

FORMAL METHODS – AN INTRODUCTION



DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR

Dr Pallab Dasgupta, Professor



FMSAFE

FORMAL METHODS FOR SAFETY CRITICAL SYSTEMS

The Evolution of Electronic Computing



1954 prediction for 2004



Computation
became free !!

1980



5 MB



32 GB

1990

Storage
became free !!

2000

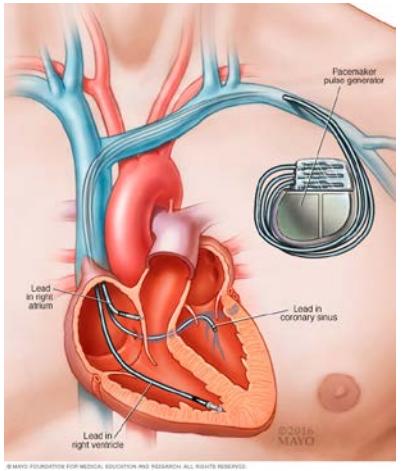


Communication
became free !!

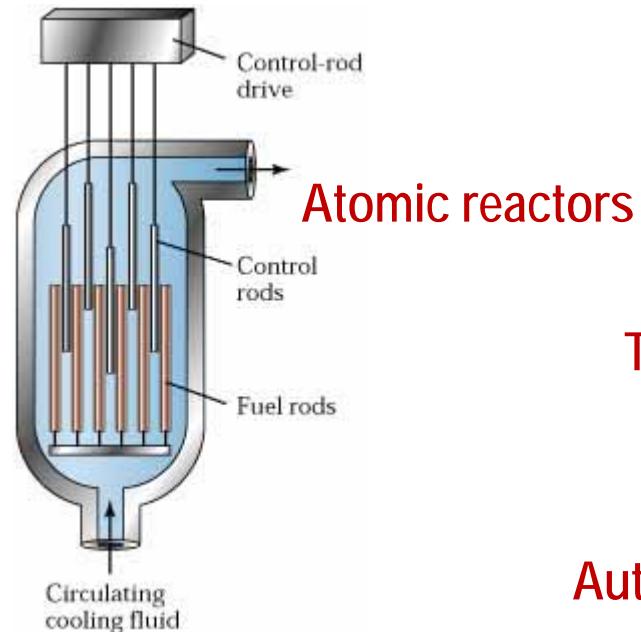


2010

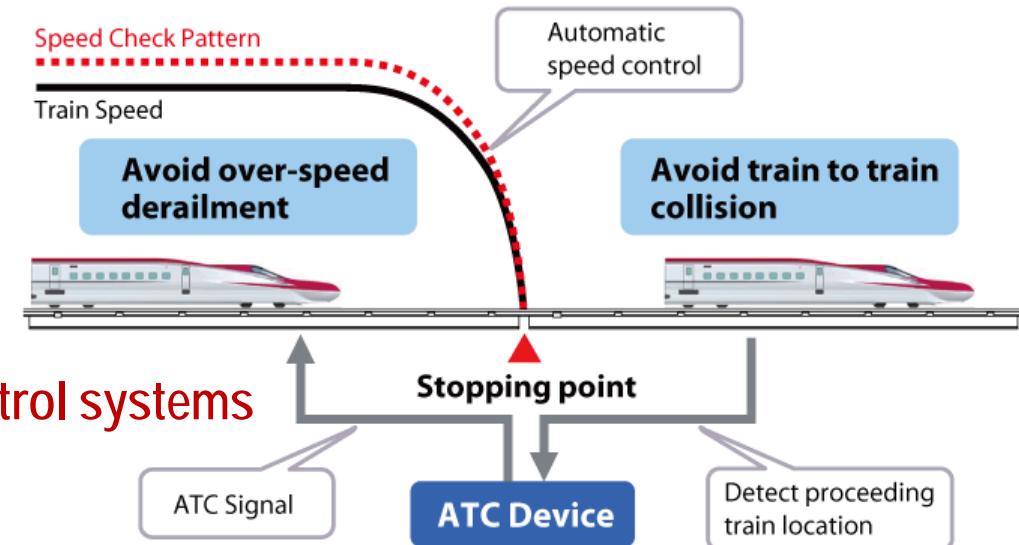
Computing is not confined to labs anymore !!



Healthcare devices

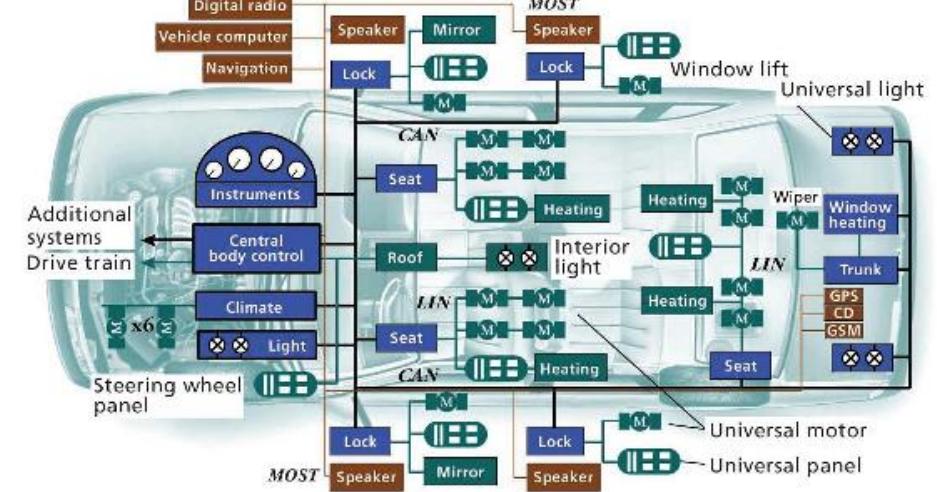


Atomic reactors



Train control systems

Automotive control systems



CAN Controller area network
GPS Global Positioning System
GSM Global System for Mobile Communications
LIN Local interconnect network
MOST Media-oriented systems transport

Modern systems are software based !!
Modern systems are designed using software !!

Safety and Computer Science

- In view of the proliferation of electronics and software in everything that we use:
 - Safety has a new meaning – the electronics and software must not do things that cause my gadgets to harm me
 - Only Computer Science can solve the problems related to cyber safety
 - Today there are at least two people in verification for every person in design. And this is true in:
 - Design of integrated circuits
 - Design of software
 - Design of control systems
- ⇒ Verification experts are in high demand in modern engineering. Yet bugs continue to haunt the industry.

Famous incidents from software bugs



Explosion of Ariane 5, 1996 due to
“.. conversion of a 64 bit integer
into a 16 bit signed integer lead to
an overflow ...”

