



INDIAN INSTITUTE OF TECHNOLOGY  
KHARAGPUR

Stamp / Signature of the Invigilator

EXAMINATION ( End Semester )

SEMESTER ( Spring 2023-2024 )

Roll Number

Section

Name

Subject Number

C S 1 0 0 0 3

Subject Name

PROGRAMMING AND DATA STRUCTURES

Department / Center of the Student

Additional sheets

**Important Instructions and Guidelines for Students**

1. You must occupy your seat as per the Examination Schedule/Sitting Plan.
2. Do not keep mobile phones or any similar electronic gadgets with you even in the switched off mode.
3. Loose papers, class notes, books or any such materials must not be in your possession, even if they are irrelevant to the subject you are taking examination.
4. Data book, codes, graph papers, relevant standard tables/charts or any other materials are allowed only when instructed by the paper-setter.
5. Use of instrument box, pencil box and non-programmable calculator is allowed during the examination. However, exchange of these items or any other papers (including question papers) is not permitted.
6. Write on both sides of the answer script and do not tear off any page. **Use last page(s) of the answer script for rough work.** Report to the invigilator if the answer script has torn or distorted page(s).
7. It is your responsibility to ensure that you have signed the Attendance Sheet. Keep your Admit Card/Identity Card on the desk for checking by the invigilator.
8. You may leave the examination hall for wash room or for drinking water for a very short period. Record your absence from the Examination Hall in the register provided. Smoking and the consumption of any kind of beverages are strictly prohibited inside the Examination Hall.
9. Do not leave the Examination Hall without submitting your answer script to the invigilator. **In any case, you are not allowed to take away the answer script with you.** After the completion of the examination, do not leave the seat until the invigilators collect all the answer scripts.
10. During the examination, either inside or outside the Examination Hall, gathering information from any kind of sources or exchanging information with others or any such attempt will be treated as '**unfair means**'. Do not adopt unfair means and do not indulge in unseemly behavior.

**Violation of any of the above instructions may lead to severe punishment.**

Signature of the Student

*To be filled in by the examiner*

Question Number

1

2

3

4

5

6

7

8

9

10

Total

Marks Obtained

Marks obtained (in words)

Signature of the Examiner

Signature of the Scrutineer

**Instruction to students**

- Write your answers in the question paper itself. Be brief and precise. Answer all questions.
  - Write the answers only in the respective spaces provided.
  - The questions appear on the next *nine* pages.
  - Please ask for supplementary sheets during the test if you need more rough space.
  - All the questions use the programming language C.
  - Not all blanks carry equal marks (unless otherwise stated). In those cases, evaluation will depend on overall correctness.
  - In the questions involving fill in the blanks inside the code snippets, *each blank can be filled with at most one expression or statement as applicable.*
- 

Do not write anything on this page.

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Questions start from the next page.

**Q1.** If the following C programs terminate, then write the output. When no output can be generated, write NONE. In case, the program contains an error, write ERROR with the LINE NUMBER(s). Otherwise, say that the program does not terminate (write NO TERMINATION).

(2×10)

```
#include <stdio.h>
#include <stdlib.h>
#define SIZE 5

// structure definition for queue
typedef struct _queue {
    // array storing queue elements
    int items[SIZE];
    /* index of front and rear
    elements of queue */
    int front, rear;
} Queue;

/* function to append an element
at the end of a queue:
returns nothing */
void enqueue(Queue *q, int value);

/* function to remove an element
from the beginning of queue:
returns the removed element,
or -1 if the queue is empty */
int dequeue ( Queue *q );

int main() {
    Queue q;
    q.front = q.rear = 0;
    enqueue(&q,5); enqueue(&q,10);
    printf ("%d ", dequeue (&q));
    enqueue(&q,15); enqueue(&q,20);
    printf ("%d ", dequeue (&q));
    return 0;
}
```

**Answer:** 5 10

```
#include <stdio.h>
typedef struct Point2D {
    int x;
    int y;
} POINT;
int main () {
    POINT p = {3,4}, *ptr = &p;
    printf("%d %d",ptr->x,(*ptr).y);
    return 0;
}
```

