

Isothetic Cover

## Isothetic Covers for Digital Objects:

Algorithms and Applications

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CSE, IIT Kharagpur

RESEARCH PROMOTION WORKSHOP
INTRODUCTION TO GRAPH AND GEOMETRIC ALGORITHMS
NOVEMBER 1-3, 2011 (PDPM IIITDM JABALPUR)



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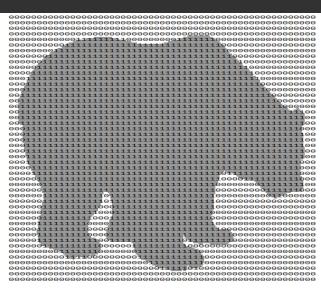
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object = set of 1s



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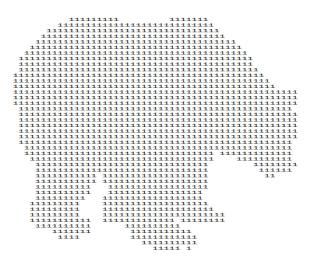
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object = set of 1s



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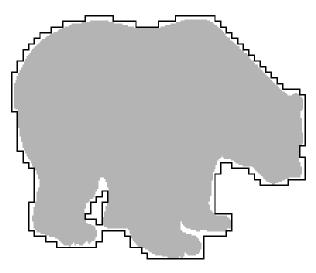
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g = 4: Isothetic Cover



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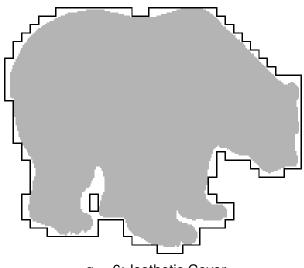
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g = 6: Isothetic Cover



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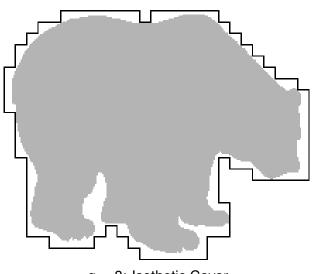
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g = 8: Isothetic Cover



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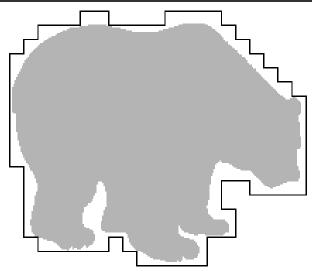
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g = 10: Isothetic Cover

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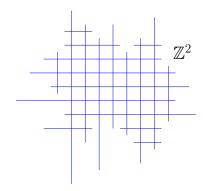
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Digital plane,  $\mathbb{Z}^2$  = set of all points having integer coordinates.



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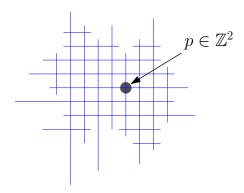
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Digital point (pixel) = a point in  $\mathbb{Z}^2$ .



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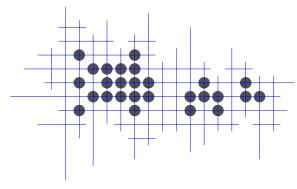
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Digital object = a set S of digital points.

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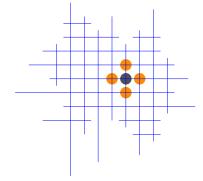
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### 4-neighborhood of *p*:

$$N_4(p) = \{(x', y') : (x', y') \in \mathbb{Z}^2 \land |x - x'| + |y - y'| = 1\}$$

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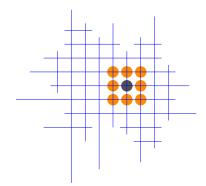
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### 8-neighborhood of *p*:

$$N_8(p) = \{(x', y') : (x', y') \in \mathbb{Z}^2 \land \max(|x - x'|, |y - y'|) = 1\}$$

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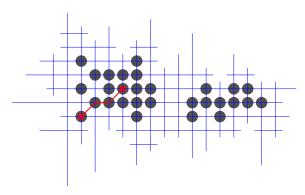
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Two points p and q are k-connected in S if there exists a sequence  $\langle p := p_0, p_1, \ldots, p_n := q \rangle \subseteq S$  such that  $p_i \in N_k(p_{i-1})$  for  $1 \leq i \leq n$ .



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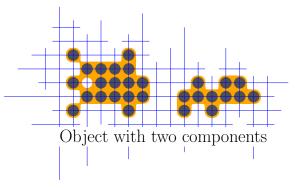
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For any point  $p \in S$ , the maximum-cardinality set of points that are k-connected to p forms a k-connected component of S.