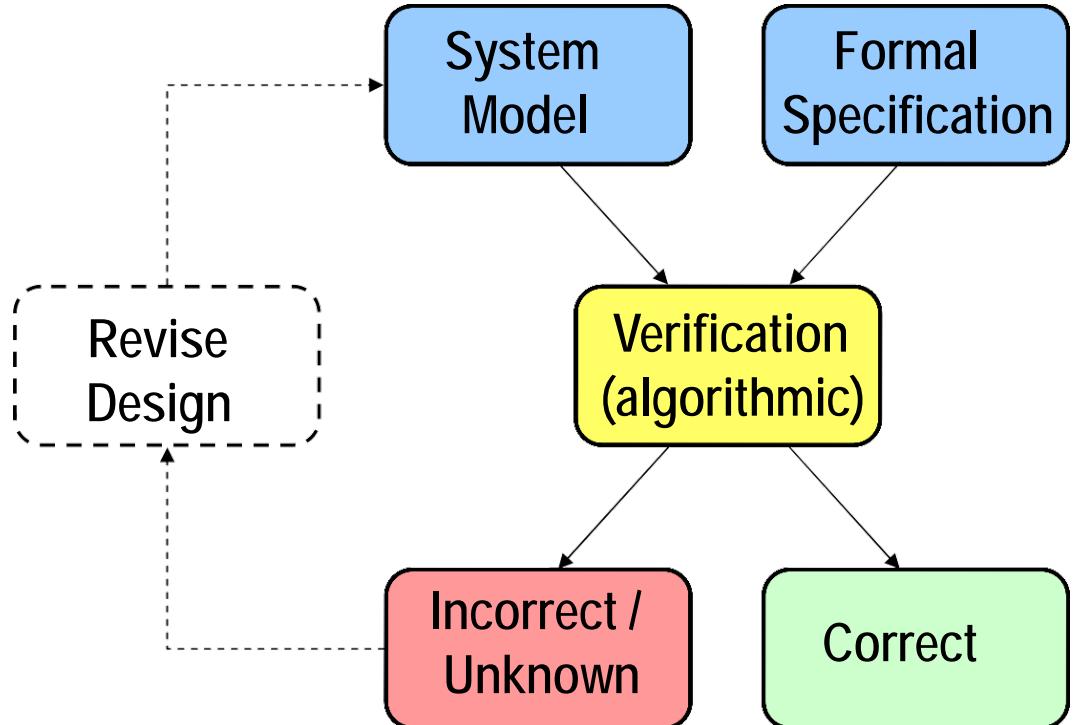


Loss of Mars Climate Orbiter, 1999 due
to “...mix-up between pounds and
kilogram....”

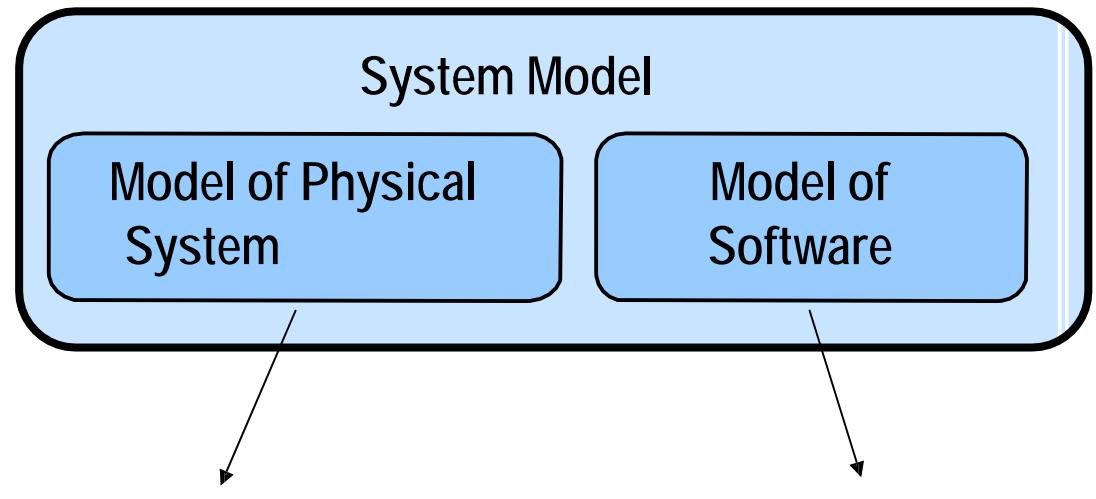


USS Yorktown died in the water,
1998 due to “....input and Division
by '0'. „ $X / 0 = \text{undefined}$...”

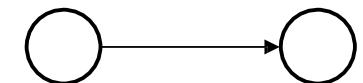
Formal Methods are used to prove designs to be correct !!



- More than 70 top scientists work in the NASA Langley formal methods group
- Top companies (Intel, IBM, Google, Microsoft, General Motors) have dedicated formal methods groups
- So does ministries of defense, atomic energy, space, etc.



