

CS 130 : Computer Systems - V

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Recap

$$\begin{array}{r} 5 \quad 101 \\ 2 \quad +010 \\ \hline 7 \quad 111 \end{array}$$

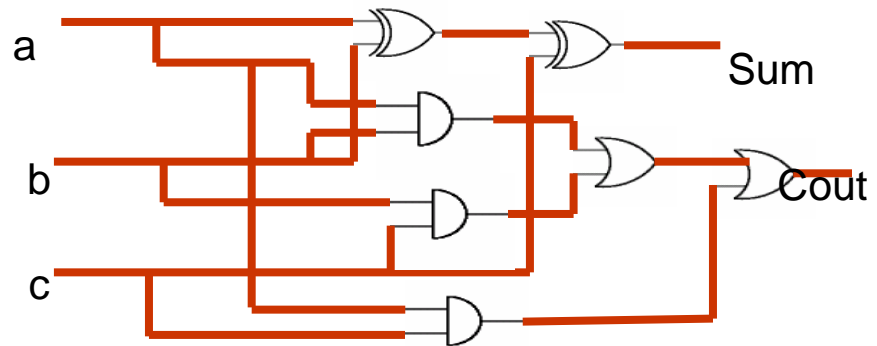
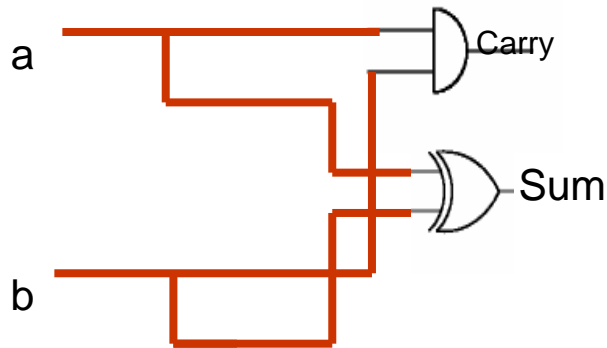
$$\begin{array}{r} 1 \quad 001 \\ 1 \quad +001 \\ \hline 2 \quad 010 \end{array}$$

$$\begin{array}{r} 3 \quad 011 \\ 1 \quad +001 \\ \hline 4 \quad 100 \end{array}$$