**Answer:** 3 4

```
#include <stdio.h>
#include <stdlib.h>
#define SIZE 3

// structure definition for stack
typedef struct _stack {
    // array storing stack elements
    int items[SIZE];
    // index of top element of stack
    int top;
} Stack;

/* function to push an element
onto a stack:
returns nothing */
void push ( Stack *s, int value );

/* function to pop an element
from the stack:
returns the popped element,
or -1 if the stack is empty */
int pop ( Stack *s );

int main () {
    Stack s;
    s.top = -1;
    push(&s, s.top); push(&s, s.top);
    printf("%d ", pop(&s));
    printf("%d ", pop(&s));
    printf("%d ", pop(&s));
    return 0;
}
```

**Answer:** 0 -1 -1

```
#include <stdio.h>
int main () {
    int *px, *py;
    int a = 10, b = 20;
    px = &a;
    *px = b;
    *py = a;
    printf ("%d %d, ", a, b);
    printf ("%d %d", *px, *py);
    return 0;
}
```

**Answer:** ERROR in Line 7: \*py = a;  
(Segmentation Fault)

```

#include <stdio.h>
void foo ( int *p, int *q,
           int x, int y ) {
    p = &y; *q = 30;
}
int main () {
    int *px, *py;
    int a = 10, b = 20;
    px = &a; py = &b;
    foo (px, py, a, b);
    printf ("%d,%d", *px, *py);
    return 0;
}

```

**Answer:** 10,30

```

#include <stdio.h>
int fun ( char *s ) {
    if ( *s == '\0' ) return 0;
    if ( *s != *(s+1) ) {
        printf ("%c", *s);
        return 1 + fun (s+1);
    }
    return fun (s+1);
}
int main () {
    printf(" %d",fun("Yiipppeeee"));
    return 0;
}

```

**Answer:** Yipe 4

```

#include <stdio.h>
int count = 0;
int pds ( int n ) {
    int m = n - 1;
    ++count;
    while(m>=0) { pds(m); m=m-2; }
    return count;
}
int main () {
    printf("%d", pds(5));
    return 0;
}

```

**Answer:** 13

```

#include <stdio.h>
int main () {
    typedef struct tag {
        char str[10];
        int a;
    } har;
    har h2 = { "IHelp", 10 };
    har h1 = h2;
    h1.str[1] = 'h';
    printf("%s %d", h1.str, h1.a);
    return 0;
}

```

**Answer:** Ihelp 10

```

#include<stdio.h>
double recurse (int A[], int N) {
    if (N == 1)
        return((double)A[N-1]);
    else
        return((double)(recurse(A,N-1)
            *(N-1)+A[N-1]) / N);
}
int main () {
    double result = 0;
    int A[] = { 1, 2, 3, 4 };
    int N = sizeof(A)/sizeof(A[0]);
    printf (".2lf", recurse(A,N));
    return 0;
}

```

**Answer:** 2.50

```

#include <stdio.h>
typedef struct _str {
    int mem1, mem2;
    struct _str* next;
} STR;
int main () {
    STR var1 = { 1, 2, NULL };
    STR var2 = { 10, 20, NULL };
    var1.next = &var2;
    STR *ptr1 = &var1;
    printf ("%d %d",
        ptr1->next->mem1,
        ptr1->next->mem2);
    return 0;
}

```

**Answer:** 10 20

- Q2.** The following C function takes a string (pointer to character) as argument, removes all duplicate adjacent characters from the string using a *stack* (`st[]` with top index) and returns the shortened string in reverse. For example, if the input string is “azxxzy”, then the output will be “ya” because the removal of “xx” modifies the string to “azzy”, and then the removal of “zz” modifies the string to “ay”, and finally “ay” does not containing duplicates, so the output string became “ya”. Similarly, if the input string is given as “aacdd” or “abccba”, then the output will be an *empty string* in both cases (and the function returns the phrase “EMPTY”). Fill in the blanks in the following code snippet (*stack operations should be written explicitly inside the code*) to achieve the desired result. **(5)**

```

char *shortenString ( char *str ) {
    char st[100];   int top = -1, i, j;
    for ( i = 0; str[i] != '\0'; ++i ) {
        if ( (top == -1) || ( _____ str[i] != st[top] _____ ) ) (1)
            st[++top] = _____ str[i] _____ ; /* push here */ (1)
        else _____ --top _____ ; /* pop here */ (1)
    } /* check for emptiness below */
    if ( _____ top == -1 _____ ) return "EMPTY"; (1)
    else {
        char* shortStr = (char*) malloc ((top+2)*sizeof(char));
        for ( j=0; top != -1; j++ )
            shortStr[j] = _____ st[top--] _____ ; /* pop here */ (1)
        shortStr[j] = '\0';
        return shortStr;
    }
}

