

Unknown Target function,  $f: x \rightarrow y$

Training Examples  
 $\langle x_1, y_1 \rangle \dots \langle x_N, y_N \rangle$

Learning Algorithm

Final Hypothesis  
 $g \approx f$

Hypothesis Set  
 $H = \{h_1, h_2, \dots, h_M\}$

Learning Diagram

What is learning?

When can we learn?

Can we Really learn?

How to learn?

How to learn/do it well?

Path Ahead !!

► Hoeffding Inequality:

$$\text{Prob} \left[ |E_{\text{in}}(g) - E_{\text{out}}(g)| > \epsilon \right] \leq 2Me^{-2\epsilon^2 N}$$

P.A.C.

Concept Learning

# Ordering of Hypothesis:

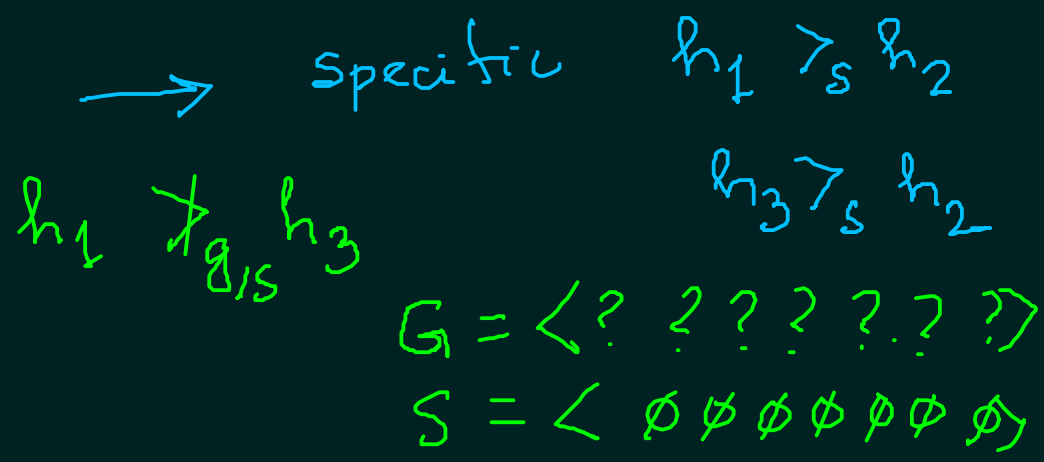
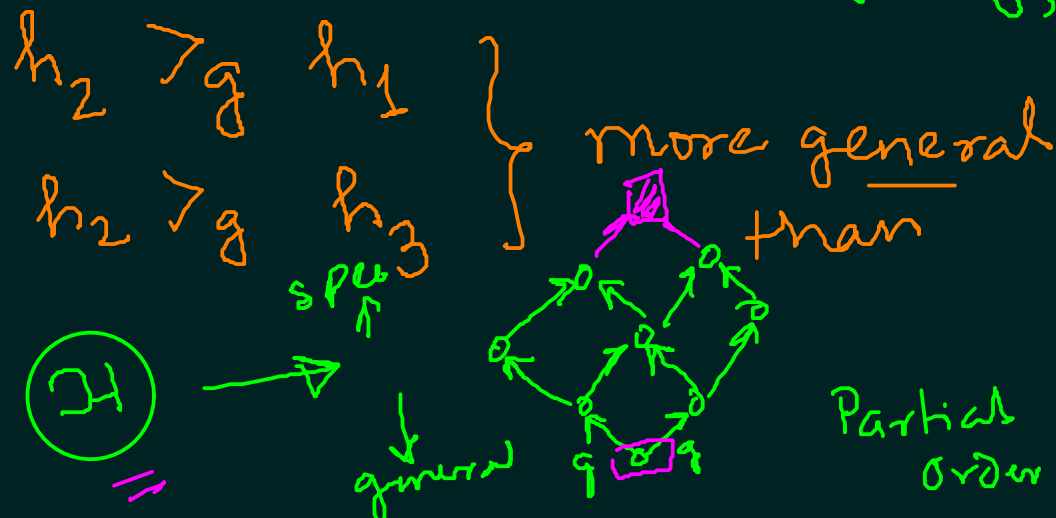
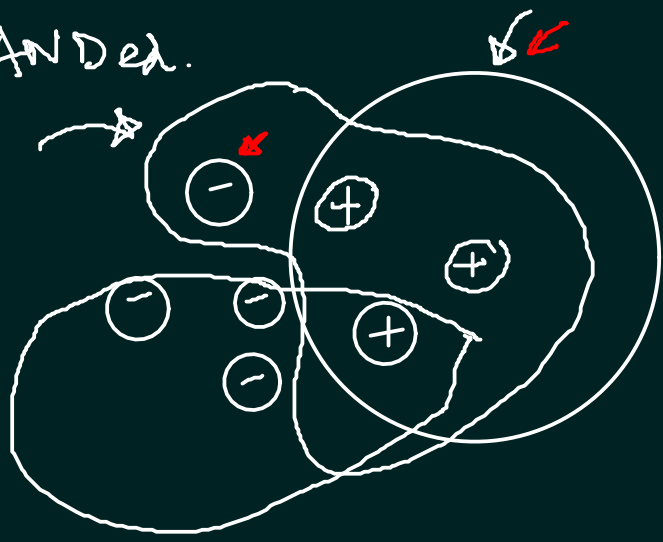
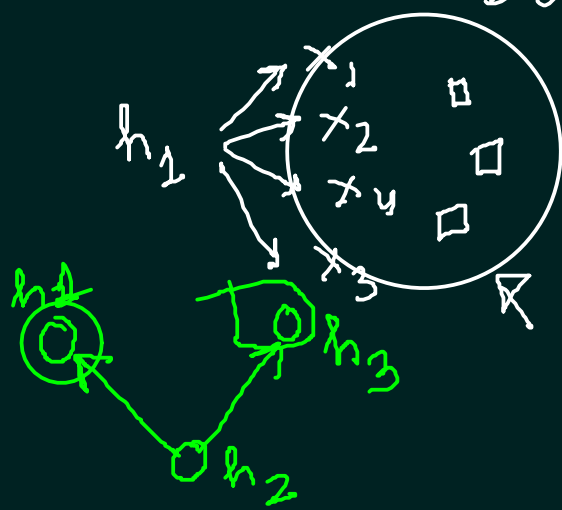
Sky	Temp	Humid	Wind	Water	Forecst	EnjoySpt
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