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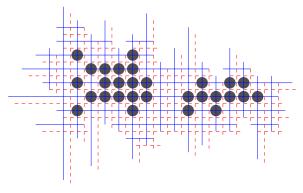
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Grid  $\mathbb{G}$  with grid size g = 1 (red dashed lines)



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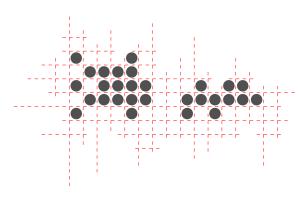
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Grid  $\mathbb{G}$  with grid size g=1 (red dashed lines)



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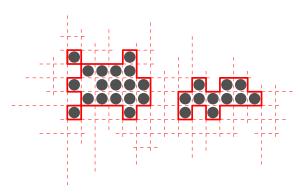
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Isothetic cover for g=1



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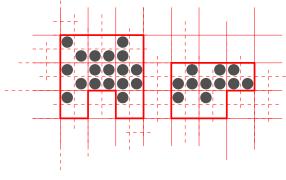
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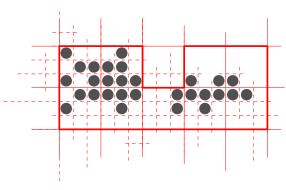


Isothetic cover for g=2



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Isothetic cover for g = 3



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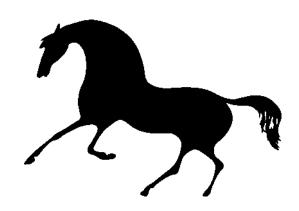
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Shape 3D





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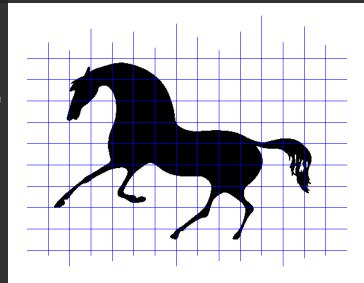
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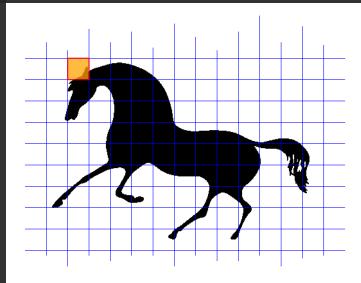
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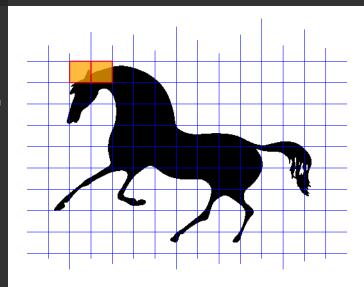
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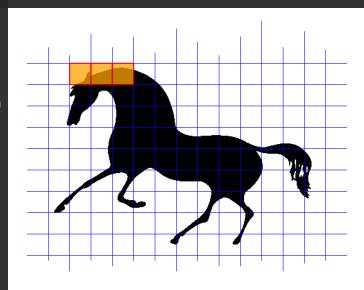
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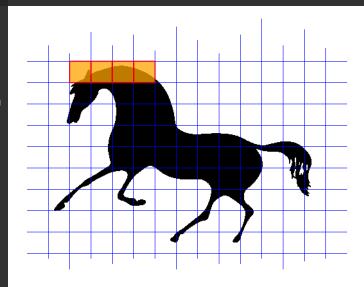
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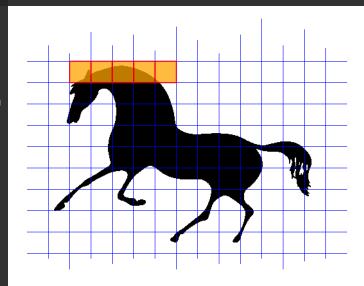
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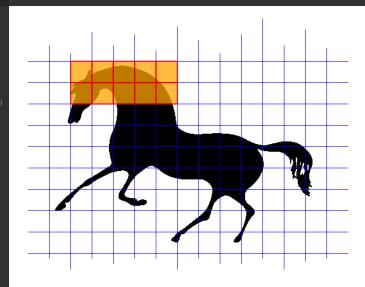
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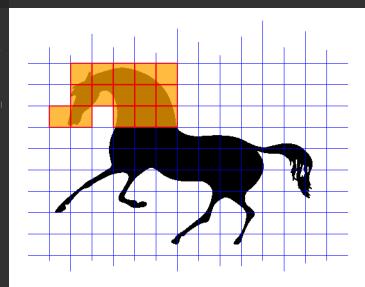
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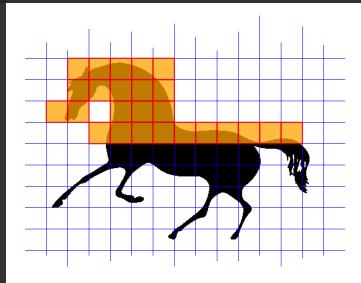
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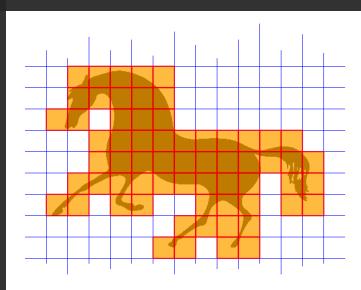
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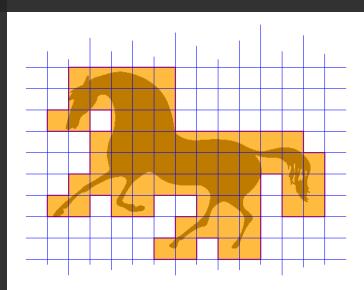
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#### Application:

