

## Table Driven Predictive Parser

A non-recursive predictive parser can be constructed that maintains a stack (explicitly) and a table to select the appropriate production rule.

### Parsing Table

The **rows** of the predictive parser table are indexed by the **non-terminals** and the **columns** are indexed by the **terminals** including the **end-of-input marker (\$)**. The content of the table are production rules or error situations. The table cannot have multiple entries.

## Parsing Stack

The parsing stack can hold both **terminals** and **non-terminals**. At the beginning, the stack contains the **end-of-stack marker** (\$) and the **start symbol** on top of it.

## Parsing Table Construction

- If  $A \rightarrow \alpha$  is a production rule and  $a \in \text{FIRST}(\alpha)$ , then  $P[A][a] = A \rightarrow \alpha$ .
- If  $A \rightarrow \varepsilon$  is a production rule and  $a \in \text{FOLLOW}(A)$ , then  $P[A][a] = A \rightarrow \varepsilon$ .

## Actions

- If the **top-of-stack** is a terminal symbol (token) and matches with input token, both are **consumed**. A mismatch is an error.
- If the **top-of-stack** is a non-terminal  $A$ , the input token is  $a$ ,  $P[A][a]$  has the entry  $A \rightarrow \alpha$ , then  $A$  is to be replaced by  $\alpha$ , with the head of  $\alpha$  on the top of the stack.

## Example

Consider the production rules of the non-terminal **SL**.

$$\text{SL} \rightarrow \text{S SL} \mid \varepsilon$$

The  $\text{FIRST}(\text{SL} \rightarrow \text{S SL}) = \{\text{id if while scan print}\}$  and  $\text{FOLLOW}(\text{SL}) = \{\text{end else}\}$ . So,  $P[\text{SL}][\text{IDENTIFIER}] = P[\text{SL}][\text{IF}] = P[\text{SL}][\text{WHILE}] = P[\text{SL}][\text{SCAN}] = P[\text{SL}][\text{PRINT}] = \text{SL} \rightarrow \text{S SL}$  and  $P[\text{SL}][\text{END}] = P[\text{SL}][\text{ELSE}] = \text{SL} \rightarrow \varepsilon$ .

### Note

Multiple entries in a table indicates that the grammar is not  $LL(1)$ . But it is interesting to note that in some cases we can drop (with proper consideration) some of these entries and construct a parser.

### Example

Consider the ambiguous grammar  $G_1$  for expressions.

$$E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid (E) \mid ic$$

After the removal of **left-recursion** we get the following ambiguous, no-left-recursive grammar:

### Example

$$E \rightarrow (E)E' \mid icE'$$

$$E' \rightarrow +EE' \mid -EE' \mid *EE' \mid /EE' \mid \varepsilon$$

We calculate  $\text{FIRST}(E') = \{+ \ - \ * \ / \ \varepsilon\}$  and the  $\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{\$ \ ) \ + \ - \ * \ /\}$ .

### Example

Naturally,

$$P[E'][\pm] = \{E' \rightarrow +EE', E' \rightarrow \varepsilon\} \text{ and}$$

$$P[E'][*/] = \{E' \rightarrow *EE', E' \rightarrow \varepsilon\}.$$

We may drop the  $\varepsilon$ -productions from these four places and get a nice parsing table<sup>a</sup>.

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<sup>a</sup>But it does not work for all grammars. Consider  $S \rightarrow aSa \mid bSb \mid \varepsilon$ .

### Note

It seems that the removal of two  $\varepsilon$ -production disambiguates the grammar. The corresponding unambiguous grammar  $G_2$  is as follows:

$$E \rightarrow (E)E' \mid icE' \mid (E) \mid ic$$

$$E' \rightarrow +E \mid -E \mid *E \mid /E \mid \varepsilon$$

We have  $L(G_1) = L(G_2)$  and  $\text{FOLLOW}(E') = \{\$, \})\}$ , so there is no multiple entries in the table<sup>a</sup>.

### Error Recovery

- The token on the top of stack does not match with the token in the input stream.
- The entry in the parsing table corresponding to nonterminal on the top of stack and the current input token is an error.