Carry

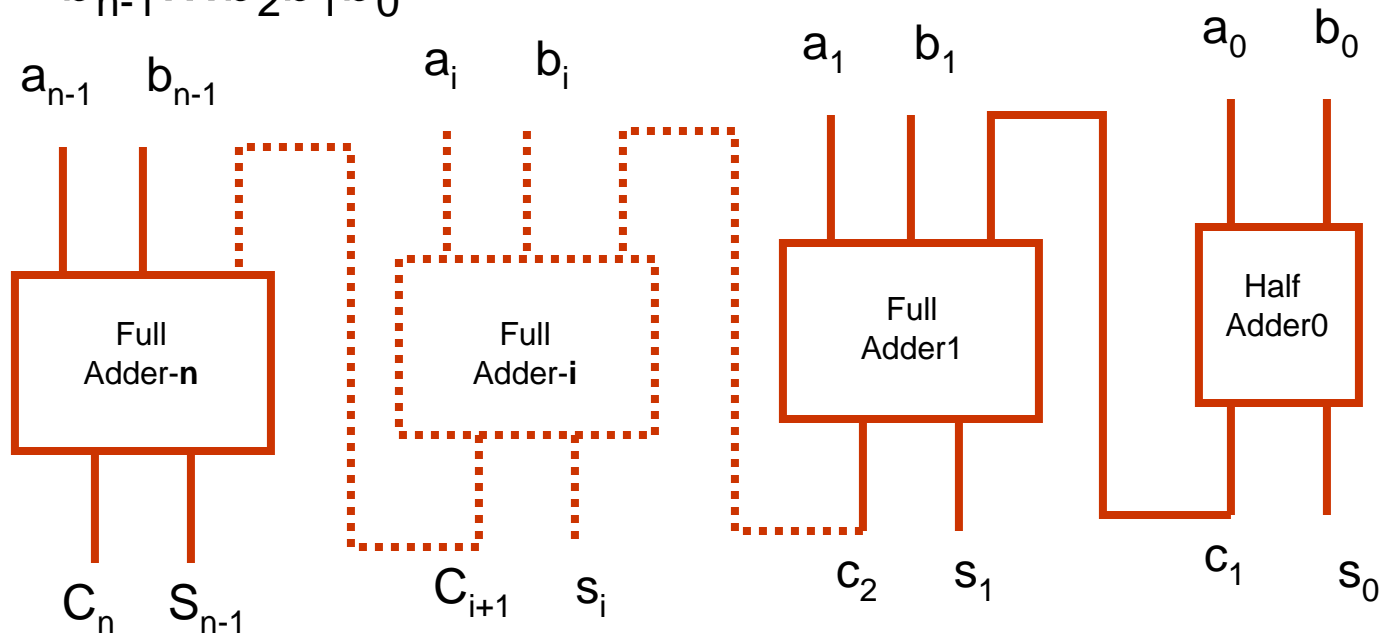
Sum

- Carry := A AND B
- Sum := A XOR B



Multi-Bit Adder - Recap

- Let $A = a_{n-1} \dots a_2 a_1 a_0$
- Let $B = b_{n-1} \dots b_2 b_1 b_0$



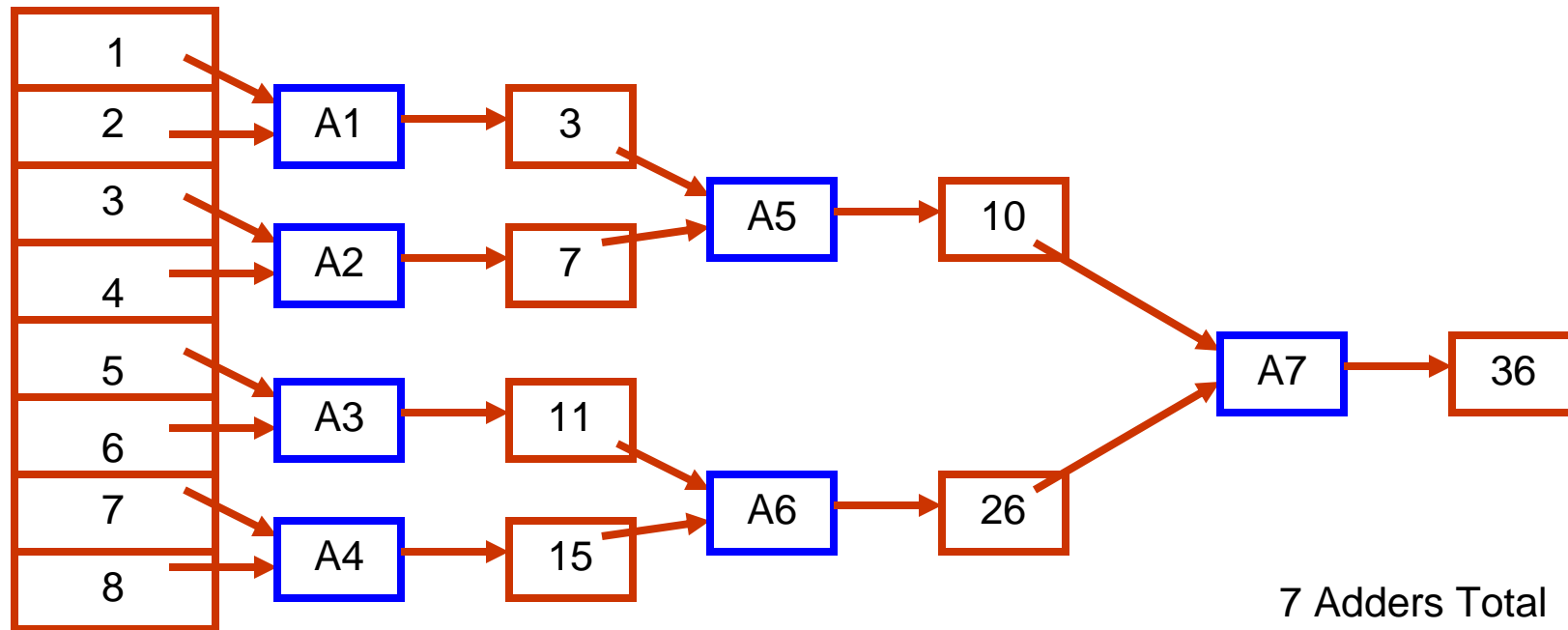


About N-Bit Adder

- Multiple adder units cascade
- Each unit increments data size by 1 bit
- Scalable
 - Can be done for any n .
- Simple easy procedure to repeat. Very regular in structure
 - Can be automated easily
 - Can be verified easily

