

# Online Advertising: Paid Search Deep Dive

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# Search Advertising

# SERP Anatomy – User Perspective

bing MS Beta

WEB IMAGES VIDEOS MAPS NEWS MORE

laptop

60,600,000 RESULTS Any time ▾

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# SERP Anatomy – Designer Perspective

The image shows a Bing search results page for the query 'laptop'. The search bar at the top contains the query 'laptop' and is labeled 'Query'. Below the search bar, the page displays '60,600,000 RESULTS' and 'Any time'. The results are categorized into several sections:

- Mainline Ads:** The top two results are advertisements for Windows 8 laptops and AMD laptops, highlighted with an orange box and labeled 'Mainline Ads'.
- Organic Results:** The middle three results are organic search results from Best Buy, Amazon, and Dell, highlighted with an orange box and labeled 'Organic Results'.
- Bottom Ads:** The bottom two results are advertisements for Sony VAIO Pro and RentACenter laptops, highlighted with an orange box and labeled 'Bottom Ads'.
- Sidebar Ads:** A vertical column of related searches is located on the right side of the page, including 'HP Laptops', 'Best Deals On Laptops', 'Walmart Laptops', 'Best Laptops', 'Top 10 Laptops', 'Dell Laptop', 'Free Laptop', and 'Best Buy', highlighted with an orange box and labeled 'Sidebar Ads'.

At the bottom of the page, there is a navigation bar with the numbers 1, 2, 3, 4, 5, and 'Next'.

## Terminology

- **Query**, User Query, Web Query, Search Term
- **Mainline Ads**, North Ads, Top Bar Ads
- **Organic Result**, Algorithmic Result, Natural Result, Free Result
- **Bottom Ads**, South Ads
- **Sidebar Ads**, Right Side Ads

# ...and that of Search Ad

Title



**Cheap Auto Insurance**

Display URL



**Auto.AutoQuoteWizard.com**

Ad Text



Get the Lowest **Auto** Rates In Just 60 Seconds. Save Hundreds.

Destination URL:

[http://www.autoquotewizard.com/auto?arrival\\_id=100956579](http://www.autoquotewizard.com/auto?arrival_id=100956579)

The screenshot shows a web browser window with the URL [http://www.autoquotewizard.com/auto?arrival\\_id=100956579](http://www.autoquotewizard.com/auto?arrival_id=100956579) in the address bar. The page content includes a yellow banner with the text "AutoQuoteWizard.com", a heading "Fill out the form below, and you could save hundreds on Car Insurance .", and a form titled "Vehicles" for entering car details. The form includes fields for Vehicle Year, Make, Model, Submodel, Ownership, Primary use, and Annual mileage, each with a dropdown menu. A "Primary Vehicle" label is also present.

# Facebook Ad

The image shows a screenshot of a Facebook profile for Bill Wilson. The profile includes a cover photo of a man and a woman, a profile picture of the same couple, and a bio section with a text input field and an "Attach" button. The "Information" section lists relationship status as "Married to Charlene Wilson" and birthday as "October 8". The "Friends" section shows 295 friends with a "See All" link and a grid of six friend profile pictures.

The main content area displays three posts:

- Post 1:** A link post titled "Single-Family Housing Starts Fade In July" with a line graph showing a downward trend. The text says: "Sometimes, you need to look deeper than the headlines to get the news that matters. This basic truth's latest example comes from the July Housing Starts data, as published by the U.S. Census Bureau. source: OKCHomeSellers link: Full Article..."
- Post 2:** A link post titled "Home Builder Confidence Falls Again; Home Buyers Gain Leverage?" with a line graph showing a downward trend. The text says: "After reaching a 3-year high just 90 days ago, the National Association of Homebuilders' Housing Market Index is now at a multi-year low after falling by almost half. source: OKCHomeSellers link: Full Article..."
- Post 3:** A link post titled "Real Estate Property Marketing Plan To Sell Your Oklahoma City Home — Part 20, Trulia Pro" with the Trulia logo. The text says: "This is the twentieth post in the series 'Real Estate Property Marketing Plan To Sell Your Oklahoma City Home'. From our comprehensive marketing plan: 20. Feature the listing on Trulia.com. We maintain a 'Pro' account with Trulia which means our listings will show as 'Featured'!"

On the right side of the profile, there is a "Create an Ad" section. A red circle highlights an advertisement for "Horse Property For Sale". The ad features a photo of a large house and text: "Gorgeous horse property. 20 acres with beautiful 4200 foot house, large barn and 4 stall horse barn. Pipe fenced pasture. Virtual Tour." Below the text is a "Like" button and a "More Ads" link.

# Twitter Ad

This screenshot shows the Twitter interface with several elements highlighted by red boxes and arrows:

- Promoted Account:** A red box highlights the 'VerizonWirelessDeals' account in the 'Who to follow' section, with an arrow pointing to it.
- Promoted Tweet:** A red box highlights a tweet from 'Coke Zero' with the text '#itsnotyourfault you've spent hours filling out brackets. CokeURL.com/jj2z'. An arrow points to this tweet.
- Promoted Trend:** A red box highlights the '#BracketBusters' trend in the 'Trends' section, with an arrow pointing to it.

This screenshot shows the Twitter search results for the query 'cars'. The interface includes the Twitter logo, a search bar with 'cars' entered, and a 'Search' button. The results are categorized as 'Realtime results for cars' and show a mix of organic tweets and sponsored content.

Annotations on the screenshot include:

- Relevant Sponsors Most Recent Tweet:** A speech bubble points to a tweet from 'GMVolt' with the text 'My Question to GM CEO Rick Wagoner http://tinyurl.com/9e2bcc (expand) about 9 hours ago · Reply · View Tweet'. This tweet is marked as a 'Sponsor Result'.
- Relevant Sponsor Ads. Paid Placement. Can link to Twitter Accounts or Other Properties:** A speech bubble points to a 'Sponsor Results' section on the right side of the page, which displays various car-related advertisements like 'edmunds.com', 'GM Blogs', 'cnet Car Tech', and 'SEAT'.