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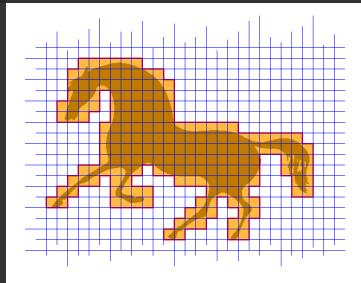
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### Disadvantages

- Scans the entire image
- Cell joining required to output the vertex sequence

Alternative solution: Combinatorial algorithm.



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### Disadvantages

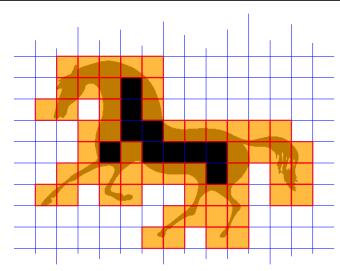
- Scans the entire image
- Cell joining required to output the vertex sequence

Alternative solution: Combinatorial algorithm.



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Combinatorial



Fully black cells can be disregarded



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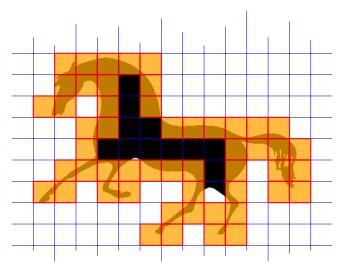
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Avoid also some partly black cells. Just consider the border cells.



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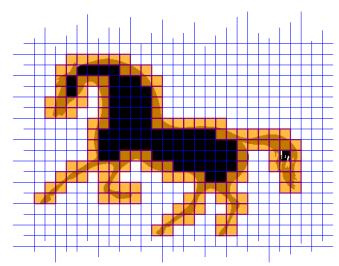
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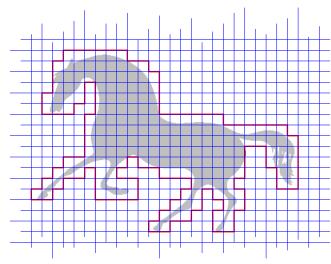
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Avoid the concept of cell joining



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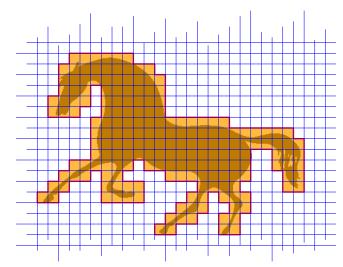
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The isothetic polygon contains the object



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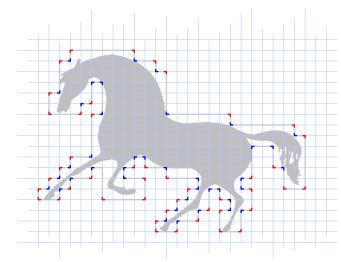
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Vertex angles are 90° and 270°





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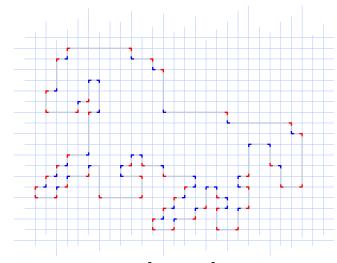
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Vertex angles are  $90^{\circ}$  and  $270^{\circ}$ 



### Backtracking—A serious issue

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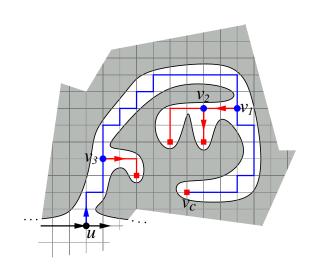
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### Backtracking—A serious issue