Let's Add m Numbers

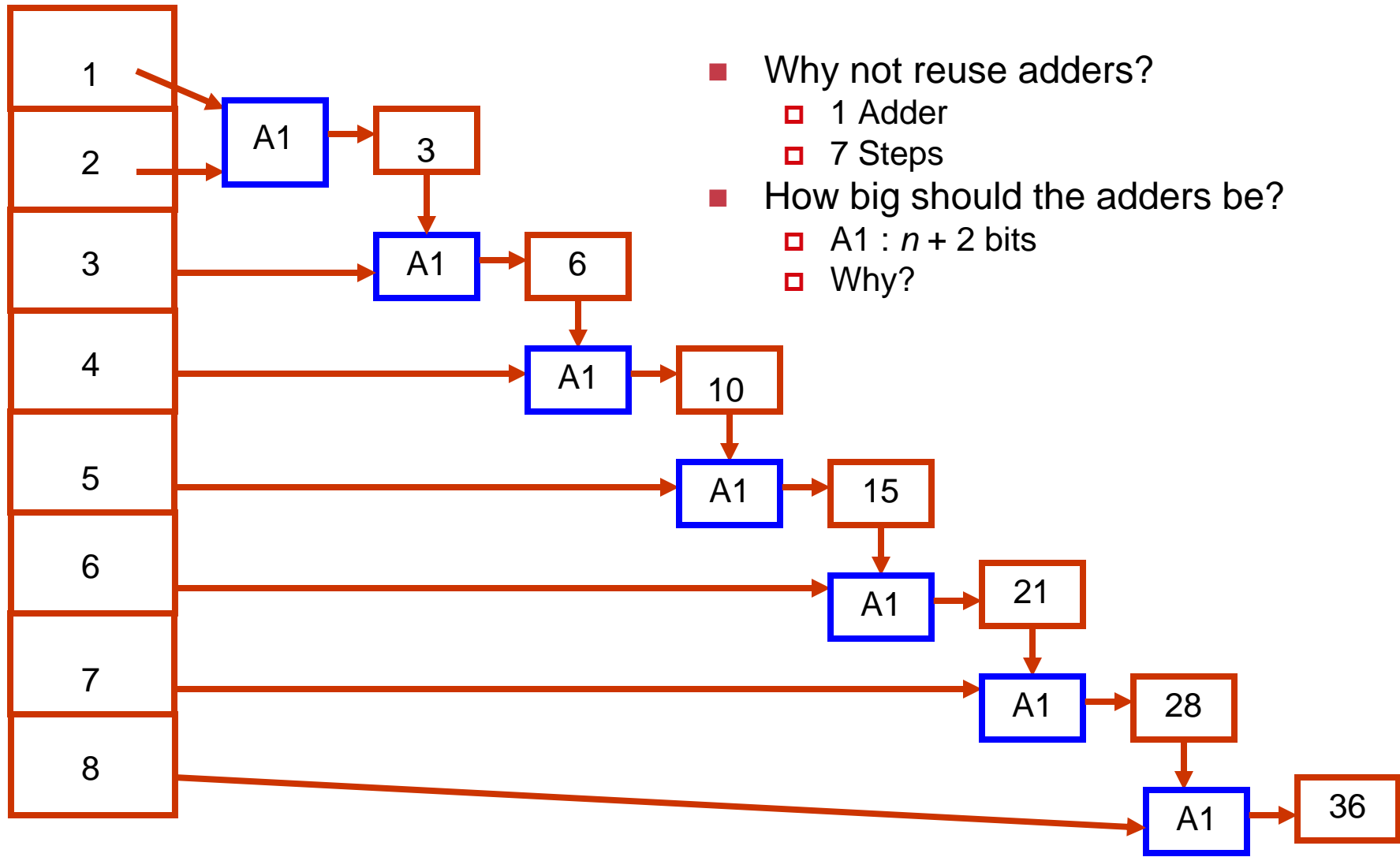
- Numbers are n -bits each



Analysis

- How big should the adders be?
 - A1 : n bits
 - A2 : n bits
 - A3 and A4 : n bits
 - A5 and A6 : $n + 1$ bits;
 - In general, we don't know whether operands are big or not
 - A7 : $n + 2$ bits
 - How many full adders and half-adders?
- How many steps are needed to finish the operation?
 - A1, A2, A3 and A4 need not wait for any one
 - A5 and A6 should wait for (A1,A2) and (A3,A4) respectively
 - A7 must wait for A5 and A6
 - Three steps
- Summary : Three Steps, Seven Adders

Can we cut down on adders?



