## Introduction to GRAPHS



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## Graphs

## A Graph $G=(V, E)$ consists of the

 following:- A set of Vertices or Nodes V
- Nodes may have one or more labels
- A set of Edges E where each edge connects vertices of $V$
- An edge usually defines a connection or relationship between vertices or nodes
- The edges can be undirected or directed
- Each edge can have one or more labels
- Usually there is at most one edge between vertices, there could be multiple edges between the same nodes.
- Normally an edge connects two vertices, but in general we could have hyper-edges


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## Some Applications of Graphs

- Maps, Routes
- Layouts
- Circuits and Networks
- Relationships
- Constraints
- Dependencies
- Flow Charts
- State Machines



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Instructions

- fill in words from the list

```
List of Words
* Aft * Laser
- Ale - Lee
* Eel * Line
- Hike . Sails
* Hoses * Sheet
- Keel - Steer
    - Knot - Tie
```


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## Graph Representation



Adjacency List

Adjacency Matrix

## Graph Representation



Adjacency Matrix
Adjacency List

## Some Algorithms on Graphs

- Paths
- Reachability
- Connected Components
- Trees, Cycles, ordering

- Costs \& Distances
- Spanning Trees
- Shortest Paths
- Flows


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## Thank you