Session 2

Deep Dive into Computational  
Advertising

# Agenda

## Setting the Stage

- SERP Anatomy
- Campaign Schema
- Paid Search Participants

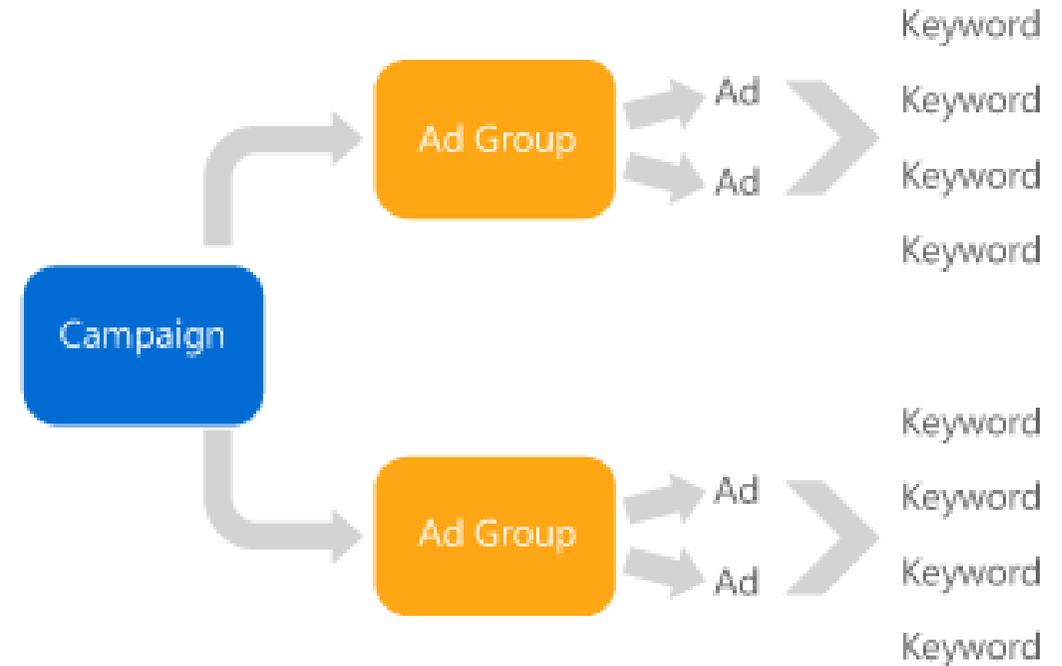
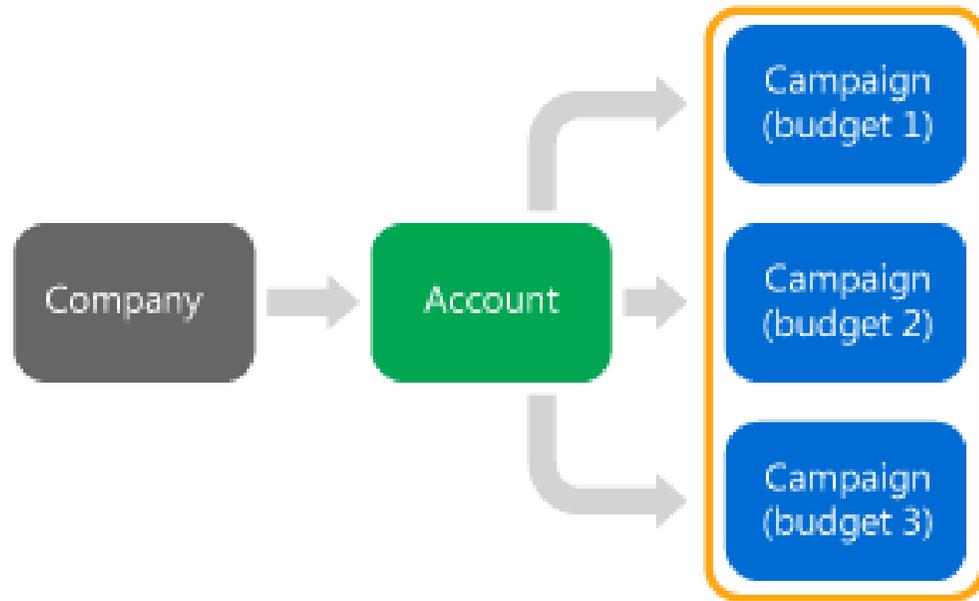
## Designing the Machine

- Campaign structure
- Algorithms for Selection, Relevance and Click Prediction

## Closer Look at Auctions

# Setting the Stage

# Campaign Schema



# Campaign Schema

Account

Campaign

Ad Group

Ad Copy

Keyword

- Contact Information
- Time Zone setting
- Billing Information
  - Currency Setting
  - Payment Setting
  - Payment Method

# Campaign Schema

Account

Campaign

Ad Group

Ad Copy

Keyword

- Way to organize marketing initiatives around one theme, product or business objective
- Best practice for billing clarity and performance optimization
- Budget and Targeting are set at campaign level

# Campaign Schema

Account

Campaign

Ad Group

Ad Copy

Keyword

- Meant to provide next level of organization
- Collection of Ads, Keywords
- Allows settings to override Campaign level settings e.g. Target, Bid etc.

# Campaign Schema

Account

Campaign

Ad Group

Ad Copy

Keywords

- Consists of Ad Title, Ad Text, Display URL and Destination URL
- Also called Creative
- This is what the end user sees on SERP

Can you suggest a good Ad Copy for "Nokia Lumia 520"?

# Campaign Schema

Account

Campaign

Ad Group

Ad Copy

Keyword

- Words or phrases that advertisers think carry intent of interest in their products or services
- A way to define target customer
- Associated with Match Type
  - Exact, Phrase, Broad
- Negative Keyword

Which negative keywords will you use if you are selling “Wedding Ring”?