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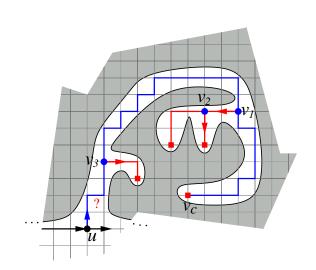
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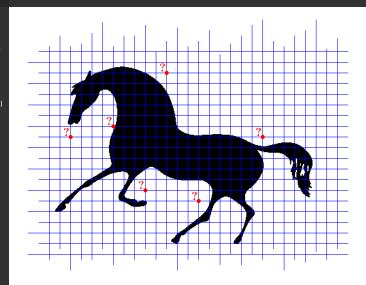
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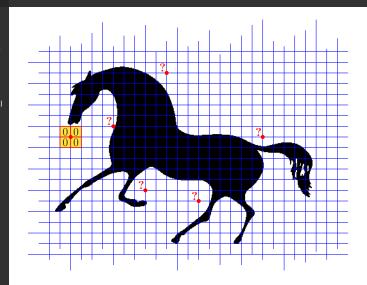
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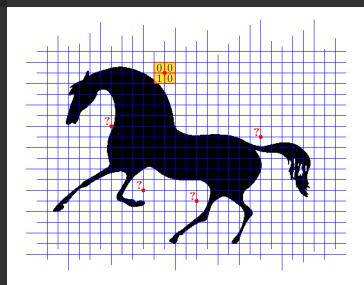
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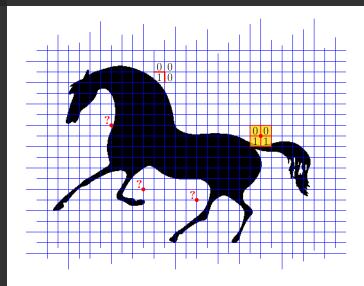
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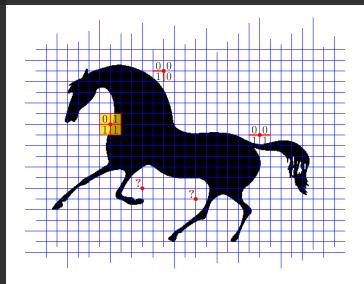
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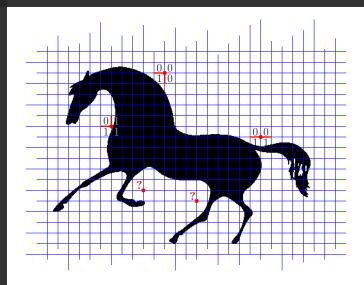
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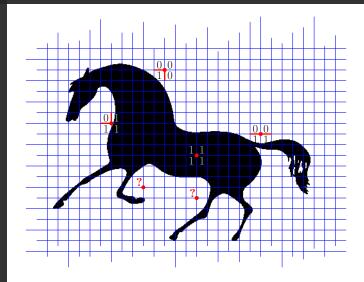
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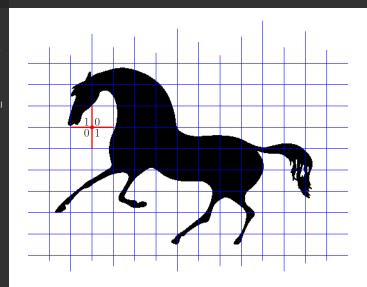
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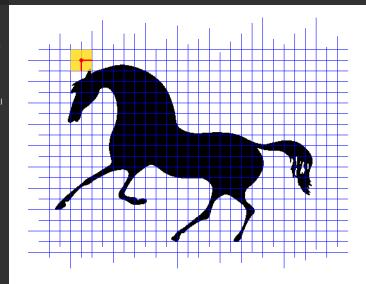
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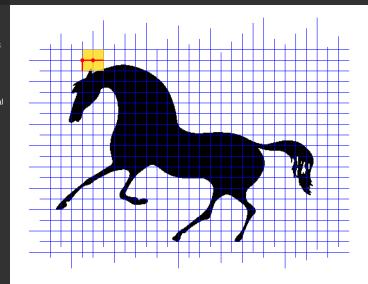
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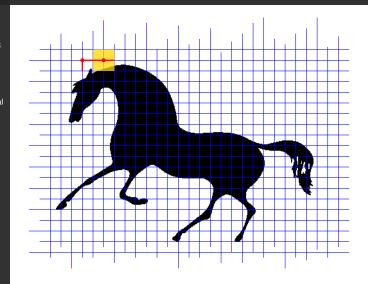
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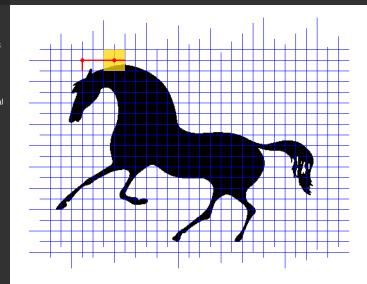
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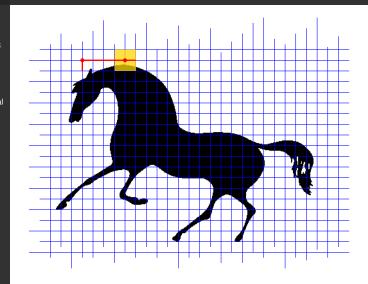