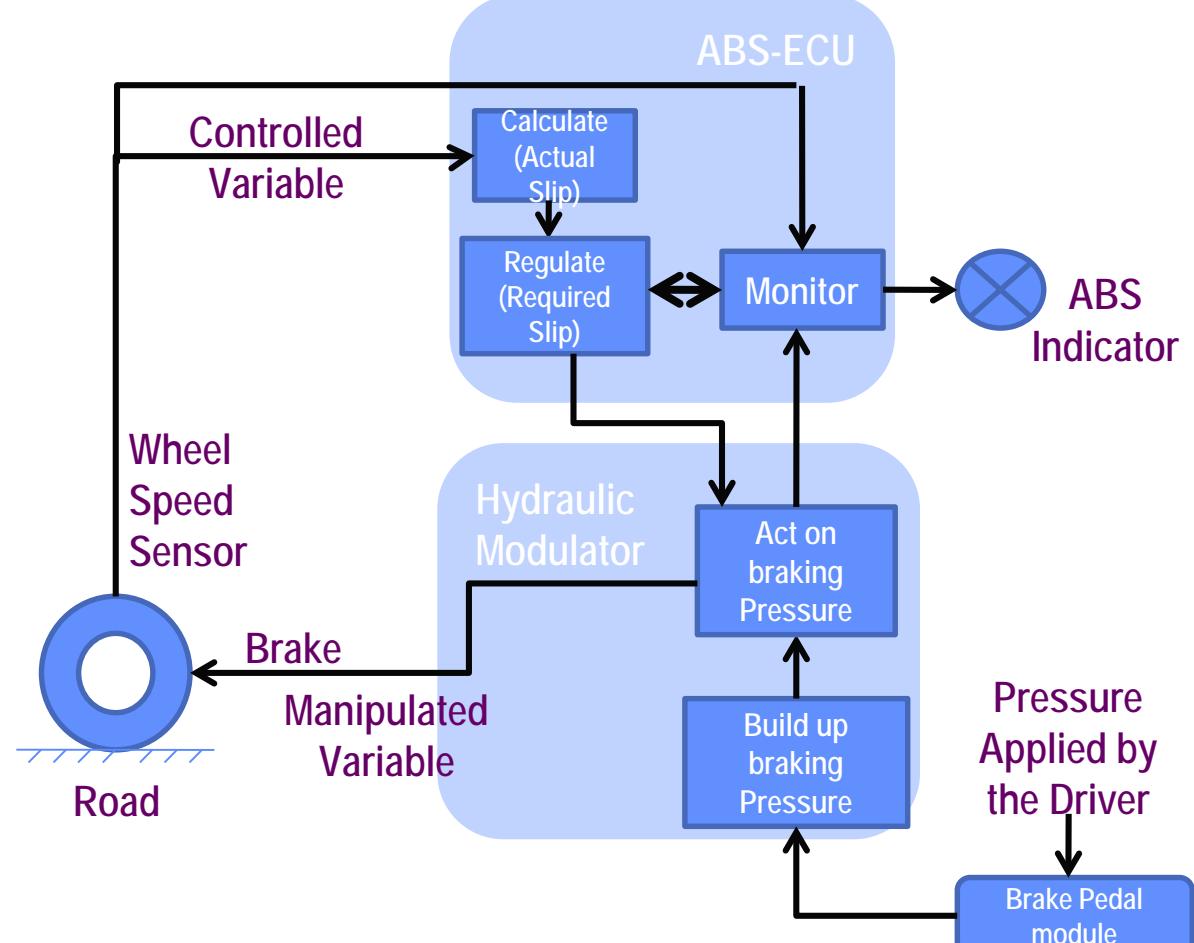
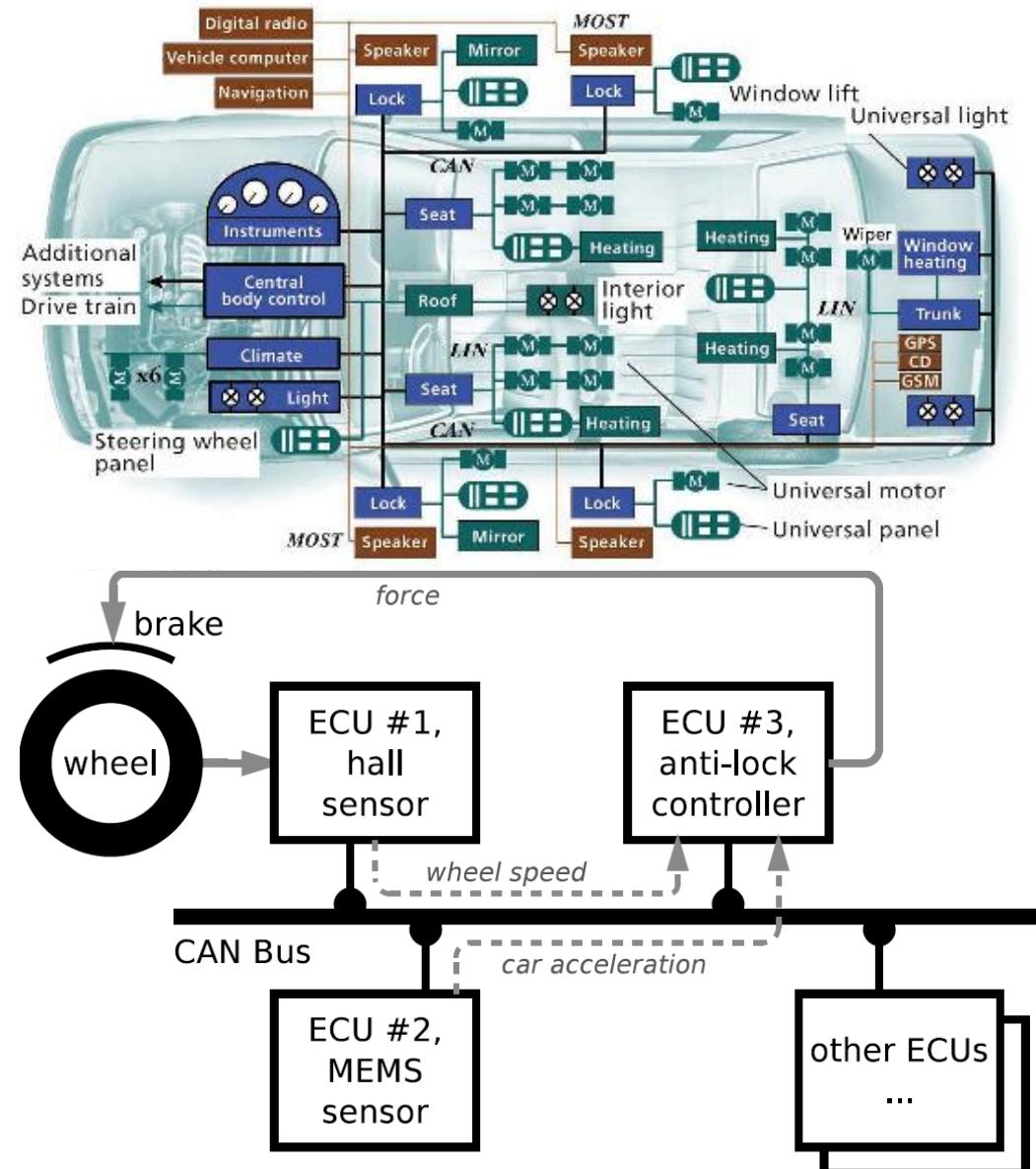
discrete and/or
continuous dynamics

$$y = y + 10$$
$$\dot{x} = f(x)$$


International Safety Standards recommending Formal Methods in Verification

- Aeronautics (DO-178C)
- Automotive (ISO 26262)
- Industrial process automation (IEC 61508)
- Nuclear (IEC 60880)
- Railway (EN 50128)
- Space (ECSS-Q-ST-80C)

Examples of Safety Critical Systems



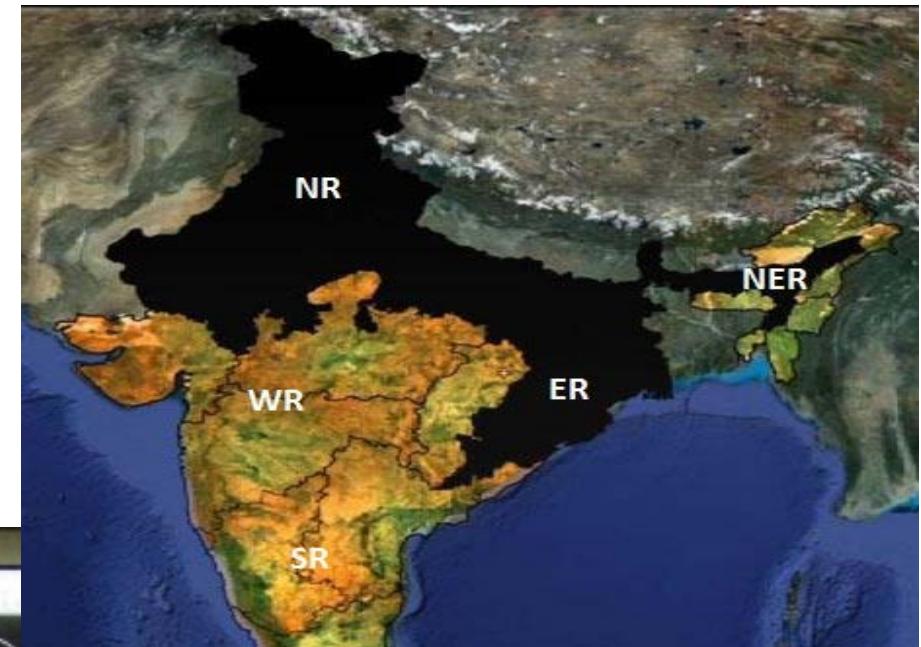
Antilock braking system (ABS)