# Campaign Schema – Putting them all together

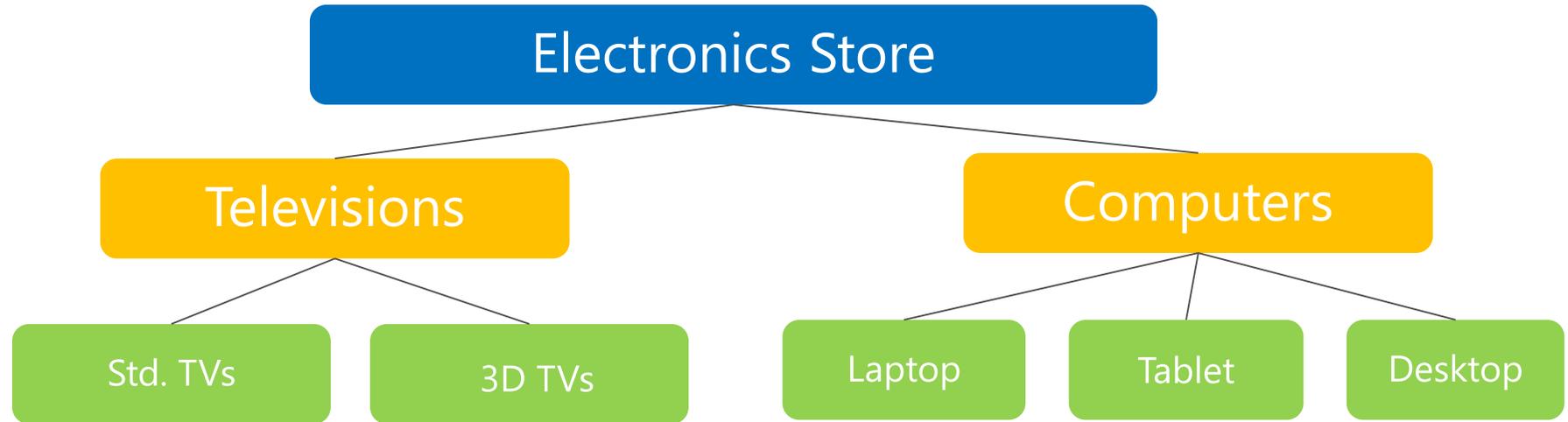
Account

Campaign

Ad Group

Ad Copy

Keyword

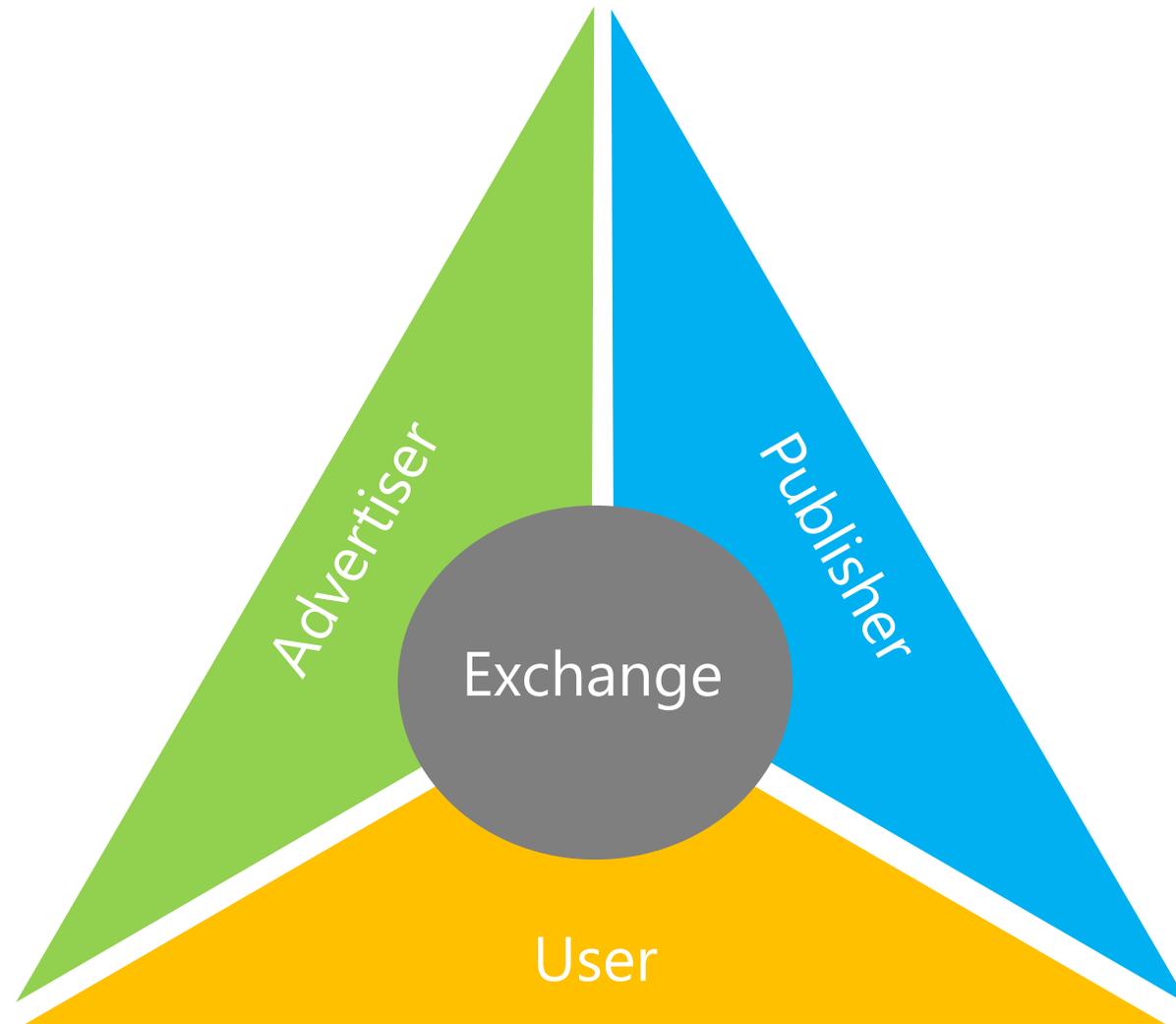


?

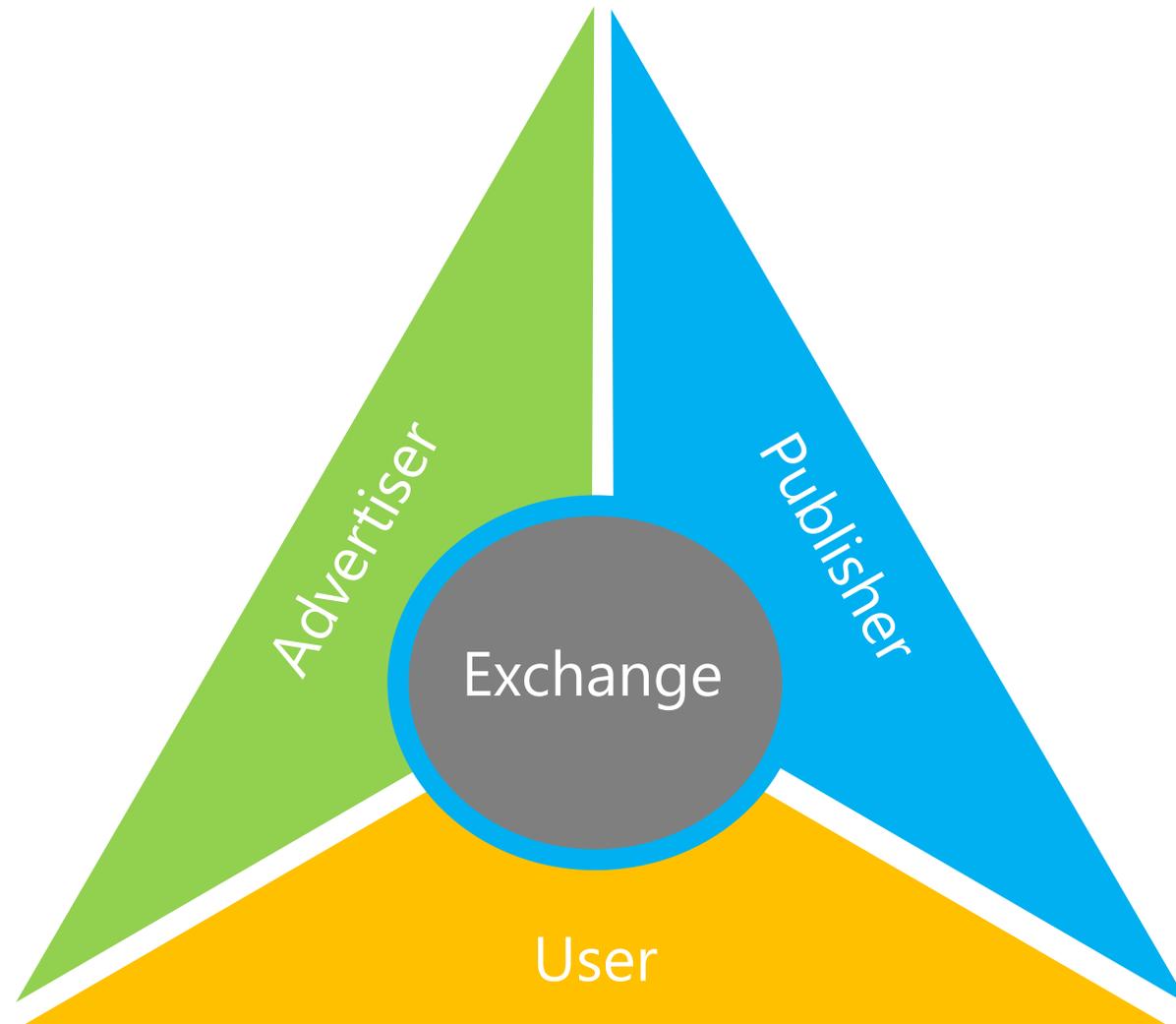
# Campaign Schema - Targeting

- Demographic
- Location
- Language
- Network
- Device
- IP
- Websites
- Day of the week
- Time of the day