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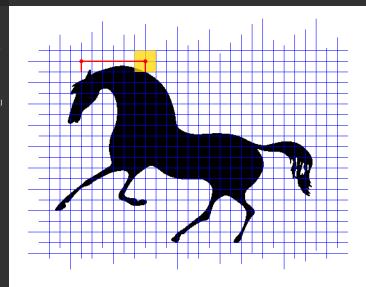
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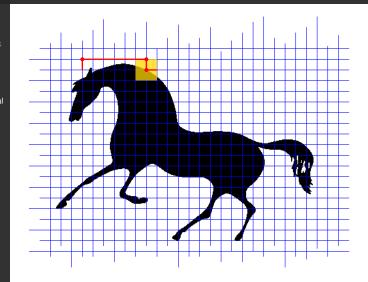
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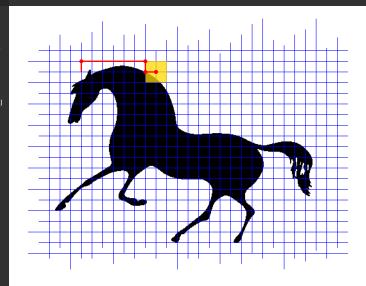
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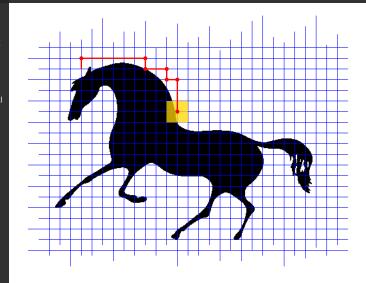
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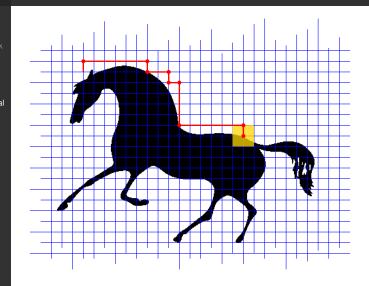
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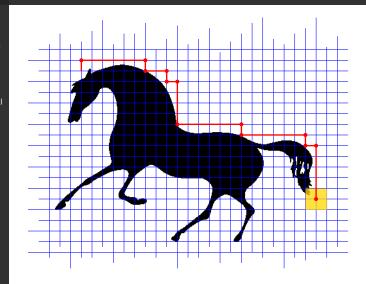
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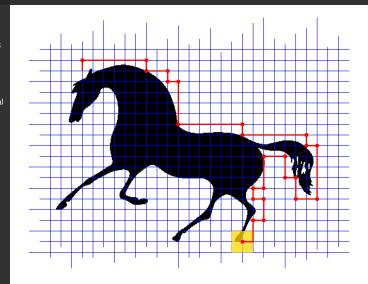
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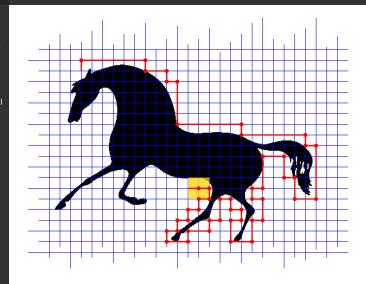
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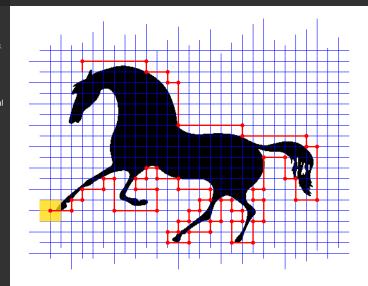
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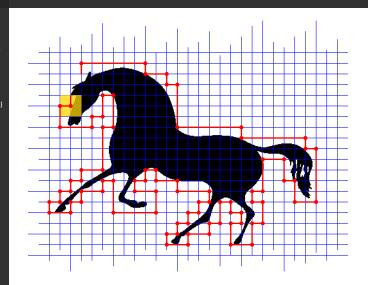
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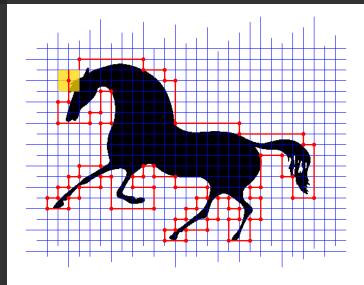
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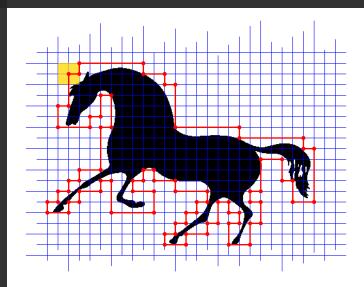
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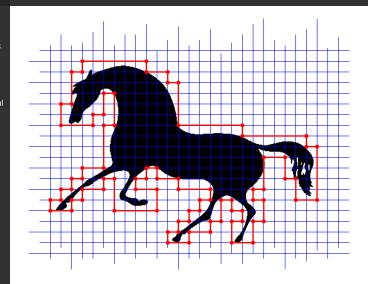
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Combinatorial