$h_1 = \langle \text{Sunny}, ?, ?, \text{Strong}, ?, ? \rangle$

$h_2 = \langle \text{Sunny}, ?, ?, ?, ?, ? \rangle$

$h_3 = \langle \text{Sunny}, ?, ?, ?, \text{Cool}, ? \rangle$

Boolean functions  $\rightarrow$  ANDed.



# Concept Learning (C TARGET)

Boolean functions

	Sky	Temp	Humid	Wind	Water	Forecast	EnjoySpt
c	Sunny	Warm	Normal	Strong	Warm	Same	Yes
c	Sunny	Warm	High	Strong	Warm	Same	Yes
c	Rainy	Cold	High	Strong	Warm	Change	No
	Sunny	Warm	High	Strong	Cool	Change	Yes

$h \approx c$  (Sky=Sunny)  $\wedge$  (Humid=High)

- $h_1 = \langle \text{Sunny}, ?, \text{High}, ?, ?, ? \rangle$   
 $h_2 = \langle \text{Rainy}, ?, ?, ?, \text{Cool}, ? \rangle$   
 $h_3 = \dots$   
 $h_m$

Training Example (TE)

?  $\rightarrow$  anything (TRUE)  
 $\emptyset \rightarrow$  nothing (FALSE)

Only 4 TEs

Goal:  $\forall x \in X, h(x) = c(x)$

Search Problem: Sky = { Sunny, Rainy, Cloudy }  $\Rightarrow |Sky| = 3$   
 |Temp| = |Humid| = |Wind| = |Water| = |Forecast| = 2

# Instances =  $3 \times 2 \times 2 \times 2 \times 2 \times 2 = 96 \rightarrow 2^{96}$  Hypothesis all together!

# Hypothesis (our Restriction) =  $(3+2) \times (2+2) \times (2+2) \times (2+2) \times (2+2) \times (2+2) = 5120$

Actual Possible =  $4 \times 3 \times 3 \times 3 \times 3 \times 3 + 1$   
 Hypothesis = 973

# Concept Learning

↳ Inductive Learning  
Hypothesis Assumption



↳ Hypothesis Set

Sky	Temp	Humid	Wind	Water	Forecast	EnjoySpt
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes <del>No</del>
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

Training Data (TE)

Learn Boolean function

▶ Most Specific Hypothesis

$$h^S = \langle \phi, \phi, \phi, \phi, \phi, \phi \rangle$$

▶ Most General Hypothesis

$$h^G = \langle ?, ?, ?, ?, ?, ? \rangle$$

## Find-S Algorithm?

↳ Take +ve Examples only

↳ Start from  $h^S$  and Relax

$$\langle \phi, \phi, \phi, \phi, \phi, \phi \rangle$$

TE<sub>1</sub>:  $\langle \text{Sunny, Warm, Normal, Strong, Warm, Same} \rangle$

TE<sub>2</sub>:  $\langle \text{Sunny, Warm, ? , Strong, Warm, Same} \rangle$

TE<sub>3</sub>: DO NOTHING

TE<sub>4</sub>:  $\langle \text{Sunny, Warm, ? , Strong, ? , ?} \rangle$

ANSWER

## NOTE:

(1) Correctness

(2) TE Noise

(3) Why most specific?