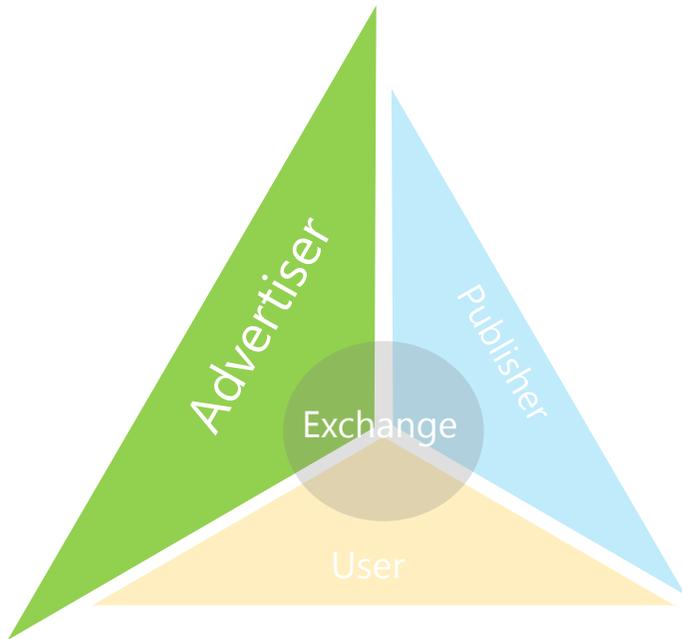
# Paid Search Participants



# Paid Search Participants



# Paid Search Participants: Advertiser's Utility

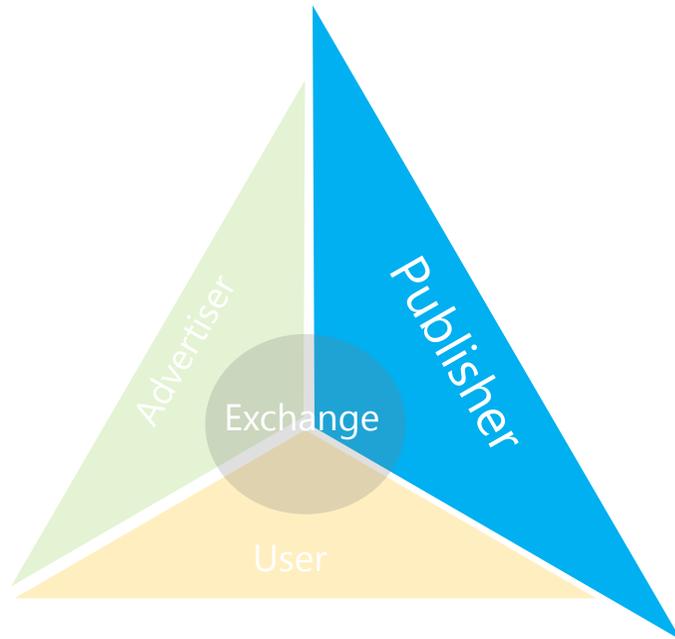


## Return on Marketing Spend (RoI)

- Volume of clicks
- Low cost per click
- Landing-Page activities
  - High click to conversion
  - High transaction value
  - User dwell time



# Paid Search Participants: Publisher's Utility

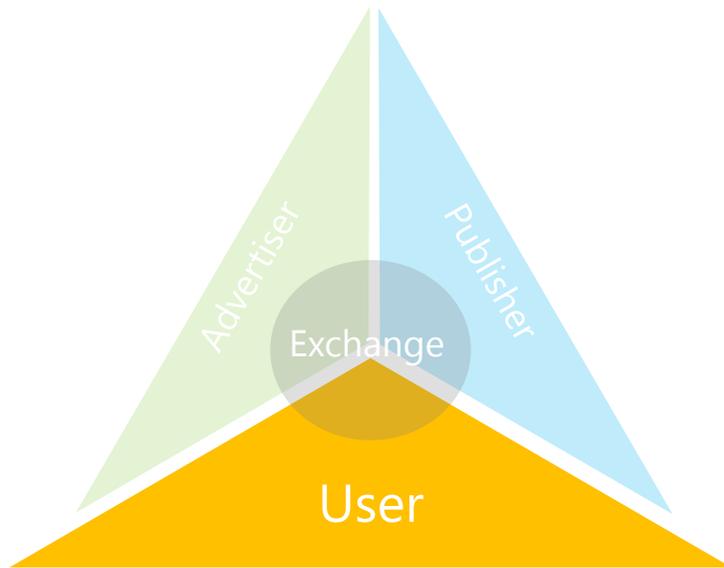


## Revenue

- Volume of clicks \* Cost per click
- Low variance in revenue and other KPIs
- Revenue growth potential
- Low operational cost
- Continued user patronage
  - Quality of ads
  - Brand image

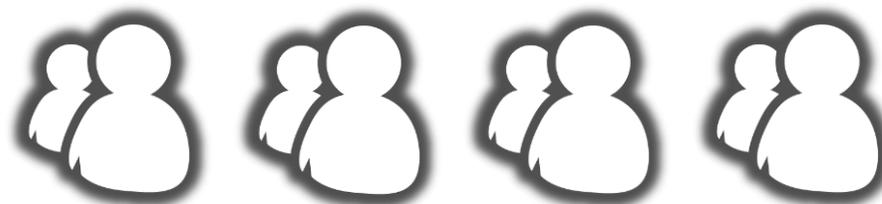


# Paid Search Participants: User's Utility



## Overall Experience

- Ads must help task completion
- Ads must not be intrusive
- No spams and malwares
- Honors privacy
- Ads must not be inappropriate – adult, gambling etc.

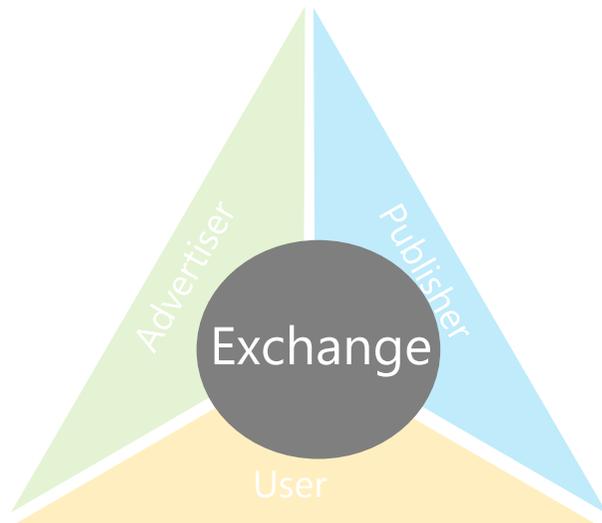


# Paid Search Participants: ... and the contradiction\*

Event		Advertiser	Publisher	User
CPC	↑			
CPC	↓			
Coverage	↑			
Coverage	↓			
IY	↑			
IY	↓			
Fraudulent Clicks	↑			
Fraudulent Clicks	↓			

\*: To be interpreted with appropriate context

# Paid Search Participants: Exchange's Utility



- Maximize volume of transactions on the platform
- Minimize the cost to serve
- Grow the network

bing Ads

Google  
AdWords

# Paid Search Participants: Growth Strategy for Exchange

Build a healthy marketplace that is attractive for all the participants

*How is this done?*

...by optimizing for a goal to maximize combined utility of Advertisers, Publishers and Users and satisfactorily managing the contradiction in their utilities

*...in other words, by*

building technology to find the **“best match”** between a **given user** and a **suitable advertisement** in a **given context**.