```

- Q3.** The following C function takes as its arguments a pointer to the head node of a linked list (the node structure is also defined below) and an integer *n* to indicate the position (node distance) from last node and then finds/prints the data of the node which is *n* positions (nodes) before the last node (*n* = 0 indicates the last node). Fill in the blanks in the following code snippet to achieve the desired result. **(5)**

```

struct node {
    int num;
    struct node *next;
};

void nthnode ( struct node *head, int n ) {
    struct node *p, *q;   int i;   q = p = head;
    for ( i = 0; (i < n) && ( _____ q != NULL _____ ); i++ ) (1)
        q = _____ q->next _____ ; (1)
    if (q == NULL) printf ("List has Less Elements than the Entered n.");
    else {
        while ( _____ q->next _____ != NULL ) { (1)
            _____ q _____ = q->next; (1)
            p = _____ p->next _____ ; (1)
        }
        printf ("%d is Positioned %d Nodes before Last Node.", p->num, n) ;
    }
}

```

- Q4. (a)** Any rational number (fractions of the form  $\frac{x}{y}$ , where  $y \neq 0$ ) can be normalized to its lowest form by dividing both its numerator and the denominator with their greatest common divisor (GCD). Complete the following C function, which takes as its argument two integers x and y (assume that,  $y \neq 0$ ) presenting the fraction  $\frac{\pm x}{\pm y}$ , and computes the lowest form of that fraction. The function also normalizes the sign of the overall fraction from the individual signs ( $\pm$ ) of x and y, finally printing it as  $\pm \frac{a}{b}$  (where,  $\frac{a}{b}$  becomes the normalized version of  $\frac{x}{y}$ ). (7)

```
void normRat ( int x, int y ) {
    int sign = 1, gcd, temp, rem;
    if ( x < 0 ) { sign = _____ -1 (or, -sign) _____ ; x = - x ; } (0.5)
    if ( y < 0 ) { sign = _____ sign * (-1) _____ ; y = - y ; } (0.5)
    if ( _____ x >= y _____ ) { gcd = x; temp = y; } (1)
    else { gcd = y; temp = x; }
    while ( _____ temp > 0 (or, temp != 0) _____ ) { (1)
        rem = _____ gcd % temp _____ ; (1)
        gcd = _____ temp _____ ; (1)
        temp = _____ rem _____ ; (1)
    }
    ( sign > 0 ) ? printf ("+") : printf ("-") ;
    printf ( " %d / %d", _____ x / gcd _____ , _____ y / gcd _____ ); (1)
}
```

- (b)** Every positive rational number (such as  $\frac{x}{y}$ , where  $x, y > 0$ ) has an essentially unique finite continued fraction representation, which can be expressed mathematically as:

$$\frac{x}{y} = q_0 + \frac{1}{q_1 + \frac{1}{q_2 + \frac{1}{q_3 + \frac{1}{\ddots \frac{1}{q_n}}}}} \equiv [q_0 \ q_1 \ q_2 \ q_3 \ \cdots \ q_n] \leftarrow (\text{notation})$$

Such a representation for any rational number follows directly the basic division (with quotient and remainder) principle, which is shown below:

$$\frac{x}{y} = q_0 + \frac{r_0}{y} = q_0 + \frac{1}{\frac{y}{r_0}} = q_0 + \frac{1}{q_1 + \frac{r_1}{r_0}} = q_0 + \frac{1}{q_1 + \frac{1}{\frac{r_0}{r_1}}} = q_0 + \frac{1}{q_1 + \frac{1}{q_2 + \frac{r_2}{r_1}}} = \cdots = q_0 + \frac{1}{q_1 + \frac{1}{q_2 + \frac{1}{\ddots \frac{1}{q_n}}}}$$

Note that, each division above of the form  $\left[ \frac{x}{y}, \frac{y}{r_0}, \frac{r_0}{r_1}, \frac{r_1}{r_2}, \dots, \frac{r_{n-3}}{r_{n-2}}, \frac{r_{n-2}}{r_{n-1}} \right]$  produces the quotients  $[q_0, q_1, q_2, q_3, \dots, q_{n-1}, q_n]$ , and the remainders  $[r_0, r_1, r_2, r_3, \dots, r_{n-1}, 0]$ , respectively. Here, the final remainder, i.e.  $r_n = 0$ , since such a representation of any rational number is *finite*.

