## Mid Semester Examination, Autumn 2003-04

September 23, 2003

Total time: 2 hours

Total points: 50

1. Write regular expressions for representing the following languages over the alphabet  $\{0, 1\}$ :  $(2\times4)$ (a)  $\{\alpha \mid \alpha \text{ starts with } 0 \text{ and ends with } 1\}$ **(b)**  $\{\alpha \mid \alpha \text{ starts with } 01 \text{ and ends with } 10\}$ (c)  $\{\alpha \mid \alpha \text{ contains } 000 \text{ as a substring}\}$ (d)  $\{\alpha \mid \alpha \text{ does not contain } 000 \text{ as a substring}\}$ **2.** (a) Design a DFA to accept the language  $\{0,1\}^* \setminus \{11,111\}$ . **(4)** (b) Design an NFA with three states to accept the language of the regular expression 0\*1\*0\*0. **(4)** (c) Design an  $\epsilon$ -NFA to accept the set of strings over  $\{0,1\}$ , that have at least one 1 in the last ten positions. (4) **3.** Let L be a regular language and let  $n \in \mathbb{N}$  be a pumping lemma constant for L. (a) Show that any integer  $n' \ge n$  can be used as a pumping lemma constant for L. **(4)** (b) The minimum pumping lemma constant for L is the smallest positive integer m, such that m can be a pumping lemma constant for L. Determine the minimum pumping lemma constants for the languages over the alphabet  $\{0, 1\}$ , defined by the following regular expressions:  $(2\times3)$ (1) 01(2) 01\* $(3) (01)^*$ **4.** Prove that the following languages over the alphabet  $\{0,1\}$  are not regular.  $(5\times2)$ (a)  $\{\alpha \mid \alpha \text{ is not a palindrome}\}$ **(b)**  $\{0^i 1^j \mid i \neq j\}$ **5.** Which of the following languages over the alphabet  $\{0,1\}$  is/are regular?  $(5\times2)$ (a)  $\{\alpha \mid \alpha \text{ contains an equal number of occurrences of } 0 \text{ and } 1\}$ **(b)**  $\{\alpha \mid \alpha \text{ contains an equal number of occurrences of } 01 \text{ and } 10\}$