# Paid Search Participants: Growth Strategy for Exchange

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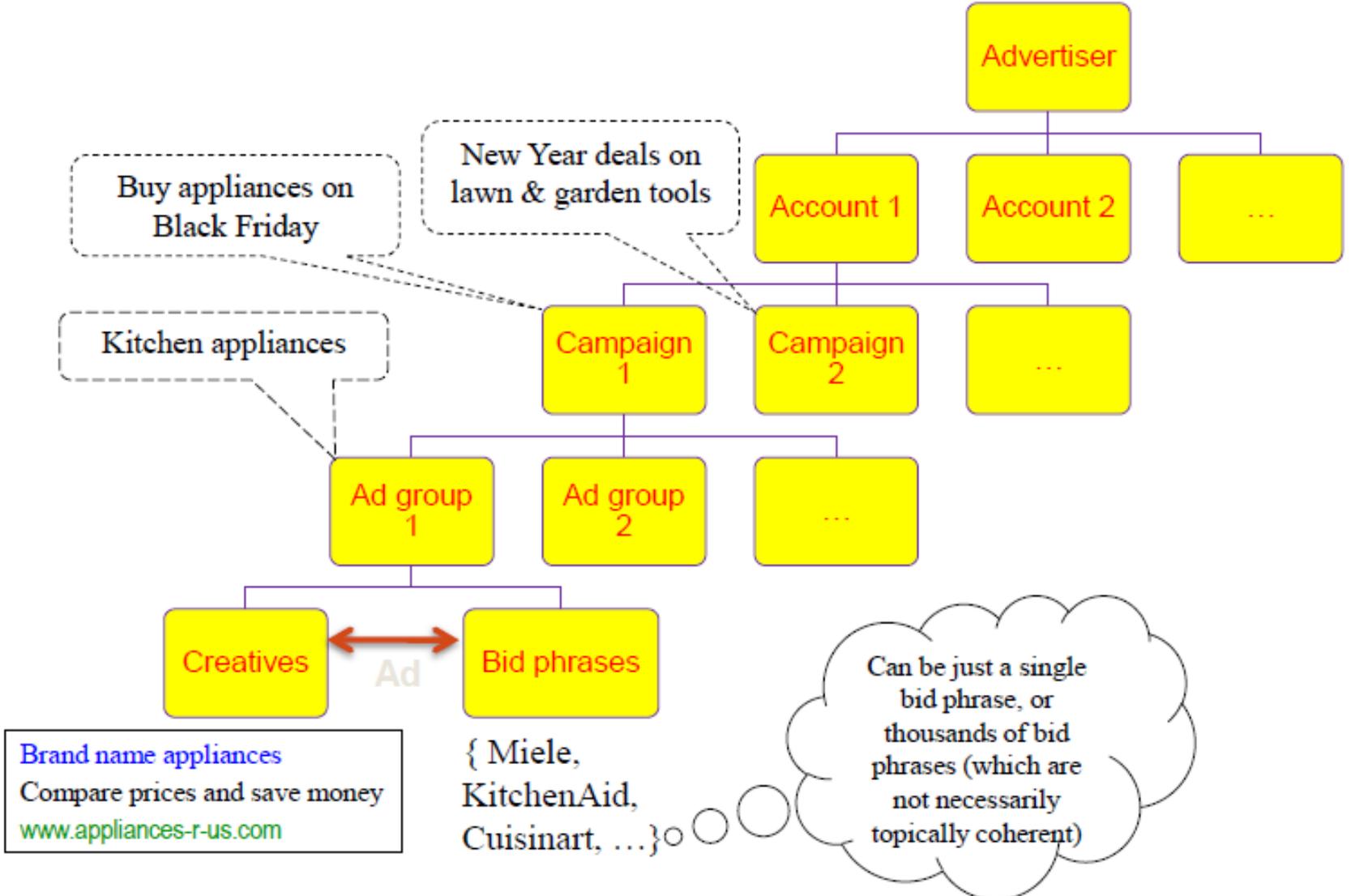
# Designing the Machine

Slides contributed by  
Dr. Manish Gupta, Sr. Applied Scientist, Microsoft  
([gmanish@Microsoft.com](mailto:gmanish@Microsoft.com))

# Anatomy of a Sponsored Search Ad



# Textual Ad Schema



# Main Issues

- Given a query
  - ✓ Select the top-k ads to be shown on the k slots in order to maximize total expected revenue
- What affects the total revenue
  - ✓ Relevance of the ad to the query
  - ✓ Bids on the ads
  - ✓ User experience on the landing page (ad quality)

# Selecting an Ad

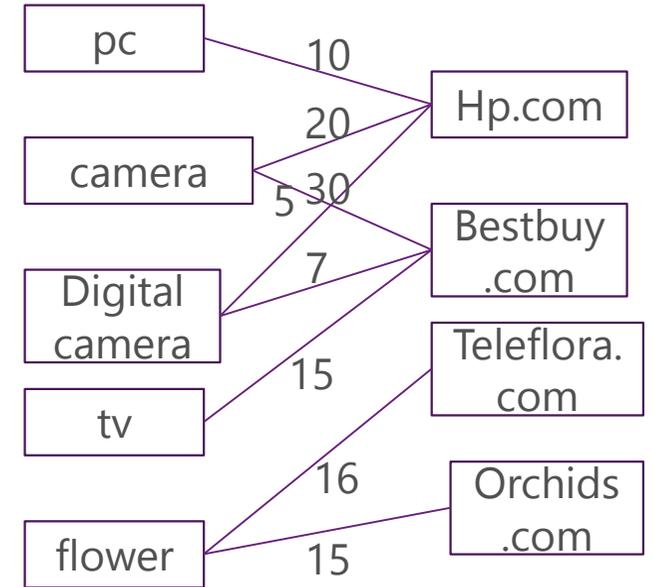
- Each participant has its own utility
  - ✓ Advertisers want ROI and volume
  - ✓ User wants relevance
  - ✓ Publisher wants revenue per impressions/search
  - ✓ Ad network wants revenue and growth
- Ad selection: optimize for a goal balancing the four utilities
- IR based Ad Relevance Computation
  - ✓ Use a search engine to match ads to context
    - ❖ Ads are the "documents"
    - ❖ Context (user query or webpage content) are the query
  - ✓ Problem: word matches might not always work
  - ✓ Need to extract topical information
- Machine learning from clicks
  - ✓ Estimate  $CTR = Pr(\text{click} | \text{ad}, \text{query}, \text{user})$
  - ✓ Ad-Ad similarity & collaborative filtering
- Bid value for ad (usually second price auction is used)

# Ad Selection Approaches

- Exact match
  - ✓ The ad's bid phrase matches the query
  - ✓ Need query normalization
  - ✓ Cannot bid on all feasible queries
- Broad match: translate the query into bid phrases
  - ✓ The ad platform finds good ads for a given query (the advertiser did not bid on that specific keyword, but the query is deemed of interest to the advertiser)
  - ✓ Pricing can be misleading
  - ✓ Significant portion of the traffic has no bids

# Query Rewriting

- Rewrite the user query  $q$  into  $Q' = (q_1, q_2, L)$
- Use exact match to select ads for  $Q'$
- Offline vs Online
  - ✓ Offline can be done only for queries that repeat often
  - ✓ Online
    - ❖ For rare queries offline not practical or simply does not work
    - ❖ Lot less time to do analysis (a few ms)
- Using search logs (frequent rewrites from query logs)
  - ✓ Insertions: game codes -> video game codes
  - ✓ Substitutions: john wayne bust -> john wayne statue
  - ✓ Deletions: skateboarding pics -> skateboarding
  - ✓ Spell correction: real eastate -> real estate
  - ✓ Specialization: jobs -> marine employment
- Using clicks
  - ✓ SimRank on bipartite graph of queries and ads
  - ✓ Edge weights could be #clicks for (ad, query) pair or CTR
  - ✓ Iterative computation
    - ❖ "Two queries are similar if they are connected to similar ads"
    - ❖ "Two ads are similar if they are connected to similar queries"