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P. Bhowmicl

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### The line of proof:

- The interior of a cell lies outside  $P_{\mathbb{G}}(S)$  if and only if the cell has no object occupancy.
- All vertices are detected and correctly classified.
- If p is a point lying on  $P_{\mathbb{G}}(S)$ , then  $0 < d_{\mathbb{T}}(p, S) \leqslant g$
- The construction of  $P_{\mathbb{G}}(S)$  always concludes at the start vertex.

- Best case:  $O(|P|/g) \leftarrow$  found in practice
- Worst case: O(|P|)



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 $<sup>^{1}|</sup>P| = \text{perimeter of } P_{\mathbb{G}}(S)$ 



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### The line of proof:

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### Isothetic Cover

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Isothetic Cover

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 $H_{\mathbb{G}}(S)$  = smallest-area orthogonal polygon such that

- S lies inside  $H_{\mathbb{G}}(S)$  $\Rightarrow P_{\mathbb{G}}(S)$  lies inside  $H_{\mathbb{G}}(S)$
- intersection of H<sub>G</sub>(S) with any horizontal or vertical line is either empty or exactly one line segment.

rules over vertex subsequences.





Isothetic Cover

P. Bhowmick

Introduction

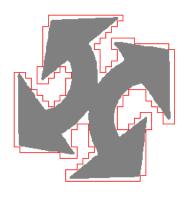
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Combinatorial

Applications Hull  $H_{\mathbb{G}}(S)$  = smallest-area orthogonal polygon such that

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Algorithm—Uses combinatorial rules over vertex subsequences.





Isothetic Cover

P. Bhowmick

Introduction

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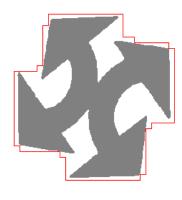
Combinatoria

Applications

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Algorithm—Uses combinatoria rules over vertex subsequences.





Isothetic Cover

P. Bhowmick

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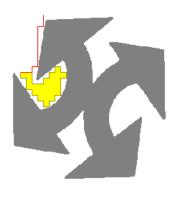
Combinatoria

Applications

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Algorithm—Uses combinatorial rules over vertex subsequences.





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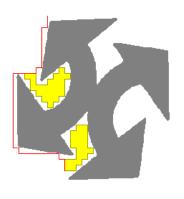
Combinatoria

Applications

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Algorithm—Uses combinatorial rules over vertex subsequences.





Isothetic Cover

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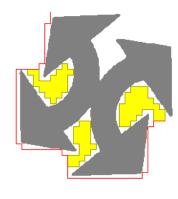
Combinatorial

Applications

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Algorithm—Uses combinatorial rules over vertex subsequences.





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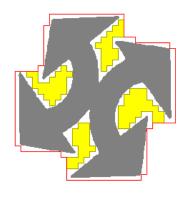
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Combinatoria

Applications Hull  $H_{\mathbb{G}}(S)$  = smallest-area orthogonal polygon such that

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Algorithm—Uses combinatorial rules over vertex subsequences.





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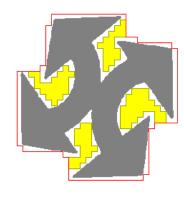
Combinatoria

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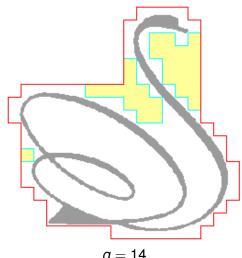
 $H_{\mathbb{G}}(S)$  = smallest-area orthogonal polygon such that

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Algorithm—Uses combinatorial rules over vertex subsequences.