Examples of Safety Critical Systems

- Power Grids



NATIONAL LOAD DESPATCH CENTER - Control room
At the Top of Control Hierarchy

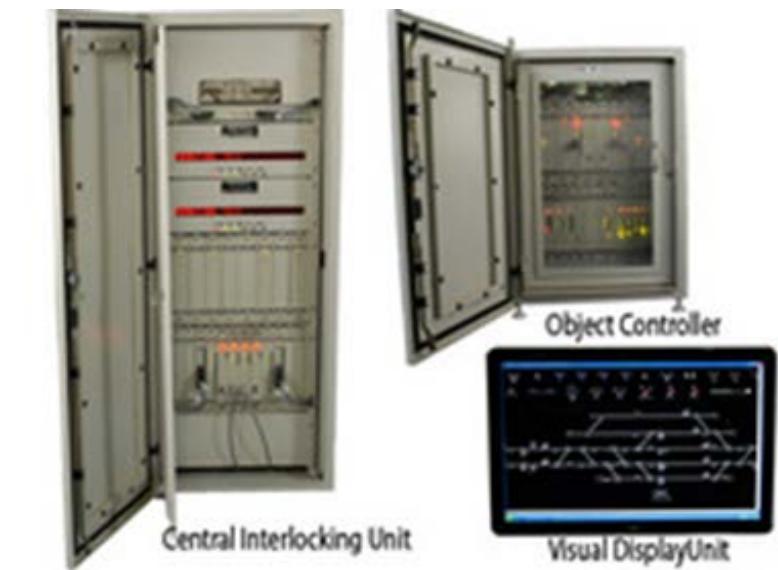
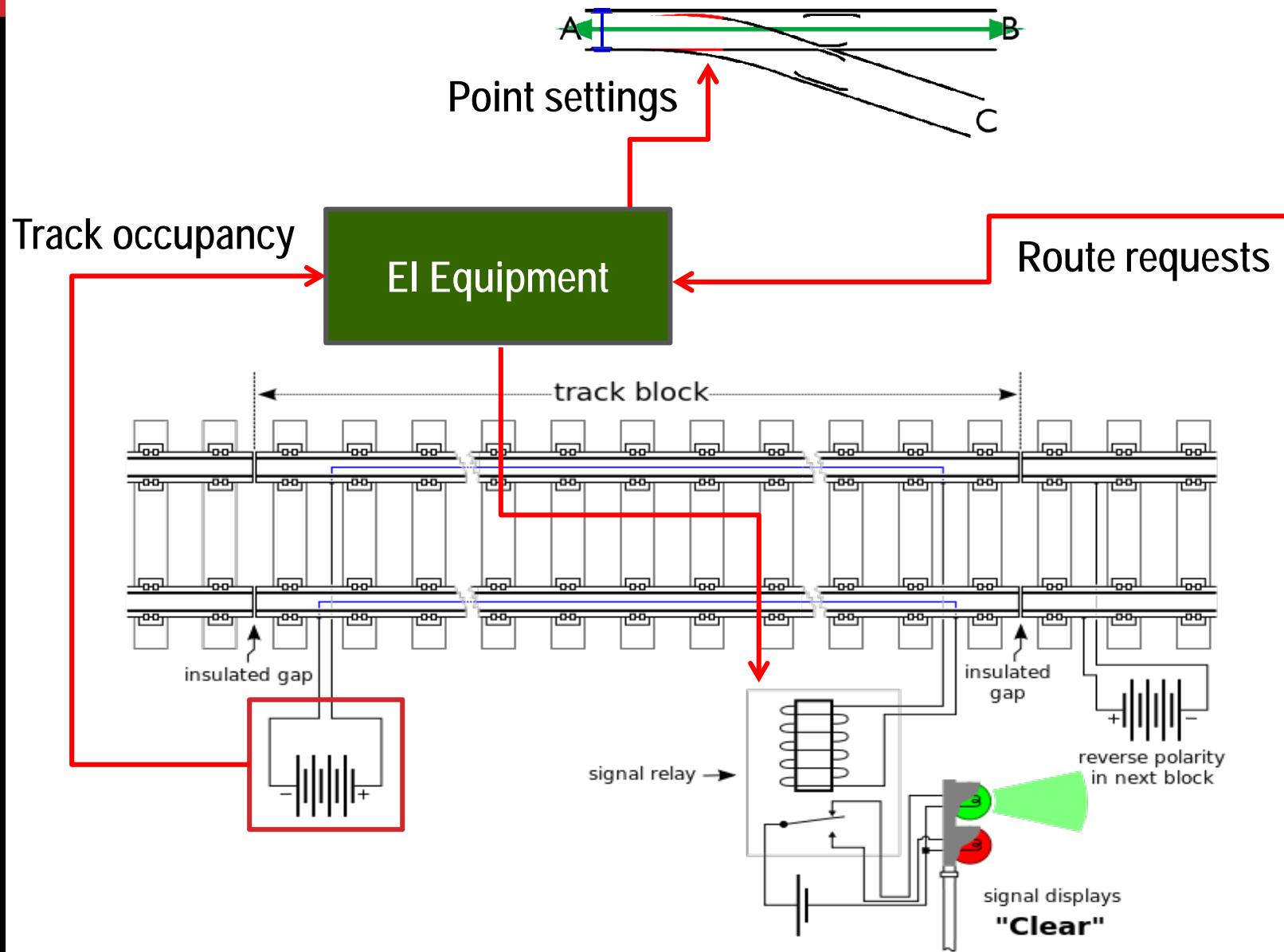