Complete the following C function, which takes as its argument two positive integers x and y, computes the finite continued fraction representation for  $\frac{x}{y}$ , and prints the representation obtained in the notational form,  $[q_0 \ q_1 \ q_2 \ q_3 \ \cdots \ q_n]$ , as shown above. (5)

```
void cfRat ( unsigned int x, unsigned int y ) {
    unsigned int z;
    printf ("[ ");
    do { printf ("%u ", _____ x / y _____ ); (1)
        z = y;
        y = _____ x - y * ( x / y ) (or, x % y) _____ ; (2)
        x = _____ z _____ ; (1)
    } while ( _____ y > 0 (or, y != 0) _____ ); (1)
    printf ("]");
}
```

- (c) The generalized (and infinite) form for the continued fractions are:  $a_0 + \frac{a_1}{a_2 + \frac{a_3}{a_4 + \frac{a_5}{\ddots}}}$

There are interesting algebraic manipulations possible with this. In particular, you can determine square root of any positive number  $n$  using this concept. For example, to determine  $x = \sqrt{n}$ , we solve the equation  $x^2 = n$  as:

$$x^2 - 1 = n - 1 \implies (x+1)(x-1) = n-1 \implies x-1 = \frac{n-1}{1+x} \implies x = 1 + \frac{n-1}{1+x}$$

Now, the  $x$  in the RHS denominator can be further decomposed iteratively as continued fractions with the existing  $x$  from LHS itself – thereby stepwise expanding to,

$$x = \sqrt{n} = 1 + \frac{n-1}{1+x} = 1 + \frac{n-1}{2 + \frac{n-1}{1+x}} = \dots = 1 + \frac{n-1}{2 + \frac{n-1}{2 + \frac{n-1}{\ddots}}}$$

Complete the following C function, which takes as its argument a positive integer  $n$ , and computes/returns its square root (i.e.,  $\sqrt{n}$ ) by iterative expansion of the continued function as shown above. Though the continued fraction form may be infinite, but your computation of square root must stop when the difference of the derived roots in successive steps fall below a threshold (say,  $|\text{next} - \text{root}| \leq 10^{-6}$ ). You may use functions from `math.h` library. (4)

```
double sqRoot ( unsigned int n ) {
    double root, next = 1.0;
    do {
        root = next;
        next = 1.0+(n-1)/(1.0+root) (or, 1.0+(n-1)/(1.0+next)) ; (2)
    } while ( fabs ( next - root ) > 0.000001 ) ; (1)
        (or, ((next-root)>0.000001) || ((root-next)>0.000001) )
    return next (or, root) ; (1)
}
```

- (d) Generalizing the procedure adopted in Part (b), the real roots of a quadratic equation (of the form  $x^2 + bx + c = 0$ , where  $b^2 \geq 4c$ ) can also be determined. We may find one root as follows:

$$x^2 + bx + c = 0 \implies x = -b - \frac{c}{x} = -b - \frac{c}{-b - \frac{c}{x}} = \dots = -b - \frac{c}{-b - \frac{c}{\ddots}}$$

However, the other root can then be obtained by the known formula, i.e.  $\frac{c}{x}$ .

Complete the following C function, which takes as its argument two real values  $b$  and  $c$  presenting the quadratic equation of the form  $x^2 + bx + c = 0$  (assume that,  $b^2 \geq 4c$  and  $b \neq 0$ ), and computes/prints both of its roots by the iterative expansion of the continued function as shown above. Though the continued fraction form may be infinite, but your computation of square root must stop when the difference of the derived roots in successive steps fall below a threshold (say,  $|\text{next} - \text{root}| \leq 10^{-6}$ ). You may use functions from `math.h` library. (4)

```
void quadRoot ( double b, double c ) {
    double root, next = - b;
    do {
        root = next;
        next = - b - c/root (or, - b - c/next) ; (1)
    } while ( fabs ( next - root ) > 0.000001 ) ; (1)
        (or, ((next-root)>0.000001) || ((root-next)>0.000001) )
    printf ("Roots=(%lf,%lf)", next (or, root) , c/next (or, c/root) ) ; (2)
        (or, -next-b; or, -root-b)
}
```