## Similar Queries

Camera – Digital Camera

pc – camera

pc – digital camera

tv – camera

tv – digital camera

pc-tv

# Ad Relevance by Online Learning

- Offline (batched) learning
  - ✓ Learned from historical data
  - ✓ Slow response to emerging patterns
  - ✓ Initial biases never corrected
    - ❖ if the system never showed “golf classes” for “iPod” it can never learn if this matching is good.
- Online learning
  - ✓ Combine exploitation with exploration
  - ✓ Pick ads that are good according to current model
  - ✓ Pick ads that increase your knowledge about the entire space of ads

# Online Content Matching

- Web advertising for two types of web pages
  - ✓ Static page (Offline):
    - ❖ Matching of ads can be based on prior analysis of their entire content
    - ❖ Works well for static content pages that are displayed repeatedly
  - ✓ Dynamic page (Online):
    - ❖ Ads need to be matched to the page while it is being served to the end-user.
    - ❖ Limiting the amount of time allotted for its content analysis.
- When a user views a page, the ad selection engine has only a couple hundred milliseconds to provide the ads.

# Collaborative Filtering Connection

- Traditional IR based-on fixed query-result relevance
- Ads: Rank by CTR probability
  - ✓ Continuous CTR feedback for each (query, ad) pair
  - ✓ Learn the “best match between a user in a given context and a suitable advertisement”
- Data is sparse, in order to get the best match, we need to find similar ads, pages, and users
- Make use of dyadic interaction systems (recommendation systems)
  - Note dyad is a pair: (user, movie), (user, ad), etc.
  - Predict response to unknown dyads using collaborative filtering

# Sponsored Search (Big Picture)

- Ads corpus = Bid phrases + Title + URL + landing page
- Ad query = Search keywords + context (location, user profile, search history)
  - ✓ Sponsored Search: Context = Web search results
  - ✓ Content match, banners: Context=Publisher page
- Ad search is similar to web search but with these differences
  - ✓ Ad database is smaller
  - ✓ Ad database entries are small
  - ✓ Ranking depends also on bids and CTRs
  - ✓ The query (current page) can be much larger than the target document
- Finding the best textual ad is an information retrieval problem with multiple, possible contradictory utility functions

# Probability of Click Estimation

Given:

{Query, Ad, Keyword}

Produce:

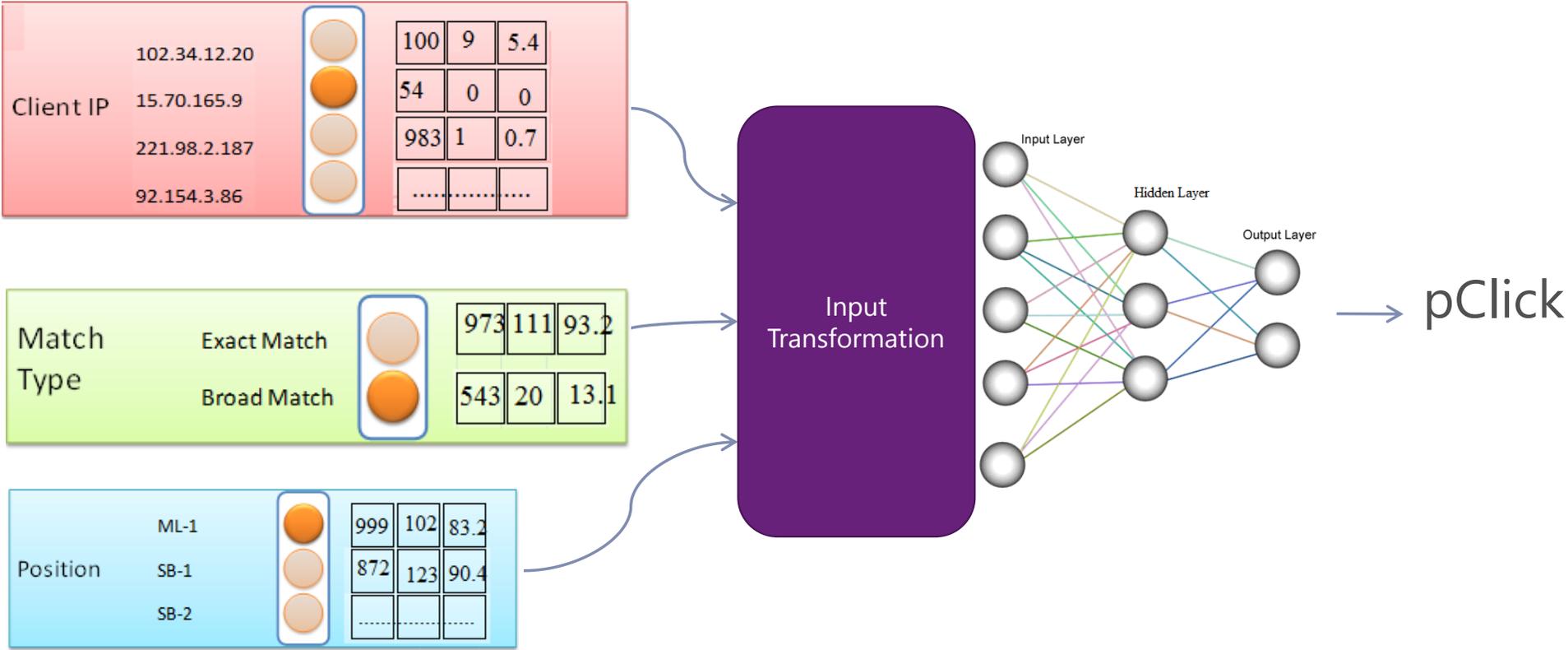
Predicted CTR:

$p\text{Click} \sim \text{CTR}$

Uses:

Ranking, Allocation and Pricing

# Probability of Click Estimation



pClick is learnt using Logistic Regression or Neural Net type models

# Interactions in Sponsored Search

- Advertisers
  - ✓ Submit ads associated to certain bid phrases
  - ✓ Bid for position
  - ✓ Pay CPC
- Users
  - ✓ Make queries to search engine, expressing some intent
- Search engine
  - ✓ Executes query against web corpus + other data sources
  - ✓ Executes query against the ad corpus
  - ✓ Displays a Search Results Page (SERP) = integration of web results, other data, and ads

# Budget and Other Factors

- Advertisers can specify budgets
- Budgets can be implemented as follows
  - ✓ Spend it quickly till out of money
  - ✓ Spend it slowly till end-of-day
  - ✓ Spend it as the search engine sees fit
  - ✓ Spend it on a certain demography of users only
- There are sometimes “reserve prices”
  - ✓ Minimum cost to be shown on a given kw (depends on kw)
- There are sometimes “minimum bids”
  - ✓ Minimum bid required to participate in action (could depend on advertiser and keyword)

# Three Problems for a Search Engine

- Ad retrieval
  - ✓ Match to query/context
- Ordering the ads
- Pricing on a click-through

# Closer Look at Auctions

Slides contributed by  
Dr. Manish Gupta, Sr. Applied Scientist, Microsoft  
([gmanish@Microsoft.com](mailto:gmanish@Microsoft.com))

# Short Introduction to Game Theory

- Set of players.
- A set of strategies available to those players (each has its own set)
- A specification of payoffs for each player for each combination of strategies.
- Each player's payoff depends on the strategy chosen by every other player!
- Dominant strategy
  - ✓ Strategy = a complete definition of how a player will play a game.
  - ✓ Strategy X (for a player) dominates another strategy Y if for all choices by other player(s), X yields at least as much payoff as Y.
  - ✓ Strategy X is dominant if it dominates all other strategies.