Course Topics

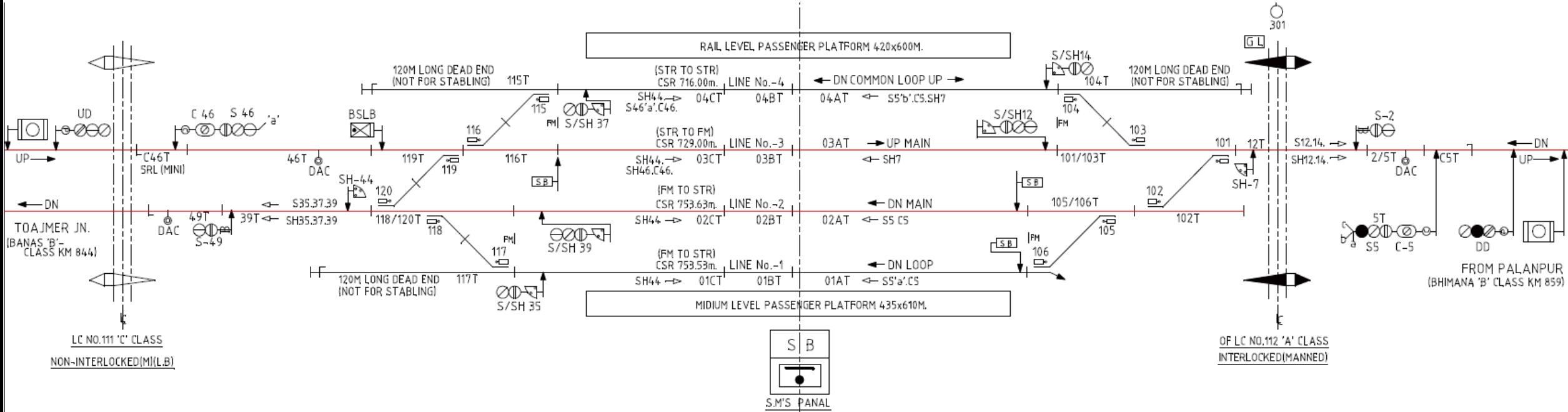
- Formal Specifications.
 - Automata over finite and infinite words, Communicating concurrent state machines, Temporal and Modal Logics, Relationship between Logic and Automata, Satisfiability, Validity and Model checking problems.
- Handling Large State Spaces.
 - Succinct representations of state spaces and their traversal, SAT and BDD-based symbolic reachability approaches, abstraction refinement approaches.
- Model Checking.
 - Temporal logic model checking, Symbolic and automata theoretic approaches.
- Formal representation of time.
 - Timed automata, Timed temporal logic, Model checking timed systems.
- Formal representation of hybrid systems.
 - Hybrid automata, Reachability problems in hybrid automata, Polyhedral approximation techniques.
- Formal analysis of programs.
 - Abstract interpretation, Predicate abstraction, Model checking software systems.
- Industrial applications of formal methods.

A Real World Case Study

Electronic Interlocking in Railways



Life-cycle of signaling logic: Step-1 (Yard Layout)



Traditionally the layout (signal plan) is created manually

- Upgradations are reflected manually on paper
 - No automatic consistency checking
 - No automatic way to guarantee that upgradations in signaling plan and control table are consistent

Life-cycle of signaling logic: Step-2 (Control Table)

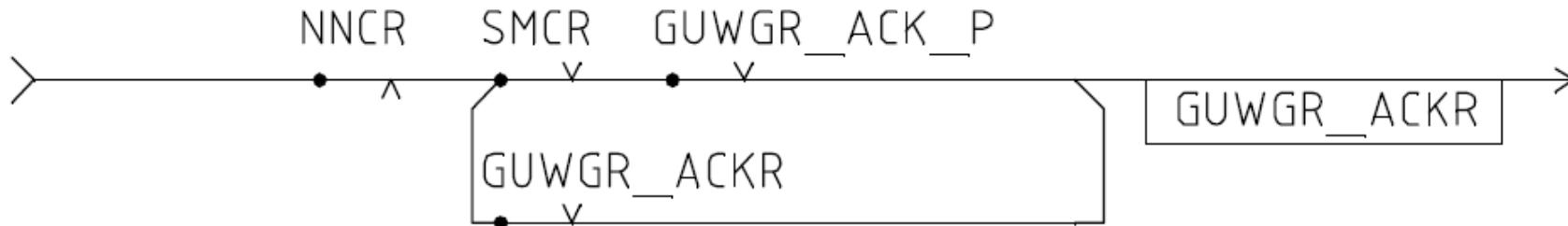
S.NO	MOVEMENT		BUTTON OPERATION		IN ROUTE						IN OVERLAP						SIGNAL TO DANGER	ROUTE RELEASED TRACK CIRCUITS OCCUPIED/CLEARED	APPROACH LOCKING	ROUTES LOCKED	SIGNAL ASPECT CONTROLLED BY		REMARKS								
	FROM	TO	GN	UN	POINTS		TRACK CIRCUITS	ISOLATION POINTS NORMAL	GATE CONTROL & OTHERS SLOTS REQUIRED NORMAL	CRANK HANDLE	POINTS		TRACK CIRCUITS	ISOLATION POINTS	GATE CONTROL & OTHERS SLOTS REQUIRED NORMAL	CRANK HANDLE															
					NORMAL	REVERSE					NORMAL	REVERSE																			
1.	S2	BHIMANA	S2	UM	-	-	2/5T	-	-	-	-	-	-	-	-	-	2/5T	-	-	-	(S5.C5-LN1 2 4) SH7-LN 3 4. SH12 SH14.	-	-	CONTROLLED BY BHIMANA SIDE SINGLE LINE TOKENLESS B/INSTT. IN TGT POSITION WITH SSDAC.							
2.	S5b	S:9	S5	02	105/106	101/102	2/5T 12T 101/103T 102T 105/106T, 02AT&BT/CT	-	301	CH-3 CH-1	117/118 119/120	-	118/120T 39T,	-	-	-	CH-6 CH-10	2/5T 12T 101/103T 102T 105/106T	2/5T	DEAD	-	C46-LN4 W 103/104 R S2 C5-LN2 SH39 SH44-LN2 C46-LN3 X	S39 R OR Y OR G	-	-						
3.	C5	S39	S3+ COGN	02	105/106	101/102	-	-	301	CH-3 CH-1	-	-	-	-	-	-	-	2/5T 12T 101/103T 102T 105/106T OR THRO'EM. CO.CANC.	-	-	-	S2 S5-LN2 S35 SH35.S37 SH37 SH39. SH44-LN1 2 3 4 C46-LN3 X (C46-LN4 W 103/104 R)	-	-	CLEAR\$ 60 SEC AFTER OCC. OF C5T & REPLACED TO 'ON' WHEN C5T IS CLEARED						
4.	S5'a'	S35	S5	01	-	101/102 105/106	2/5T 12T 101/103T 102T 105/106T, 01AT&BT/CT	-	301	CH-1 CH-3	117/118 119/120	-	117T 117/118	-	-	CH-9 CH-10 CH-6	2/5T 12T 101/103T 102T 105/106T	2/5T 12T 101/103T 102T 105/106T	DEAD	-	S2 .C5-LN1. SH44-LN2 3 X C46-LN3 X SH44-LN4 W 103/104 R C46-LN4 W 103/104 R S2 .C5-LN1. SH35. SH44-LN1 C46-LN3 X C46-LN4 W 103/104 R	S35 R OR Y	-	-							
5.	C5	S35	S5 COGN	01	-	101/102 105/106	-	-	301	CH-1 CH-3	-	-	-	-	-	-	2/5T 12T 101/103T 102T 105/106T OR THRO'EM. CO.CANC.	-	-	-	S2 .S5-LN1. SH35. SH44-LN1 SH44-LN1 2 3 X C46-LN3 X (SH37.S37 W 117/118 R) (SH44-LN4 W 103/104 R) (117/118 R) (C46-LN4 W 103/104 R)	-	-	CLEAR\$ 60 SEC AFTER OCC. C-C5T & REPLACED TO 'ON' WHEN C5T IS CLEARED							

Traditionally the control table is created manually from the layout

- Upgradations are reflected manually on paper
- No automatic consistency checking
- No automatic way to guarantee that upgradations in control table are consistent with application logic

Life-cycle of signaling logic: Step-3 (Application Logic)

```
GUWGR_ACKR = !NNCR & ((SMCR & GUWGR_ACK_P) # GUWGR_ACKR);
```



Traditionally the application logic is created manually from the control table

- Uses traditional relay logic (ladder network) for legacy reasons
- Lack of standardization in terms of the set of relays used to define the logic
- RDSO has been working towards a standard for Indian Railways. This will significantly help if vendors are made to comply.