- Q5.** Fill in the blanks of the following C function which recursively arranges an array of integers such that all negative numbers and zeros precede all positive numbers. For example, given an array of a list of integers {1, 14, -3, 4, 5, 6, 0, -2}, a possible arrangement would be {-2, 0, -3, 4, 5, 6, 14, 1}. (8)

```

void negpos ( int *A, int n ) { (1)
    int i = 0, j = n-1, temp;
    while ( A[j] > 0 ) j--; (1)
    while ( A[i] <= 0 ) i++; (1)
    if ( i < j ) {
        temp = A[i];
        A[i]= A[j]; (1)
        A[j]= temp; (1)
        negpos ( A+i+1, j-i-1 ); (3)
    }
}

```

- Q6.** Consider the following C program and answer the following questions. Assume that a variable of data type int required 4 bytes of storage space.

```

#include <stdio.h>
int check ( int *p, int n ) {
    int i, temp, mid;
    for ( i=0; i<n-1; i++ )
        if ( p[i] > p[i+1] ) { temp = p[i]; p[i] = p[i+1]; p[i+1] = temp; }
    for ( i=n-1; i>0; i-- )
        if ( p[i] < p[i-1] ) { temp = p[i]; p[i] = p[i-1]; p[i-1] = temp; }
    mid = (p[0] + p[n-1]) / 2;
    return ( ( mid > p[n/2] ) ? 1 : 0 );
}
int main () {
    int A[10] = { 2, 4, -3, 6, -9, 1, -5, 2, 10, 7 }, val = check(A,10);
    printf ("%lu %d %d %d", sizeof(A)/sizeof(int), A[0], A[9], val);
    return 0;
}

```

- (a) What is the output of the above C program? (4)

**Answer:** 10 -9 10 0

- (b) Suppose the address of A[3] is 1866954492 (in decimal). What would be the address of A[7]? (2)

**Answer:** 1866954508

- (c) What value would be passed to the argument variable p in the function check(.) when it is called in the program from main()? (2)

**Answer:** 1866954480

- (d) What would be the value of &A + 1? (2)

**Answer:** 1866954520



**Q7.** Consider a 2D grid ( $nr \times nc$ ) of characters and a single word (pattern), Your task is to find all occurrences of the given word in the grid in the diagonal direction North-East (Right and Up) as illustrated in Fig. 1. Fill in the blanks of the following C functions to achieve the desired result. **(9)**

Consider the following example of a  $5 \times 5$  grid ( $nr = nc = 5$ ),

```

g a a g g
g a g a g
g a g a a
g a g a g
g a g a g

```

- If the pattern is "gag", there are 4 matches (refer to Fig. 2).
- If the pattern is "agg", there is 1 match.
- If the pattern is "gaag" there is 0 match.

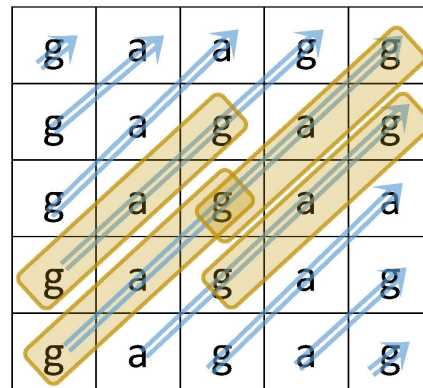
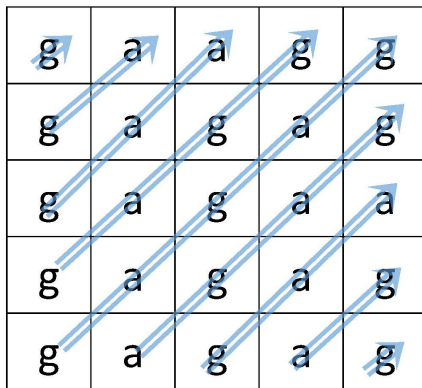


Fig 1: Diagonal directions to be considered      Fig 2: Matches of pattern "gag" in the grid

```

int matchRUDiag ( char cmat[][100], char *pattern,
                  int nr, int nc, int i, int j ) {

    if ( pattern[0] == _____ '\0' ) /* base condition 1 */ (1)
        return _____ 1 _____ ; (0.5)
    if ( (i>=nr) || (j>=nc) ) _____ /* base condition 2 */
        return _____ 0 _____ ; (0.5)

    if ( pattern[0] == _____ cmat[i][j] ) /* recursive call */ (1)
        return matchRUDiag ( _____ cmat, pattern+1, nr, nc, i-1, j+1 _____ ) ; (2)

    return _____ 0 _____ ; /* unmatched condition return */ (1)
}

int checkRUDiag ( char cmat[][100], char *pattern, int nr, int nc ) {
    int count = 0, i, j;

    for ( i = 0; i < _____ nr _____ ; i++ ) (1)
        for ( j = 0; j < _____ nc _____ ; j++ ) (1)
            if ( matchRUDiag(cmat, pattern, nr, nc, i, j) )
                _____ count ++ ; (1)

    return count;
}