# Nash Equilibrium

- Nash equilibrium
  - ✓ choice of strategies in which each player is assumed to know the equilibrium strategies of the other players, and no player has anything to gain by changing his own strategy unilaterally.
- Pure strategy
  - ✓ deterministic definition of how a player will play a game
- Mixed strategy
  - ✓ an assignment of probabilities to each pure strategy --the players throw coins to pick the strategy they follow
- A game could have many Nash equilibria or none, if players must follow pure strategies.
- Nash theorem:
  - ✓ In every  $n$ -player game in which every player has finitely many pure strategies there exists a set of mixed strategies that forms a Nash equilibrium.

# Game Theory for Ads

- Advertisers make bids (their moves)
- Advertiser seek attention and volume – prefer higher positions
- Engines order ads and price clicks according to some rules known to all bidders
- The bidders can all keep reacting to each other

# Types of Auctions

- First-price sealed-bid
  - ✓ Bidders place their bid in a sealed envelope
  - ✓ Simultaneously give them to the auctioneer.
  - ✓ Highest bidder wins, pays his bid.
- Second-price sealed-bid auctions (Vickrey auctions)
  - ✓ Bidders place their bid in a sealed envelope
  - ✓ Simultaneously give them to the auctioneer.
  - ✓ Highest bidder wins, pays price equal to the second highest bid.
- Open Ascending-bid auctions (English auctions)
  - ✓ Price is steadily raised by the auctioneer
  - ✓ Bidders drop out once the price becomes too high.
  - ✓ Eventually there is only one bidder who wins the auction at the current price.
- Open Descending-bid auctions (Dutch auctions)
  - ✓ Price starts at infinity and is steadily lowered by the auctioneer
  - ✓ The first bidder to accept the current price, wins
  - ✓ Pays the current price.

# Second Price Auction (Vickrey Auction)

- All buyers submit their bids privately
- Buyer with the highest bid wins; pays the price of the second highest bid



# Truthfulness (Incentive Compatibility) of Vickrey Auction

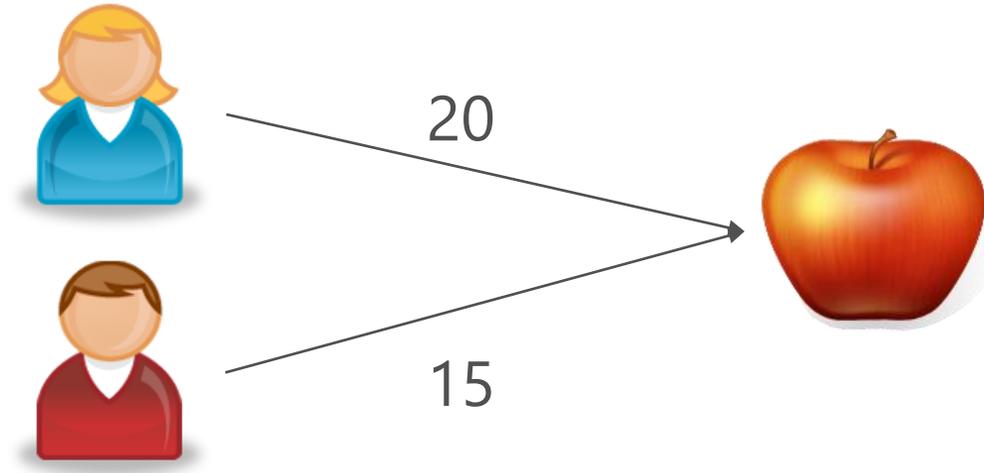
- An auction mechanism is truthful, if the dominant strategy for every player is to truthfully bid their own value.
- Telling the truth is optimal in second-price (Vickrey) auction
- Suppose your value for the item is \$100; if you win, your net gain (loss) is \$100-price
- If you bid more than \$100
  - ✓ You increase your chances of winning at price  $> \$100$
  - ✓ You do not improve your chance of winning for  $< \$100$
- If you bid less than \$100
  - ✓ You reduce your chances of winning at price  $< \$100$
  - ✓ There is no effect on the price you pay if you do win
- Dominant optimal strategy: bid \$100
- Key: The price you pay is out of your control
- Vickrey's Nobel Prize due in large part to this result!



# Vickrey-Clark-Groves (VCG)

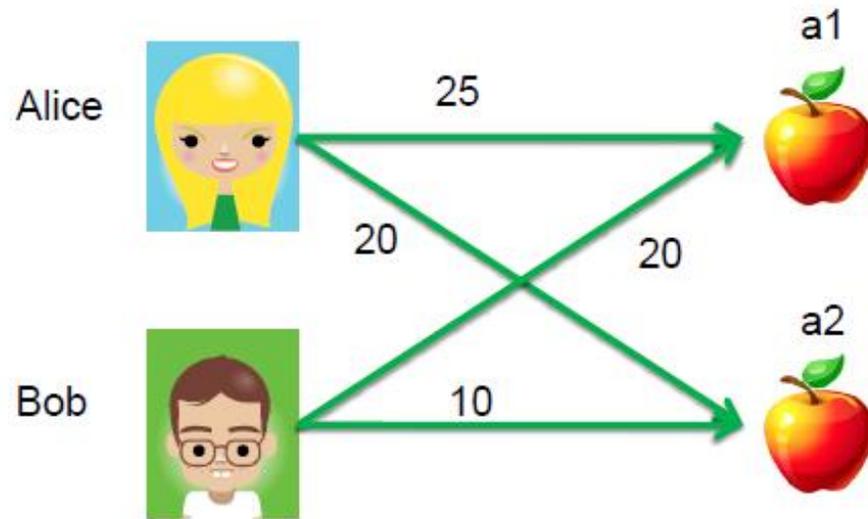
- Generalization of Vickrey
- Works for arbitrary number of goods, including allowing combination bids
- Auction procedure:
  - ✓ Collect bids
  - ✓ Allocate goods to maximize total social value (goods go to those who claim to value them most) = maximum weighted matching
  - ✓ Payments: Each bidder  $b$  pays his externality =  $(\text{max TSV without } b\text{'s participation}) - (\text{max TSV for everyone else when } b \text{ participates})$
  - ✓ NB:  $(\text{max TSV for everyone else when } b \text{ participates}) = \text{max weighted matching without } b \text{ \& without } b\text{'s items.}$
- Incentive compatible (truthful) = all the bidders do best when they bid their true value i.e. reveal their private information

# VCG Example



- Price paid by Alice for her apple does not depend on her bid
  - ✓ Should not bid more than her value –might pay too much!
  - ✓ Should not bid less –might not get it!
- Thus VCG leads to truthfulness