How would we verify 1000 pages of logic which looks like this?

S2GNR = S2GN_P & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWR;

S5GNR = S5GN_P & !S2GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWR;

SH7GNR = SH7GN_P & !S2GNR & !S5GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWNR;

S12GNR = S12GN_P & !S2GNR & !S5GNR & !SH7GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWR;

SH12GNR = SH12GN_P & !S2GNR & IS5GNR & !SH7GNR & !S12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWR;

S14GNR = S14GN_P & !S2GNR & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !EWNR;

SH14GNR = SH14GN_P & !S2GNR & IS5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & IS35GNR & !SH35GNR & !S37GNR & ISH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRBR & !FWNR;

S35GNR = S35GN_P & !S2GNR & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !S46GNR & !S49GNR & !GSBR & !GSRRB & !FWNR;

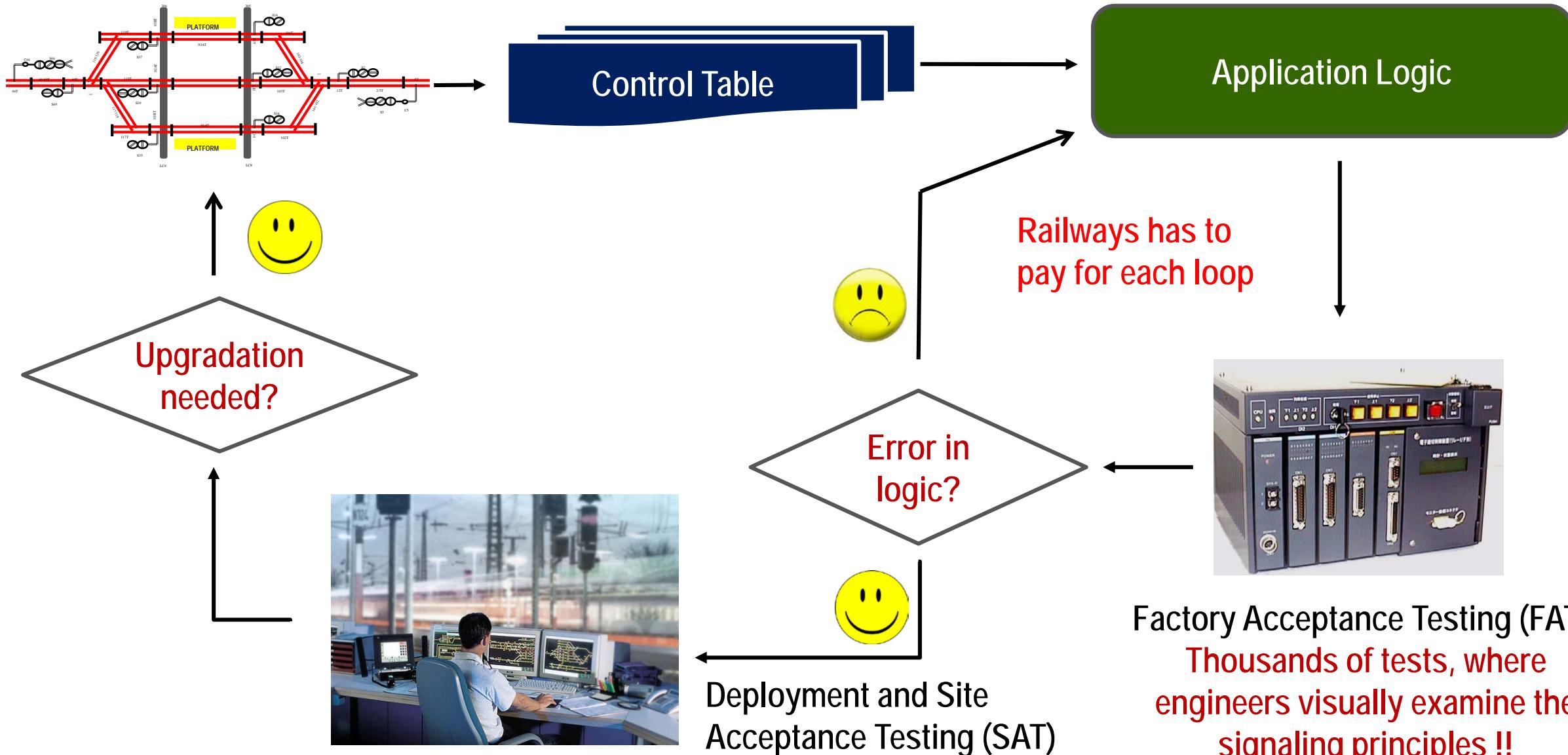
SH35GNR = SH35GN_P & !S2GNR & IS5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !S37GNR & ISH37GNR & !S39GNR & !SH39GNR & !SH44GNR & !S46GNR & !S49GNR & !GSBR & !GSRRB & !FWNR;

S37GNR = S37GN_P & !S2GNR & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !SH44GNR & !S46GNR & !SH46GNR & !S49GNR & !SH49GNR & !GSBR & !GSRR & !EWNR;

SH37GNR = SH37GN_P & !S2GNR & IS5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !SH44GNR & !S46GNR & !SH46GNR & !S49GNR & !SH49GNR & !GSBR & !GSRR & !EWNR;

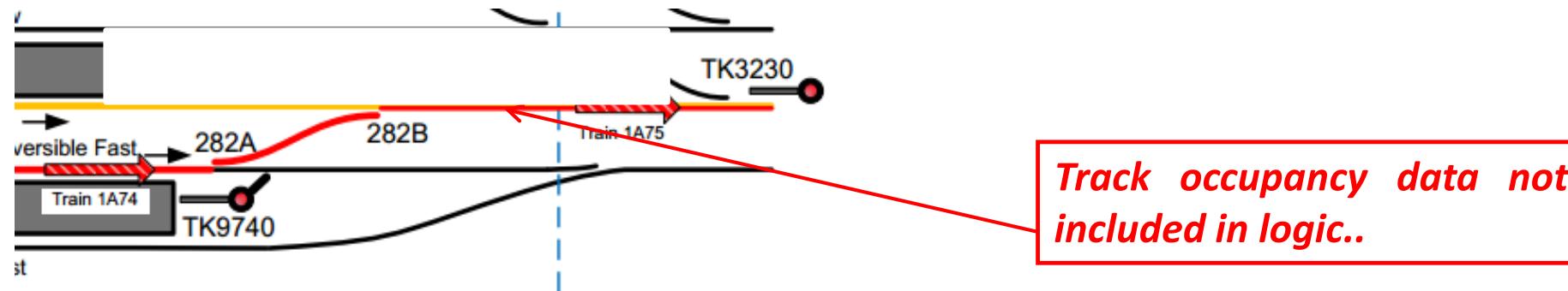
S39GNR = S39GN_P & !S2GNR & !S5GNR & !SH7GNR & !S12GNR & !SH12GNR & !S14GNR & !SH14GNR & !S35GNR & !SH35GNR & !S37GNR & !SH37GNR & !S39GNR & !SH39GNR & !S44GNR & !S46GNR & !S49GNR & !GSBR & !GSBRR & !EWNP;