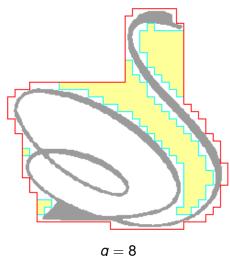






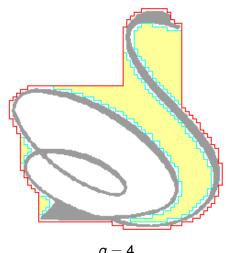
$$g = 14$$





$$g = 8$$





$$g = 4$$



## Convex partitioning

Isothetic Cover

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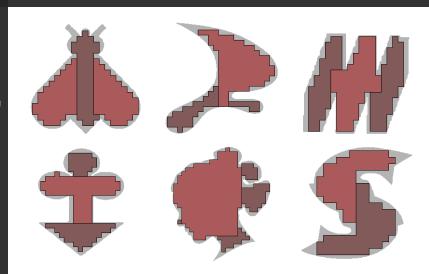
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## Convex partitioning

### Isothetic Cover

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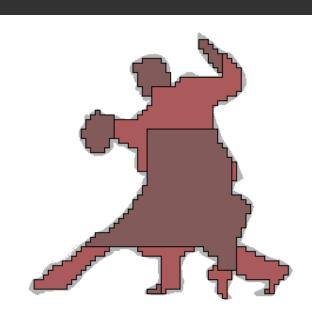
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## Shortest isothetic path

#### Isothetic Cover

P. Bhowmick

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#### Isothetic Cover

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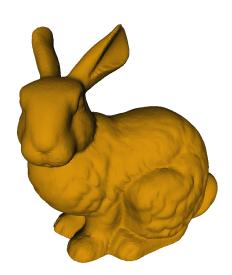
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Hull





Isothetic Cover

P. Bhowmick

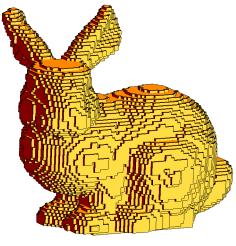
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$$g = 2$$



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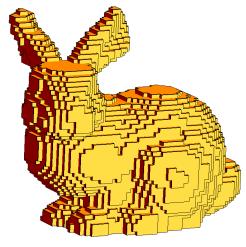
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$$g = 3$$



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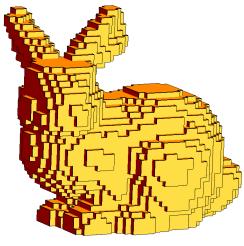
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3D



$$g = 4$$



### Isothetic Cover

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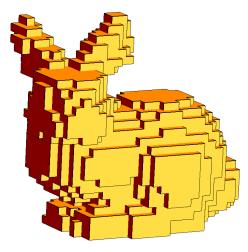
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$$g = 6$$



### Isothetic Cover

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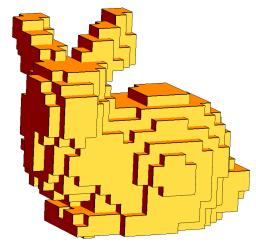
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Shape



$$g = 8$$



### Isothetic Cover

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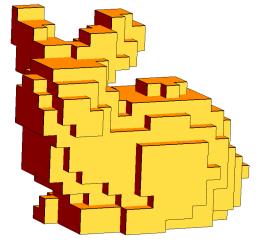
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Hull



$$g = 10$$



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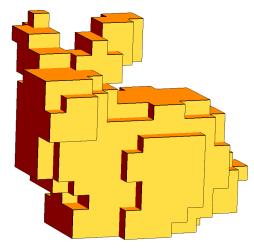
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, .pp..oa..o...

Shape



$$g = 12$$



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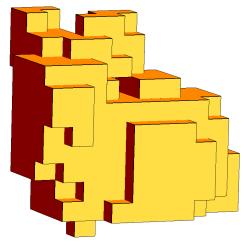
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3D



$$g = 16$$



Isothetic Cover

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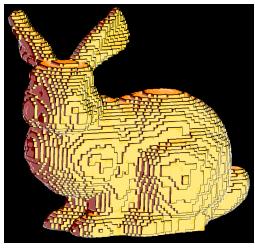
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$$g = 2$$



Isothetic Cover

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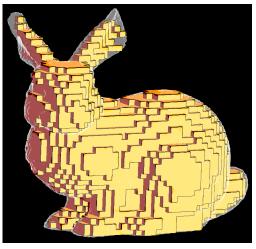
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$$g = 4$$



#### Isothetic Cover

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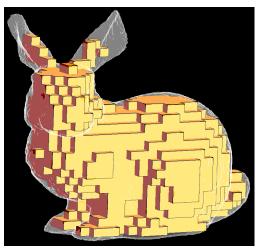
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$$g = 6$$



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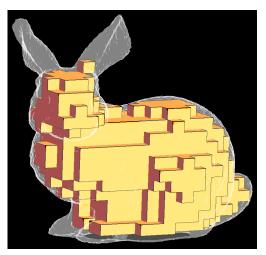
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$$g = 8$$