```

- Q8.** Given a sorted array  $A[]$  of  $n$  natural numbers and a natural number  $x$ , find a pair in the array whose sum is closest to  $x$ . Assume that the values of the numbers in  $A[]$  as well as the value of  $x$  is at most 100. Fill in the blanks of the following C function to achieve the desired result. Assume that you may use the function having the prototype as `int abs(int x);` from `stdlib.h` library that takes as input an integer and returns its absolute value. **(12)**

```

#include <stdlib.h>
#define MAXVAL 100
void closestPair ( int A[], int n, int x ) {
    /* index variables to hold the pair whose sum is closest to x */
    int idxL, idxR;
    /* variable to store current minimum difference between a pair and x */
    int minDiff = 2 * MAXVAL;
    /* auxiliary variables to be used inside iteration */
    int i, left, right, mid, elm;
    for ( i = 0; i<n; i++ ) {
        elm = A[i];
        /* using binary search technique to find the element d
           in the array A[] such that (elm + d) is closest to x */
        left = _____ i + 1 _____ ; (1)
        right = _____ n - 1 _____ ; (1)
        while ( left <= right ) {
            mid = _____ ( left + right ) / 2 _____ ; (1)
                    (or, left + (right - left) / 2)
            if ( A[mid] + elm == x ) {
                idxL = _____ i (or, mid) _____ ; (1)
                idxR = _____ mid (or, i) _____ ; (1)
                minDiff = _____ 0 _____ ; (1)
                break;
            }
            /* check if this pair is closer than the closest pair so far */
            if ( abs(A[mid] + elm - x) < minDiff ) {
                minDiff = _____ abs(A[mid] + elm - x) _____ ; (1)
                idxL = _____ i (or, mid) _____ ; (1)
                idxR = _____ mid (or, i) _____ ; (1)
            }
            /* update binary searching ranges accordingly */
            if ( A[mid] + elm < x )
                left = _____ mid + 1 _____ ; (1)
            else
                right = _____ mid - 1 _____ ; (1)
        }
    }
    printf ("Pair = (%d , %d)", _____ A[idxL] _____ , _____ A[idxR] _____ ); (1)
}

```

- Q9.** A  $k$ -nearly sorted array is one where each element is at a distance of at most  $k$  from its actual sorted position. For example,  $\{2, 6, 3, 12, 56, 8\}$  is a 3-nearly sorted array. The following C function takes as input a  $k$ -nearly sorted array and sorts it. Fill in the blanks of the following C function to achieve the desired result. (6)

```
void nearlySort ( int A[], int size, int k ) {
    int i, j, key;
    for ( i=1; i<size; i++ ) {
        key = _____ A[i] _____ ; (1)
        j = i - 1;
        /* in the following loop, j must have a non-negative value
           as it represents an index of this k-nearly sorted array */
        while ( ( _____ (i-k>=0 && i-k<=j) || (j>=0) _____ ) (3)
                && (A[j] > key) ) {
            A[j+1] = A[j];
            _____ j-- ; _____ /* update j */ (1)
        }
        _____ A[j+1] _____ = key ; (1)
    }
}
```

- Q10.** Represent the following numbers in the mentioned formats.

- (a) The Binary outcome of  $(3 - 6)$  when operated in 1's complement form. Assume, there are 4 bits allocated for storage of these numbers. State whether there is an overflow. (1.5)

**Answer:**      0011 (+3) + 1001 (-6) = 1100 (-3)      NO Overflow!

- (b) The Binary outcome of  $(6 + 7)$  when operated in 2's complement form. Assume, there are 4 bits allocated for storage of these numbers. State whether there is an overflow. (1.5)

**Answer:**      0110 (+6) + 0111 (+7) = 1101 (-3)      Overflow!

- (c) The Binary representation of  $-119.362$  in IEEE754 Single-Precision Floating-Point format. (2)

**Answer:** 1 (sign)    10000101 (exp.)    11011101011100101011000 (mant.)

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The question paper ends here.

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