Life-cycle for Signaling Logic



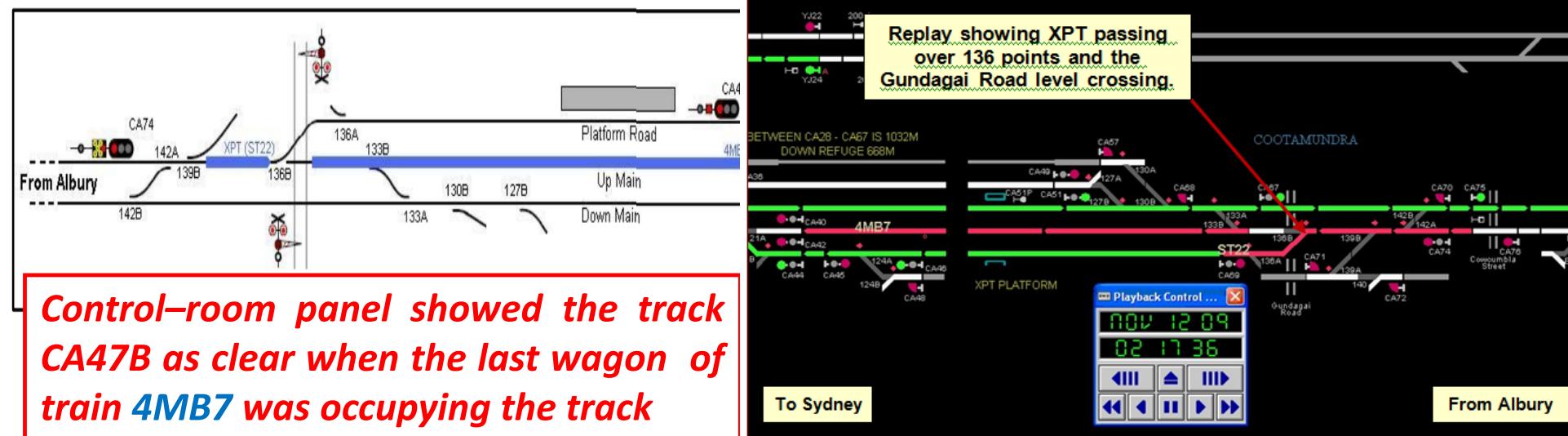
Milton Keynes, UK, 2008 - Cause

Formal investigations revealed, the axle-counter data was not included in the SSI logic associated with the aspect controls for signals TK9740 and TK3230



Cootamundra, NSW Australia, 2009 - The incident

Figure 3: Signal schematic (part) - Cootamundra Yard.



Railway Safety Standards recommend *Formal Methods*

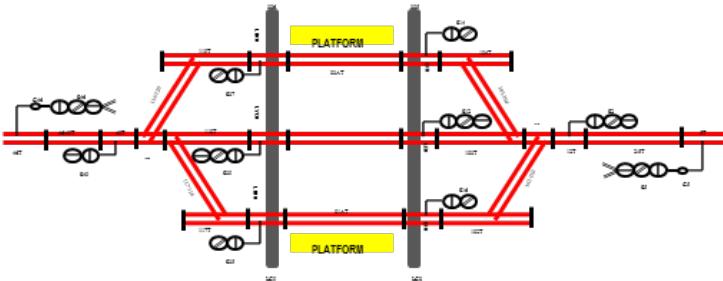
Table A.4 — Software design and implementation (clause 10)

TECHNIQUE/MEASURE	Ref.	SWSIL 0	SWSIL 1	SWSIL 2	SWSIL 3	SWSIL 4
1. Formal methods including for example CCS, CSP, HOL, LOTOS, OBJ, Temporal Logic, VDM, Z and B	B.30	—	R	R	HR	HR
2. Semi-formal methods	D.7	R	HR	HR	HR	HR

Source: Page 50, EN50128: 2001

There are no guidelines in EN50128 on how such methods may be used in the context of Application Logic

IIT Kharagpur Contributions



Layout Editor Tool

- Yard layout is created using this tool
- The tool can perform several sanity checks
- Updates can be made as and when required

SL.NO	ENTRY SIGNAL	EXIT SIGNAL	ROUTE	ROUTE		OVERLAP			OVERLAP SET	CONTROLLED BY TRACK CIRCUIT	SIGNAL REPLACED BY TRACK CIRCUIT	BACK LOCKED UNTIL TRACK CIRCUIT CLEAR	LEVEL CROSSING	CRANK HANDLES	CONFLICTING ROUTES
				POINT NORMAL	POINT REVERSE	TRACKS	POINT NORMAL	POINT REVERSE							
1	S1	S5	1A	51	---	5T, 07T	52	---	OV-5	1T, 2T, 02T, 4T, 04T, 05T1, 05T2, 05T3, 05T	1T	1T, 2T, 02T, 4T	LC 1	CH1, CH2	C-1A, 4, 8A, 78A
2	S1	S3	1BD	51	3T	52	---	---	OV1-3	1T, 2T, 02T, 4T, 6T, 06T, 06T1, 06T2, 06T3, 03T	1T	1T, 2T, 02T, 4T, 6T	LC 1	CH1, CH2	C-1B, 6, 78A
			1BM		3T, 5T, 07T	---	52	---	OV2-3				LC 1		
3	S3	S7	3	---	52	---	---	---	---	3T, 5T, 07T	3T	3T, 5T	---	CH2	8B, 78B, 6, C-1B
4	S5	S7	5	52	---	---	---	---	---	5T, 07T	5T	5T	---	CH2	8A, 78A, 4, C-1A

Control Table Generator Tool

- Control table is automatically generated from the layout created by layout editor
- The tool checks for inherent inconsistencies
- Push-button solution whenever the layout is upgraded

IIT Kharagpur Contributions

Example: Proving that the track circuits in the route up to the next signal and its overlap are clear. SafeR generates the following formal property.

