

Class coNP

$$\text{coNP} = \{ L : \neg L \in \text{NP} \}$$

Alternate definition

$L \in \text{coNP}$ if \exists a polynomial $p: \mathbb{N} \rightarrow \mathbb{N}$ & a poly-time DTM M s.t.

$$x \in L \Leftrightarrow \forall u \in \Sigma^{p(|x|)} \text{ s.t. } M(x, u) \text{ accepts.}$$

Examples

$$\rightarrow \neg \text{SAT} = \{ \phi : \phi \text{ is not satisfiable} \}$$

$$\rightarrow \text{TAUTOLOGY} = \{ \phi : \phi \text{ is true for every assignment} \}.$$

$L \in \text{coNP-Hard}$ if $\forall A \in \text{coNP}, A \leq_p L$

$L \in \text{coNP-Complete}$ if $L \in \text{coNP}$ & L is coNP-Hard

Question $\text{NP} \stackrel{?}{=} \text{coNP}$ is open. & related
to the $\text{P} \stackrel{?}{=} \text{NP}$ question.