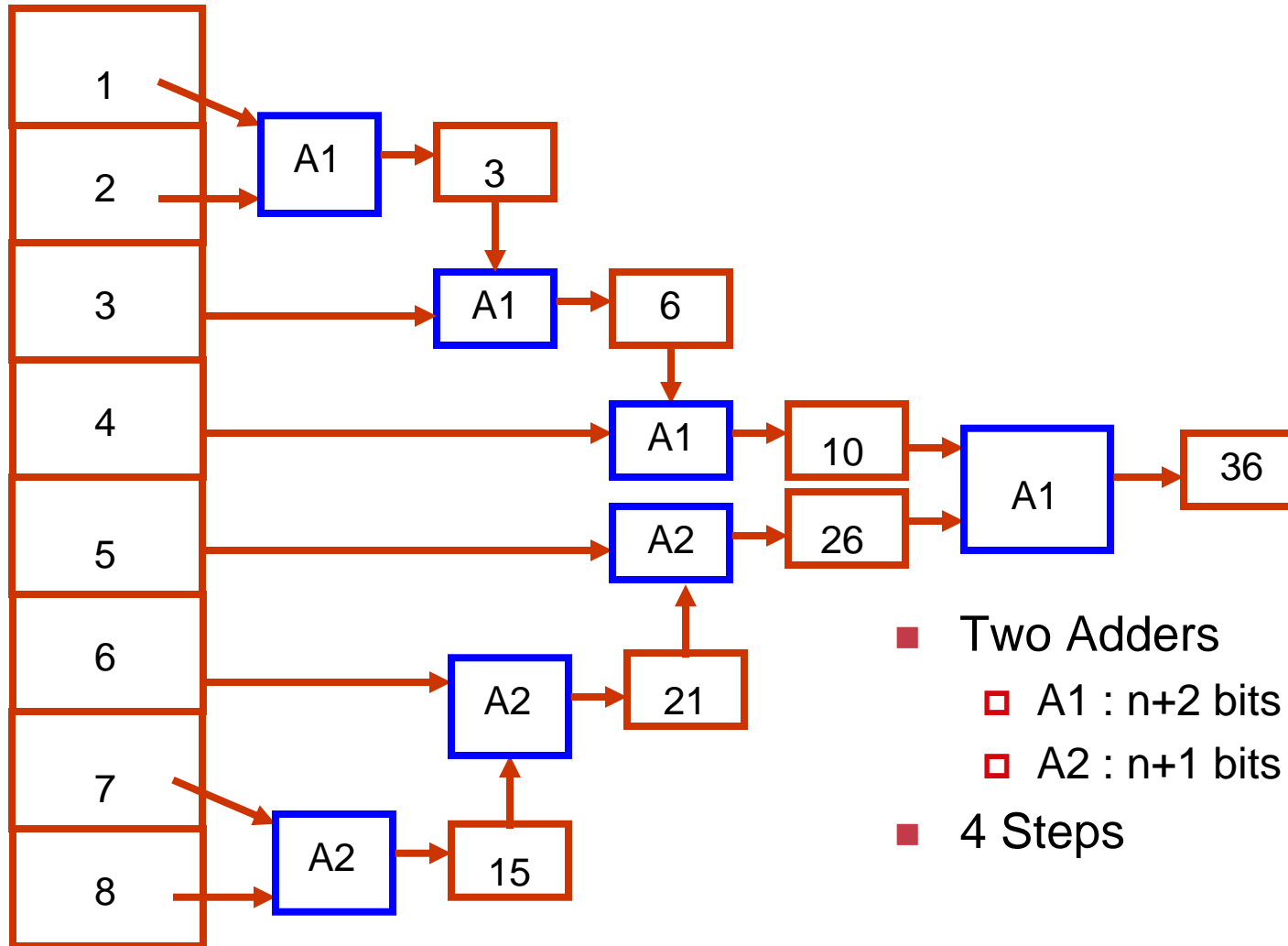
- Why not reuse adders?
 - 1 Adder
 - 7 Steps
- How big should the adders be?
 - $A1 : n + 2$ bits
 - Why?



