

Stream Ciphers

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Objectives

- **Classifications**
- **Feedback Based Stream Ciphers**
 - **Linear Feedback Shift Registers**
 - **m sequences**

Block vs Stream Ciphers

- Differences are not definitive.
- **Blocks Ciphers process plaintext in large blocks.**
- **Stream Ciphers process plaintext in small blocks, even bits**
- **Pure Block ciphers are memory-less.**
- **Stream cipher encryption depends not only on the plaintext, key but also on the current state,**

One Time Pad

- **A Vernam cipher over the binary alphabet is defined by:**

$$c_i = m_i \oplus k_i, \text{ for } i = 1, 2, 3, \dots$$

- **Unconditionally secured, $H(K) \geq H(M)$**

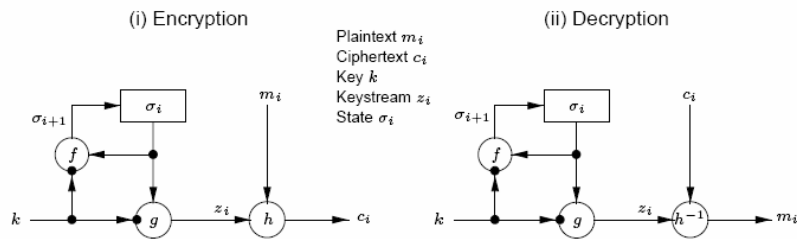
One Time Pad

- **Drawback: key as long as the plaintext.**
- **This motivates the design of stream ciphers where the key stream is generated from a small key.**
- **The intent is protection against computationally bounded adversary.**

Synchronous Stream Ciphers

- **Keystream is generated independently of the plaintext message and of the ciphertext.**
- **Encryption process:**
 - Updating a state variable using $\sigma_{i+1} = f(\sigma_i, k)$
 - Generating a key stream, $z_i = g(\sigma_i, k)$
 - Producing the ciphertext stream, $C_i = h(z_i, m_i)$
- **E.g.: Binary Additive Stream Cipher:**
 - streams are binary and h is \oplus

General Model of a synchronous stream cipher



Properties of Synchronous Stream Ciphers

1. Synchronization Requirements:

1. Sender and Receiver must be synchronized – using the same key and operating at the same state within that key
2. Insertion/Deletion may cause loss of synchronization
3. Re-synchronization may need re-initialization and/or special marks in the stream at regular intervals.

2. No Error Propagation:

1. Modified digit does not affect decryption of other digits

3. Active Attacks:

1. Insertion/Deletion/Replay cause loss of synchronization, thus is detected by the decryptor.
2. Due to lack of error propagation, the adversary can determine ciphertext and plaintext pairs.

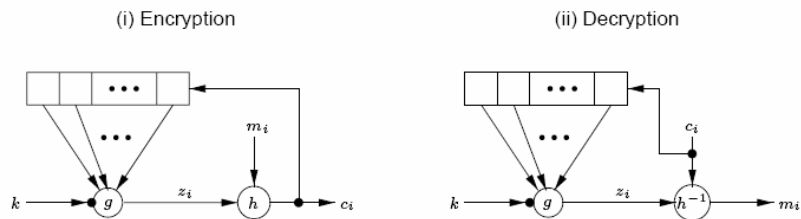
Self Synchronization Stream Ciphers

- **A self-synchronizing or asynchronous stream cipher is one in which the key stream is generated as a function of:**
 - the key
 - a fixed number of previous ciphertext digits.

Self Synchronization Stream Ciphers

- $\sigma_i = (C_{i-t}, C_{i-t+1}, \dots, C_{i-1})$
- $z_i = g(\sigma_i, k) \quad C_i = h(z_i, m_i)$
- where $\sigma_0 = (C_{-t}, C_{-t+1}, \dots, C_{-1})$ is the initial state
- and z_i is the keystream
- and c_i is the cipher-stream

General Model of a self-synchronization stream cipher



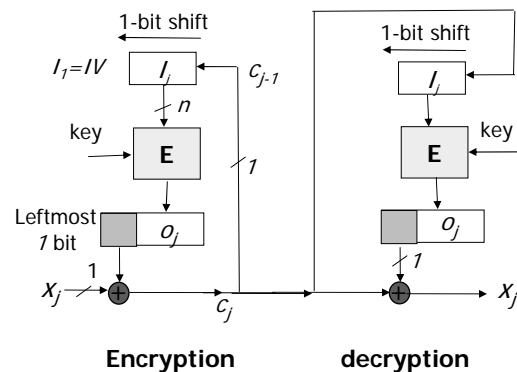
Properties

- **Self-synchronization:**
 - possible with insertions/deletions (at most t digits may be lost)
- **Limited Error Propagation:**
 - 1 digit modification/insertion/deletion may cause incorrect decryption of up to t digits.
- **Active Attacks**
 - Modification can be detected due to incorrect decryption – better than synchronous stream ciphers.
 - It is more difficult than for synch. stream ciphers to detect insertion / deletion / replay of ciphertext digits.
- **Diffusion of plaintext statistics: Better**