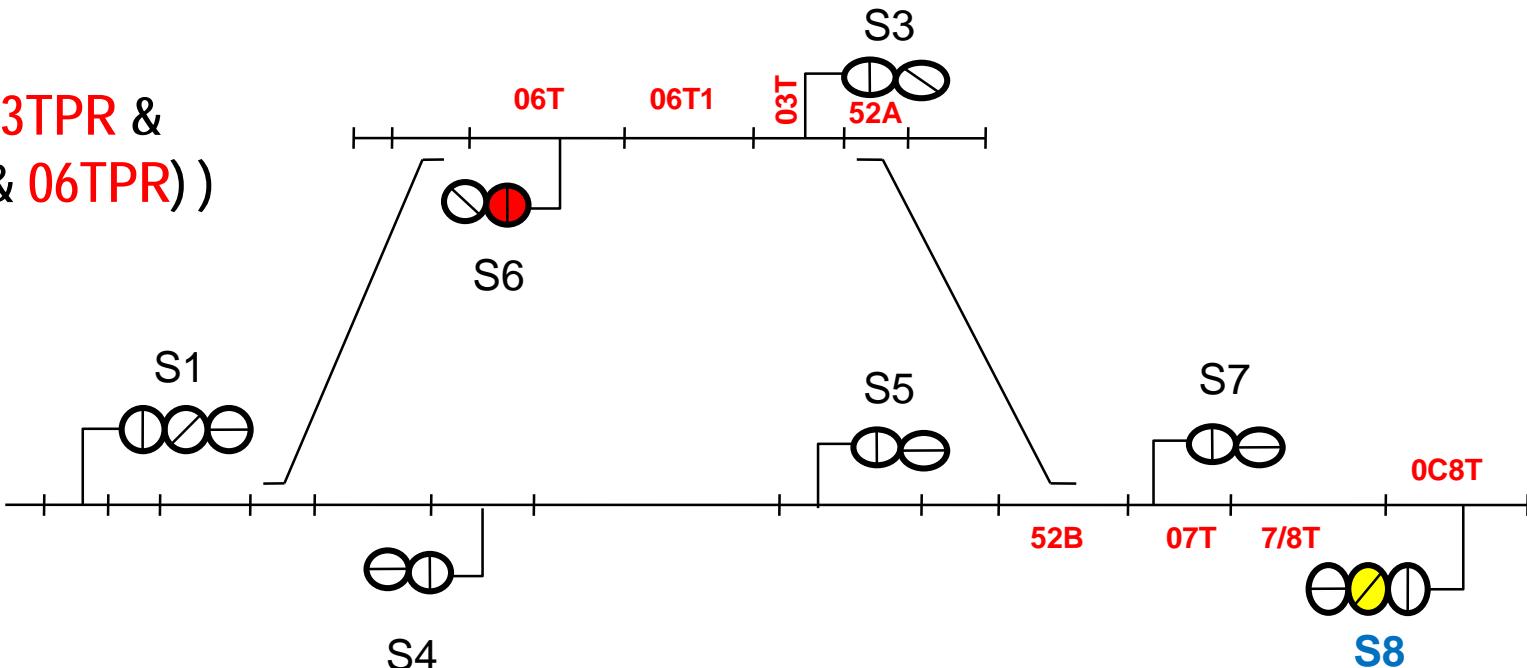
LTLSPEC G(X 8HR →

(0C8TPR & 7/8TPR & 07TPR &
52BTPR & 52ATPR & 03TPR &
06_1TPR & 06TPR))

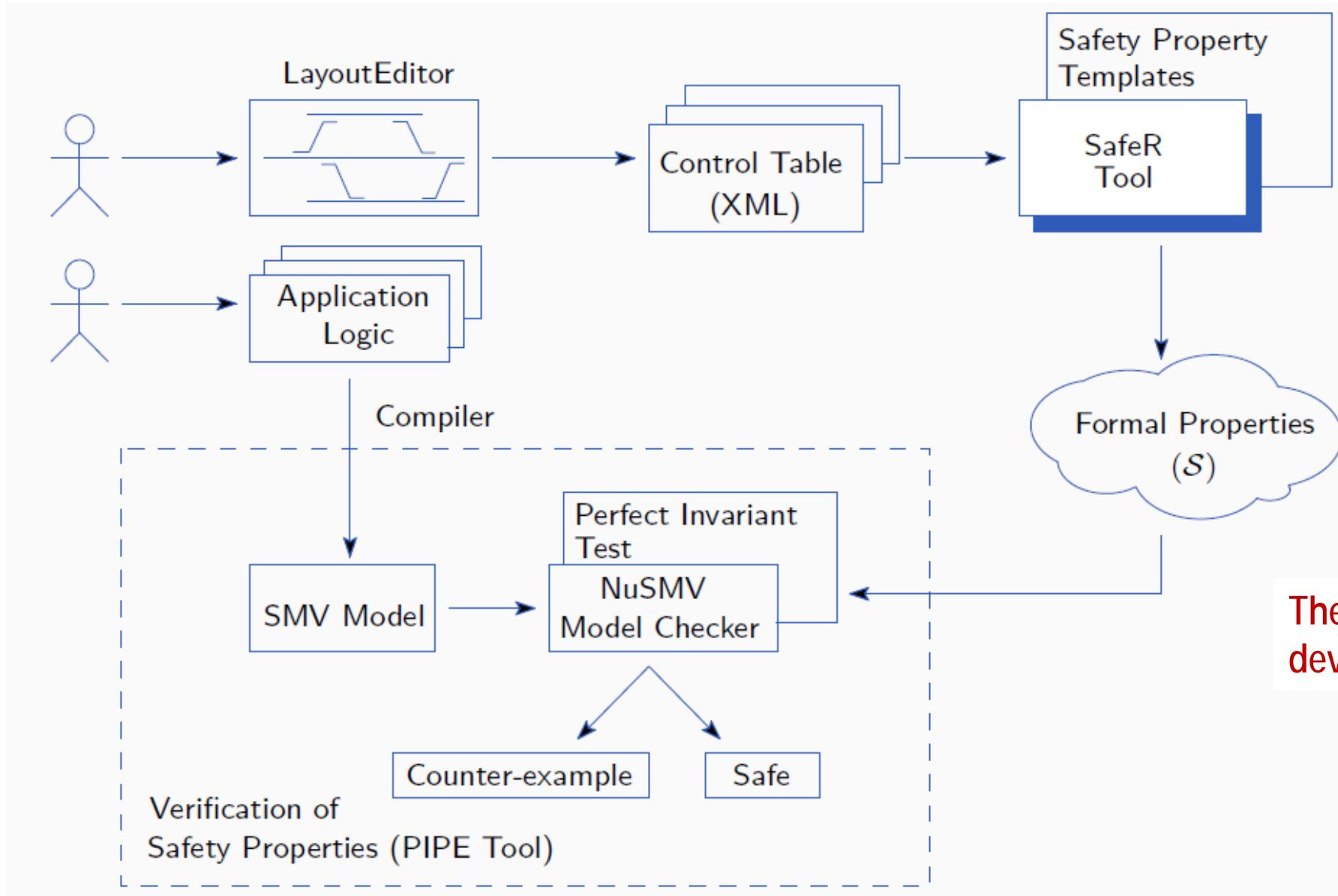
8HR is the “YELLOW” signal relay
TPR are track status relays

The SafeR Tool

- Reads the control table
- Creates a comprehensive set of *formal properties*
- Built in knowledge about international railway signaling principles
- Thousands of properties are automatically verified using back-end formal tools



IIT-KGP EI Verification Tool Flow



Theory of perfect invariants
developed for scaling verification