







Models for Cryptanalysis

• Chosen Ciphertext:

- The opponent has temporary access to the decryption function.
- He can choose ciphertexts and decrypt to obtain the corresponding plaintexts.
- In each case, the objective is to obtain the key.
- Increasing order of strength:
 - Ciphertext only < Known plaintext < Chosen
 Plaintext < Chosen Ciphertext















Index of coincidence (cont.)

An Important Property:

Suppose *x* is a string of English text, denote the expected probability of occurrences of A,B,...,Z by p_0,p_1,\ldots,p_{25} with values from the frequency graph, then:

• probability that two random elements both are A is p_0^2 , both are B is $p_1^2,...$

•then $I_c(x) \approx \sum p_i^2 = 0.082^2 + 0.015^2 + \dots + 0.001^2 = 0.065$

Question: if y is a ciphertext obtained by shift cipher, what is the $I_c(y)$?

Answer: should be 0.065, because the individual probabilities will be permuted, but the $\sum p_i^2$ will be unchanged. So, this is an Invariant. This Property is used to determine the key.



Index of coincidence (cont.)

For purpose of verify keyword length m, divide the ciphertext into m substrings, compute the index of coincidence by for each substring. If all IC values of the substrings are around 0.065, then m is the correct keyword length. Otherwise m is not the correct keyword length.

If want to use I_c to determine correct keyword length *m*, what to do?

Beginning from m=2,3,... until an *m*, for which all substrings have IC value around 0.065.

Now, how to determine keyword $K = (k_1, k_2, ..., k_m)$? Assume *m* is given.















Example

 CHREEVOAHMAERATBIAXXWTNXBEEOPHB SBQMQEQERBWRVXUOAKXAOSXXWEAHB WGJMMQMNKGRFVGXWTRZXWIAKLXFPSK AUTEMNDCMGTSXMXBTUIADNGMGPSRELX NJELXVRVPRTULHDNQWTWDTYGBPHXTFA LJHASVBFXNGLLCHRZBWELEKMSJIKNBHW RJGNMGJSGLXFEYPHAGNRBIEQJTAMRVLC RREMNDGLXRRIMGNSNRWCHRQHAEYEVTA QEBBIPEEWEVKAKOEWADREMXMTBHHCH RTKDNVRZCHRCLQOHPWQAIIWXNRMGWOII FKEE









Kasiski Test				
• A:7	M:2	U:1		
• B:6	N:1	V:2		
• C:1	O:4	W:4		
• E:8	P:1	X:7		
• G:1	Q:3	I _C (x)=0.065		
• H:4	R:4	This will be for all the other four rows.		
• I:1	S:2	If the m is anything other than 5, the L (w) (index of an incidence) is		
• K:1	T:2	the I _c (x) (index of co-incidence) is around 0.04		
		This confirms the value of m.		



The decrypted Text

 The almond tree was in tentative blossom. The days were longer often ending with magnificent evenings of corrugated pink skies. The hunting session was over with hounds and guns put away for six months. The vineyards were busy again as the well organized farmers treated their vines and more lackadaisical neighbors hurried to do the pruning they should have done in November.



Kasiski Test

String	First Index	Second Index	Difference
QLT	65	165	100
LTJ	66	166	100
TJS	67	167	100
JSU	68	168	100
SUM	69	117	48
VWV	72	132	60

Kasiski Test thus predicts key size is the gcd, which is 4.















References

 B. A. Forouzan and
 D. Mukhopadhyay, "Cryptography and Network Security", TMH, 2nd Edition.