# VCG Example



Max matching = 40  $\rightarrow$  A gets a2, B gets a1

Max matching without Bob = 25

Max matching without Bob, without a1 = 20

- **Bob pays 5**

Max matching without Alice = 20

Max matching without Alice, without a2 = 20

- **Alice pays 0**

- Max matching without Alice does not depend on her bids
- Max matching without Alice and her assigned apple does not depend on her bids
- Price paid by Alice for her apple does not depend on her bid
  - ✓ Should not bid more than her value –might pay too much!
  - ✓ Should not bid less –might not get it!
- Thus VCG leads to truthfulness

# How does the sponsored search auction work

- Search engines
  - ✓ run keyword auctions to sell available inventory of ad positions
- Advertisers
  - ✓ submit bids which indicate their willingness-to-pay per click
    - ✓ for example, bid of \$1.75 per click for the keyword "laptop"
- The search engine orders the ads in descending order
  - ✓ Bid is a key determinant of ad position
  - ✓ Other factors such as CTR are also factored in

# Unique Features of the Market for Internet Ads

- Bidding takes place continuously
- The search engines effectively sell flows (clicks/hour)
- Not unlike electricity markets unused capacity is wasted
- On the other hand, user utility might be impaired by excessive advertisement

# "Unit" of Advertisement

- Advertiser's perspective: transaction is a "unit"
  - ✓ Pricing model: pay per transaction (CPT/CPA)
- Search engine's perspective: exposure is a "unit" (CPM)
  - ✓ Pricing model: pay per exposure
- Middle ground: click is a "unit"
  - ✓ Pricing model: pay per click (CPC)
- All three pricing models are widely used
- Pay per click dominates sponsored search

# Generalized First-Price Auctions

- 1997 auction revolution by Overture (then GoTo.com, created at Idealab)
- Pay per-click for a particular keyword
  - ✓ Initially crazy idea, meant to combat search spam
  - ✓ Search engine “destination” that ranks results based on who is willing to pay the most
  - ✓ With algorithmic search engines out there, who would use it
  - ✓ Commercial web sites would! (Much better than to depend on ranking!)
- Results
  - ✓ Links arranged in descending order of bids
  - ✓ Pay your bid (First price)
  - ✓ Overture became a platform for Yahoo! and MSN--Imperfect mechanism: unstable due to dynamic nature of the environment
- Problem: GFP is unstable because bids can be adjusted dynamically

# Example on GFP

- Two slots and three bidders
  - ✓ ad in first slot: 200 clicks per hour
  - ✓ ad in second slot: 100.
- Bidders 1, 2, and 3 have values: \$10, \$4, and \$2
- If bidder 2 bids \$2.01, to make sure he gets a slot
- Bidder 1 will not want to bid more than \$2.02
- Bidder 1 gets the top spot, but then bidder 2 will want to revise his bid to \$2.03 to get the top spot
- Bidder 1 will in turn raise his bid to \$2.04, and so on.

# Generalized Second-price Auctions

- Generalized Second-Price (GSP) Auctions
- 2002 GSP implemented by Google
- Yahoo!/Overture and others switched to GSP
- Two way of generalizing:
  - ❖ Bid ranking: Order the ads by their bids. Rename ads so ad  $i$  ends in position  $i$ . Bidder in position  $i$  pays  $\text{bid}(i+1)$ .
  - ❖ Revenue ranking: Order the ads by expected revenue in position  $i$  assuming maximum bids, that is by  $b(i) \cdot \text{ctr}(i)$ 
    - Rename ads so ad  $i$  ends in position  $i$ .
    - Bidder in position  $i$  pays  $\text{bid}(i+1) \cdot \text{ctr}(i)$
    - Note that bidder  $i$  pays less than  $\text{bid}(i)$  since  $\text{bid}(i) \cdot \text{ctr}(i) > \text{bid}(i+1) \cdot \text{ctr}(i+1)$
    - If all CTRs are the same, revenue ranking is the same as bid ranking!
- CTR can be estimated for an advertiser based on click history

# GSP Example

- Same example under GSP mechanism with bid ranking
- Two slots and three bidders.
  - First slot 200 clicks per hour regardless of ad
  - Second slot gets 100 regardless of ad
  - Bidders 1, 2, and 3 have values per click of \$10, \$4, and \$2, respectively.
- If all advertisers bid truthfully, then bids are \$10, \$4, \$2.
  - Payments for slot one and two are \$4 and \$2 per click.
  - Total payment of bidder 1 is \$800 = \$1200 pay-off
  - Total payment of bidder 2 is \$200 = \$200 pay-off
  - In this example truth-telling is an equilibrium because no bidder can benefit by changing his bid.

# Is GSP a VCG?

- GSP is not VCG -- GSP has no dominant strategies
- Truth-telling is generally not an equilibrium
- With only one slot, VCG and GSP are identical
- With several slots, the mechanisms are different
  - GSP charges bidder  $i$  the bid of bidder  $i+1$  (In practice + \$0.01)
  - VCG charges bidder  $i$  for his externality

# Truth-telling is not a dominant strategy under GSP

- Proof: Example with three bidders and two slots
- Per click values are \$10, \$4, and \$2
- CTR's are 200 and 199
- (Assume all ads are equally attractive)
- If all bid truthfully bidder 1 bids \$10 and pays \$4 so his payoff is
  - $(\$10 - \$4) * 200 = \$1200$
- If bidder 1 bids \$3 (and pays \$2) his payoff is:
  - $(\$10 - \$2) * 199 = \$1592 > \$1200$

# Same Example using VCG

- Let us compute VCG payments for the example considered before.
  - Two slots and three bidders.
    - First slot 200 clicks per hour
    - Second slot gets 100.
    - Bidders 1, 2, and 3 have values per click of \$10, \$4, and \$2, respectively.
- The second bidder's payment is \$200, as before (externality imposed on 3 who loses \$200 = value for him of the slot he does not get!)
- However, the payment of the first advertiser is now \$600
  - \$200 for the externality that he imposes on bidder 3 (by forcing him out of position 2) +
  - \$400 for the externality that he imposes on bidder 2 (by moving him from position 1 to position 2 and thus causing him to lose  $(200-100)=100$  clicks per hour).
- Note that in this example, revenues under VCG are lower than under truth telling equilibrium of GSP!

# What do we have?

- GFP is not stable
- Choose between GSP and VCG
  - GSP is not truthful
  - VCG is truthful and stable but not really used (revenue?)
- Adaptation of VCG
  - The higher the bid, the better the position
  - The last bidder to get a slot pays same as GSP
  - Total payment of bidder in position  $i$  under VCG,  $p(i)$
  - $p(i) = (\alpha_i - \alpha_{i+1})b_{i+1} + p(i + 1)$ 
    - $\alpha_i$  is expected number of clicks at position  $i$
    - $b_i$  is bid of  $i^{th}$  highest bidder

# Take-away Messages

- Computational Advertising is a new growing field with lots of interesting problems.
- Two main types of ads are display ads and textual ads.
- We studied interesting problems in displaying graphic ads and textual ads.
- Finally, we discussed various auction mechanisms like GFP, GSP, VCG and an adaptation of VCG

# Further Reading

- Algorithmic Challenges in Online Advertising, Deepak Agrawal and Deepayan Chakrabarti. CIKM 2008 Tutorial
- Computational Advertising course @ Stanford: <http://www.stanford.edu/class/msande239/>
- Edelman, Ostrovsky, and Schwarz, Internet Advertising and the Generalized Second Price Auction, 2005
- Varian, Position Auctions, 2006
- Lahaie, Pennock, Saberi, Vohra, Sponsored Search, Chapter 28 in Algorithmic Game Theory, Cambridge University Press, 2007

Q&A