(4) Multiple Hyp??

# Version Space:

Sky	Temp	Humid	Wind	Water	Forecst	EnjoySpt
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

S: < Sunny, Warm, ?, Strong, ?, ? >

< Sunny, ?, ?, Strong, ?, ? >

< Sunny, Warm, ?, ?, ?, ? >

< ?, Warm, ?, Strong, ?, ? >

G: < Sunny, ?, ?, ?, ?, ? >

< ?, Warm, ?, ?, ?, ? >

- Consistent  $(h, \mathcal{D}) = \forall \langle x, f(x) \rangle \in \mathcal{D} [h(x) \equiv f(x)]$
  - Version Space,  $VS_{\mathcal{H}, \mathcal{D}} = \{ h \in \mathcal{H} \mid \text{consistent}(h, \mathcal{D}) \}$
  - General Boundary,  $G = \{ g \in \mathcal{H} \mid \text{consistent}(g, \mathcal{D}) \wedge \neg \exists g' (g' \succ_g g) \wedge \text{consistent}(g', \mathcal{D}) \}$
  - Specific Boundary,  $S = \{ s \in \mathcal{H} \mid \text{consistent}(s, \mathcal{D}) \wedge \neg \exists s' (s \succ_s s') \wedge \text{consistent}(s', \mathcal{D}) \}$
- List-And-Eliminate —

# Candidate Elimination Algorithm

Sky	Temp	Humid	Wind	Water	Forecst	EnjoySpt
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

$S_0: \langle \emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset \rangle$

$S_1: \langle \text{Sunny, Warm, Normal, Strong, Warm, Same} \rangle$

$S_2: \langle \text{Sunny, Warm, ? , Strong, Warm, Same} \rangle$

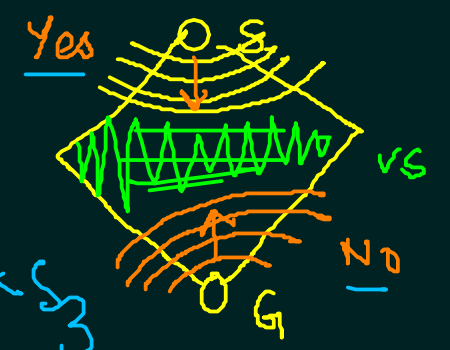
$S_3: \langle \text{Sunny, Warm, ? , Strong, ? , ?} \rangle$

$G_1: \langle \text{Sunny, ? Strong, ?} \rangle$     $G_2: \langle \text{Sunny, Warm, ? , ?} \rangle$     $G_3: \langle \text{?, Warm, ? Strong, ?} \rangle$

$G_4: \langle \text{Sunny, ? , ? , ?} \rangle$  ,  $G_5: \langle \text{? Warm, ? , ? , ?} \rangle$

$G_6: \langle \text{Sunny, ? , ? , ?} \rangle$     $G_7: \langle \text{? Warm, ? , ? , ?} \rangle$     $G_8: \langle \text{? , ? , ? , Same} \rangle$