#### Isothetic Cover

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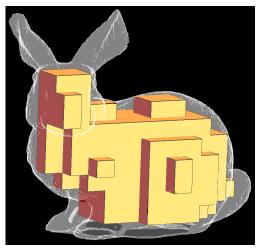
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$$g = 12$$



#### Isothetic Cover

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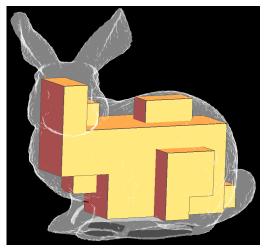
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$$g = 16$$



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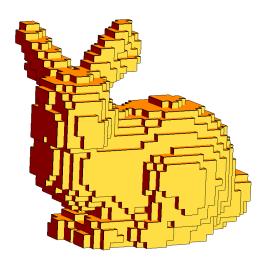
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high resolution



### Isothetic Cover

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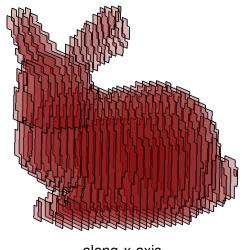
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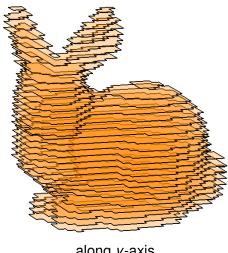
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along x-axis





along y-axis



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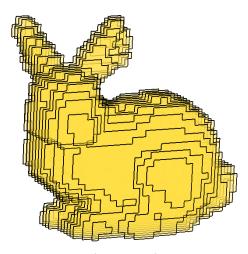
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along z-axis



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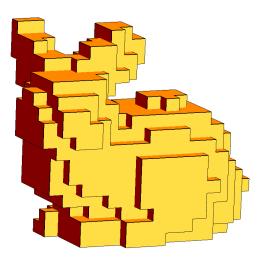
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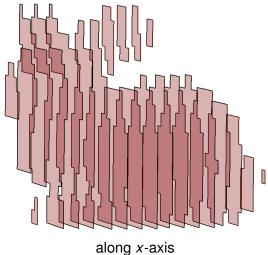
Hull

Shape 3D



low resolution







#### Isothetic Cover

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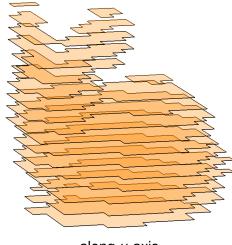
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along y-axis



#### Isothetic Cover

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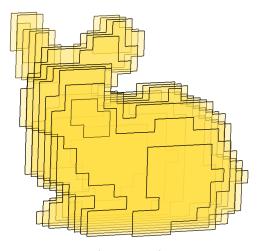
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along z-axis



# Further reading I

Isothetic Cover



A. Biswas, P. Bhowmick, M. Sarkar, and B. B. Bhattacharya, A Linear-time Combinatorial Algorithm to Find the Orthogonal Hull of an Object on the Digital Plane, Information Sciences, 216: 176-195, 2012.



A. Biswas, P. Bhowmick, and B. B. Bhattacharya. Construction of Isothetic Covers of a Digital Object: A Combinatorial Approach, Journal of Visual Communication and Image Representation, **21**(4): 295–310, 2010.



M. Dutt, A. Biswas, and P. Bhowmick, ACCORD: With Approximate Covering of Convex Orthogonal Decomposition, DGCI 2011: 16th IAPR International Conference on Discrete Geometry for Computer Imagery, LNCS 6607: 489-500, 2011.



M. Dutt, A. Biswas, P. Bhowmick, and B. B. Bhattacharya, On Finding Shortest Isothetic Path inside a Digital Object. 15th International Workshop on Combinatorial Image Analysis: IWCIA'12, 2012 [To appear in LNCS, Springer]



## Further reading II

#### Isothetic Cover

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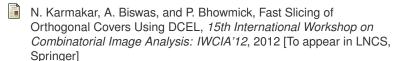
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N. Karmakar, A. Biswas, P. Bhowmick, and B.B. Bhattacharya, A Combinatorial Algorithm to Construct 3D Isothetic Covers, *International Journal of Computer Mathematics*, 2012 (in press).



N. Karmakar, A. Biswas, P. Bhowmick, and B.B. Bhattacharya, Construction of 3D Orthogonal Cover of a Digital Object, 14th International Workshop on Combinatorial Image Analysis: IWCIA'11, LNCS 6636:70–83, 2011.

R. Klette and A. Rosenfeld, *Digital Geometry: Geometric Methods for Digital Picture Analysis*, Morgan Kaufmann, San Francisco, 2004.



### Isothetic Cover

P. Bhowmick

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Hull

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## Thank You