Sequential and Parallel

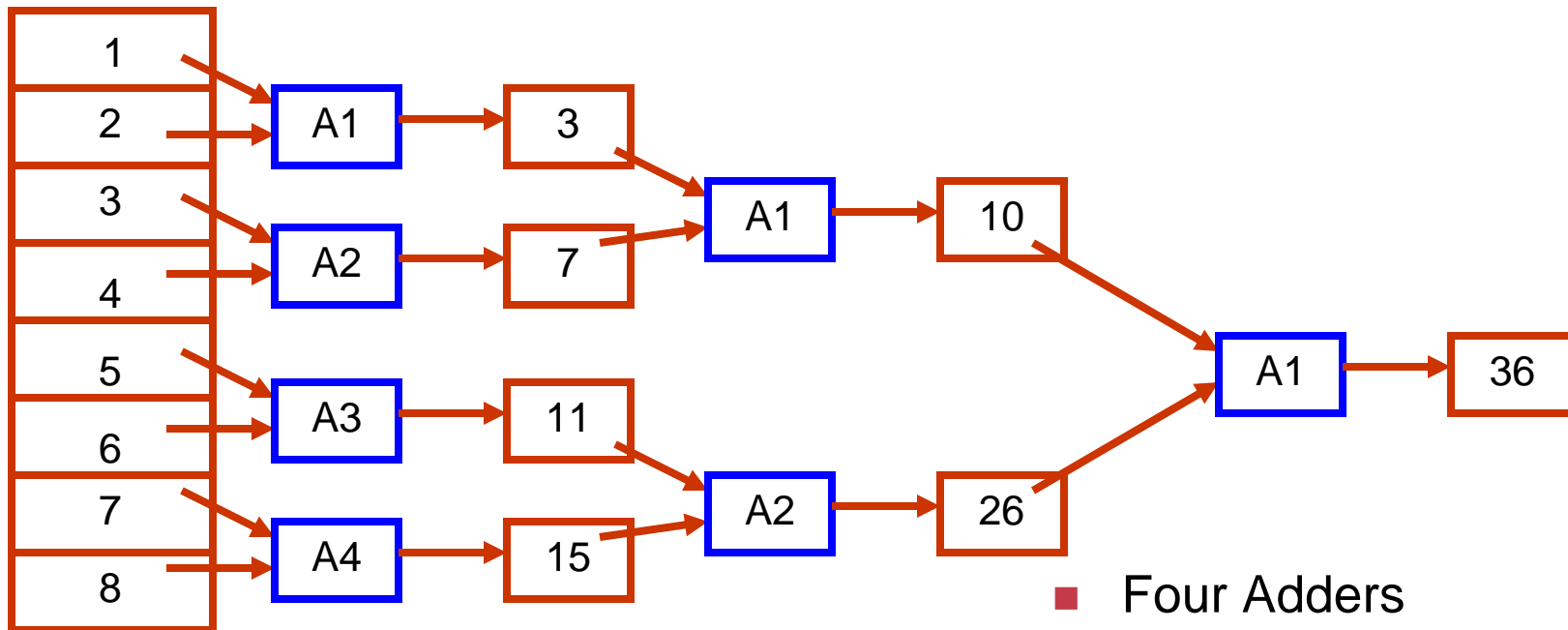
- Sequential
 - One operation at a time
 - Less resources
 - More steps
- Parallel
 - Many operations at the same time
 - More resources
 - Less steps
- Are there sweet spots in between?
 - Yes!
 - Partly sequential, partly parallel

Example (1)



- Two Adders
 - A1 : $n+2$ bits
 - A2 : $n+1$ bits
- 4 Steps

Example (2)



- Four Adders
 - A1 : $n+2$ bits
 - A2 : $n+1$ bits
 - A3 and A4 : n bits
- 3 Steps



Trade-offs

- Life is all about trade-offs 😊
- Adders occupy area
 - Assume unit area
 - Every adder used takes 1 unit of area
- Adders have delays
 - Assume unit delay
 - Every step takes 1 unit of delay
- What we did here is called the area-delay tradeoff analysis

Which Adder Scheme is Better?

- Define better ☺
- In terms of area
 - Sequential
 - But slow
- In terms of delay
 - Parallel
 - But a lot of resources
- What about area delay product?
 - Combines area and delay
 - Sequential : 7
 - Parallel : 21
 - Combination(1) : 8
 - Combination (2) : 12
 - Is Sequential better?
 - When does it stop to be better?



Comparison Metrics

Plane	DC to Paris	Speed	Passengers	Passengers/ Hr
Boeing 747	6.5 hours	610 mph	470	72.3
Concorde	3 hours	1350 mph	132	44

- Which is faster?
 - Concorde
- But is it better?
 - For speed : yes
 - Passengers carried per hour : No



Be Warned

- Comparison metrics should be chosen carefully
- Sometimes there is no agreement among engineers
- As an amateur engineer, how do you decide?
- Ask questions :
 - What is the design goal?
 - What are the design constraints?
 - What are the costs involved?
 - Are there established practices?