4.3"

```

Fig. 21.  $B_{binary}$  code of EX2.

### C.3. Preorder Traversal of $k-d$ Tree

Preorder\_Traversal\_Kd\_Tree(Kd\_Tree\_node \*root, int label)

```

1. {
2.   if(root!=null) then
3.     {
4.       if(root is a non leaf node) then
5.         {
6.           sprintf(S, "cmp %s, %d,"
              root → variable_name, root → value);
              write(S);
7.           if(root → right_edge_symbol = '>') then
8.             sprintf(S1, "bgt");
9.           else
10.            sprintf(S1, "bge");
11.          if(all leaf nodes of root node's right
              subtree contain NEXT) then
12.            {
13.              sprintf(S, "%s NEXT," S1);
14.              root->right_tree_visited := true;
15.            }
16.          else
17.            sprintf(S, "%s L%d," S1, 2*label+1);
18.            write(S);
19.          if(root->left_edge_symbol = '<') then
20.            sprintf(S1, "blt");
21.          else
22.            sprintf(S1, "ble");

```

```

23.           if(all leaf nodes of root node's left subtree
              contain NEXT) then
24.             {
25.               sprintf(S, "%s NEXT," S1);
26.               root->left_tree_visited := true;
27.             }
28.           else
29.             sprintf(S, "%s L%d," S1, 2*label);
30.             write(S);
31.           }
32.         else
33.           {
34.             if(root node do not contain NEXT) then
35.               {
36.                 sprintf(S, "L%d:," label); write(S);
37.                 generate code for the content in the
38.                 leaf node and write it;
39.               }
40.             if(root → left_tree_visited = false) then
41.               Preorder_Traversal_Kd_Tree(root →
42.               left_child, 2*label);
43.             sprintf("L%d:," 2*label + 1);
44.             if(root → right_tree_visited = false) then
45.               Preorder_Traversal_Kd_Tree(root →
46.               right_child, 2*label + 1);

```

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