$G_9: \langle \text{? , ? , ? , ? , ? , ?} \rangle \leftarrow G_1, G_2$

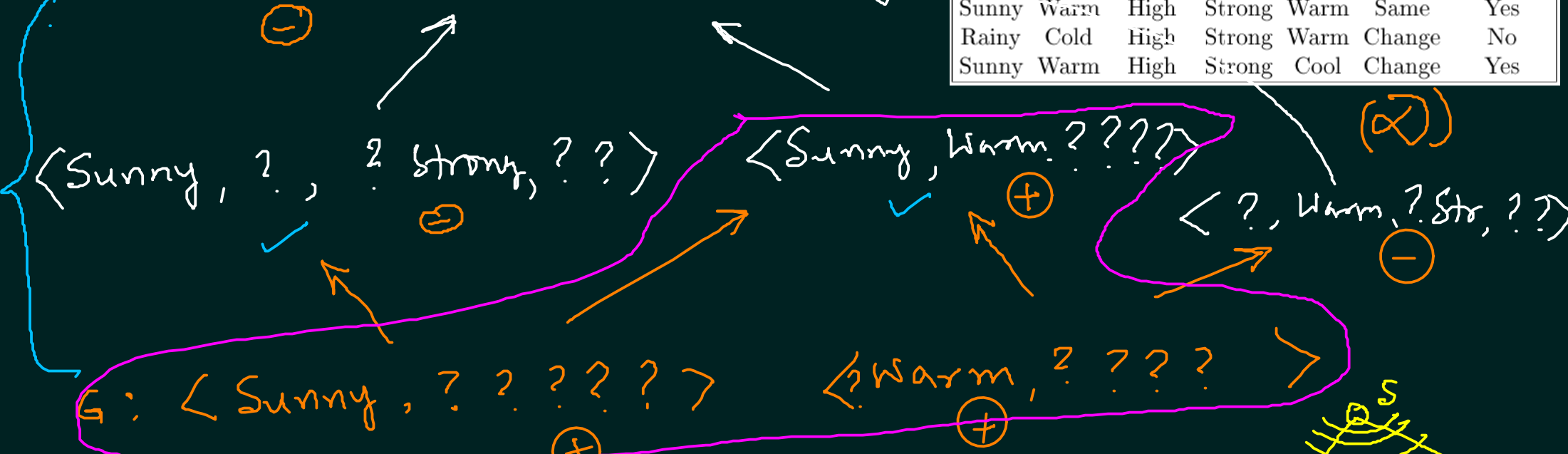


VS

$G_3, G_4$

Sky	Temp	Humid	Wind	Water	Forecast	EnjoySpt
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

S: < Sunny, Warm?, Strong, ?, ? >



▷ Correct: — Converge

→ what if TE error?

Wrong Hyp  
E vs

Correct Hyp.  
E vs



▷ If Test Data available

↳ Accuracy — 50%

Test: [ < Sunny, Warm, Normal, Light, Warm, Same > ] → +ve Yes

Train

[∞] ← data

3+      3-

$\lceil \log_2 |VS| \rceil$   
TE

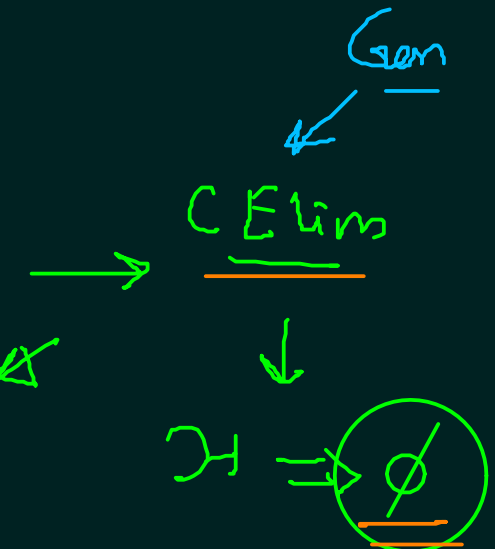
next? TE

$n$  attributes  $\rightarrow$  2 values  $\rightarrow$   
 $\# \text{Inst} = 2 \times 2 \times \dots \times 2$  (n times)

Concepts  $\rightarrow$   $2^{2^n}$  Hyp.

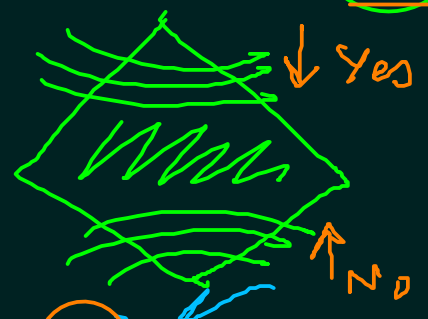
Restriction:  $\langle c \wedge b \wedge a \wedge d \rangle \leftarrow \text{Hyp}$   $\leftarrow 3^n + 1$   
 $\hookrightarrow$  [Inductive Bias]

Sun	Wrm	Norm	Strong	Cool	Change	Yes
Clody	"	"	"	"	"	Yes
Rainy	"	"	"	"	"	No



$\langle ? \wedge \text{Wrm} \wedge \text{Nor} \wedge \text{Str} \wedge \text{Cool} \wedge \text{Chg} \rangle \times$

$\langle \text{Sun} ? ? ? ? ? \rangle \vee \langle \text{Clody} , ? ? ? ? ? \rangle$



$x_1 \rightarrow \text{Yes}$   
 $x_2 \rightarrow \text{Yes}$   
 $x_3 \rightarrow \text{Yes}$   
 $x_4 \rightarrow \text{No}$   
 $x_5 \rightarrow \text{No}$

$S = (x_1 \vee x_2 \vee x_3)$   
 $G = (\neg (x_4 \vee x_5))$



Puzzle : 3 TE , 1 TE

⇒ ONLINE  
vs  
BATCH  
(next)

<u>Season</u>	<u>Weather</u>	<u>Play Football</u>
Summer	↔ Rain	Yes
Winter	↔ Dry	Yes
Winter	* Rain	NO

TE

TEST: < Summer, Dry > → ?

What can ML/c learn from 1 TE?  
(vs) Human

Ref: (ML Book)  
Tom Mitchell  
(2nd Chap)