Need for Modes of Block Ciphers

- **Block Ciphers deal with blocks of data**
- **In real life there are two important issues:**
 - plaintext much larger than a typical block length of 128 bits
 - plaintext not a multiple of the block length
- **The obvious solution is the first mode, called the Electronic Code Book (ECB)**
- **These modes were first standardized in FIPS Publication 81 in 1980.**

Example: 1 bit CFB



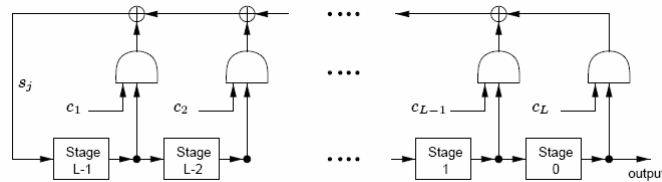
Feedback Shift Registers

- **They are the basic blocks of many keystream generators.**
 - **Linear Feedback Shift Registers (LFSRs)**
 - **well suited for hardware implementations**
 - **can produce sequences of large period**
 - **good statistical properties**
 - **can be analyzed by algebraic techniques**

Linear Feedback Shift Registers

- **An LFSR of length L consists of**
 - **L stages (or delay elements) capable of storing 1 bit each and**
 - **a clock controlling the movement of data.**
- **During each unit of time:**
 - **Content of stage 0 is output**
 - **Content of stage j is moved to stage j-1 for each j (1 to L-1)**
 - **New content of stage L-1 is the feedback bit computed as sum without carry of previous contents of a fixed subset of stages.**

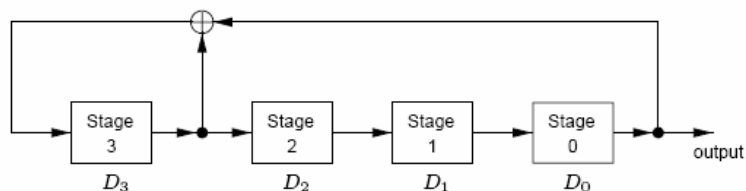
An LFSR of length L



- Denoted as $\langle L, C(D) \rangle$
 - $C(D) = 1 + c_1 D + \dots + c_L D^L$ is called the connection polynomial.
 - L is the length of the LFSR

Example

- Consider the LFSR $\langle 4, 1 + D + D^4 \rangle$



Sequence of the LFSR

| t | D₃ | D₂ | D₁ | D₀ |
|----------|----------------------|----------------------|----------------------|----------------------|
| 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 | 1 |
| 2 | 1 | 0 | 0 | 1 |
| 3 | 0 | 1 | 0 | 0 |
| 4 | 0 | 0 | 1 | 0 |
| 5 | 0 | 0 | 0 | 1 |
| 6 | 1 | 0 | 0 | 0 |
| 7 | 1 | 1 | 0 | 0 |

Sequence of the LFSR

| t | D₃ | D₂ | D₁ | D₀ |
|-----------|----------------------|----------------------|----------------------|----------------------|
| 8 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 |
| 10 | 0 | 1 | 1 | 1 |
| 11 | 1 | 0 | 1 | 1 |
| 12 | 0 | 1 | 0 | 1 |
| 13 | 1 | 0 | 1 | 0 |
| 14 | 1 | 1 | 0 | 1 |
| 15 | 0 | 1 | 1 | 0 |

Periodicity of the LFSR sequences

- **If $C(D)$ is a connection polynomial of degree L**
 - **and is irreducible over Z_2 , then each of the 2^L-1 non-zero initial states of the LFSR produces an output sequence with period equal to the least positive integer N , such that $C(D)$ divides $1+D^N$**

Periodicity of the LFSR sequences

- **For some polynomials all the cycle lengths are equal to 2^L-1 .**
- **These polynomials are called primitive polynomials.**
- **The sequence is then called m-sequence.**
- **It has good statistical properties.**
- **Example: $1+D+D^4$ was also primitive and thus we obtained a maximum length LFSR.**

Reconstructing the LFSR?

- **Given a sequence can we reconstruct the LFSR which generates the sequence.**

Generating the sequence

- **An LFSR is said to generate a sequence s if there is some initial state for which the output sequence of an LFSR is s .**
- **A sequence of finite length n is denoted by s^n .**

Linear Complexity

Linear Complexity of an infinite binary sequence s , denoted $L(s)$ is defined as:

- 1. If s is the 0 sequence, $L(s)=0$**
- 2. If no LFSR generates s , $L(s)=\infty$**
- 3. otherwise, $L(s)$ is the length of the shortest LFSR that generates s .**

Linear Complexity for a finite sequence

- Linear Complexity for a finite sequence s^n , is the shortest LFSR that generates a sequence having s^n as its first n terms.**

Example

- **Reconstruct an LFSR (of the shortest length) which generates the sequence 00111011.**

Points to Ponder!

- **Can you modify the LFSR with connection polynomial primitive to include the all 0 state?**

Further Reading

- **D. Stinson, Cryptography: Theory and Practice, Chapman & Hall/CRC**
- **A. Menezes, P. Van Oorschot, Scott Vanstone, “Handbook of Applied Cryptography” (Available online)**

Next Days Topic

- **Stream Ciphers (contd.)**