

**CS29003 ALGORITHMS LABORATORY**  
**Assignment No: 7**  
**Last Date of Submission: 11-September-2014**

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Let  $A$  and  $B$  two strings of lengths  $n$  and  $m$  over an alphabet  $\Sigma$ . (An *alphabet* is a finite set of symbols from which the individual characters of a string are chosen.) Assume that  $n$  is somewhat larger than  $m$ , and the size of the alphabet  $\Sigma$  is small. (Work with alphabets like  $\{a, b\}$ ,  $\{a, b, c\}$ ,  $\{a, b, c, d\}$ .) For  $t \geq 0$ , define  $B_t$  to be the string  $B$  with each character repeated  $t$  times. For example, if  $B$  is the string  $ccab$ , then  $B_3 = cccccaabb$ .

A string  $D = d_0 d_1 \dots d_{l-1}$  is called a *subsequence* of a string  $C = c_0 c_1 \dots c_{k-1}$  if  $d_j = c_{i_j}$  for all  $j = 0, 1, 2, \dots, l-1$  for some indices in  $C$  satisfying  $0 \leq i_0 < i_1 < i_2 < \dots < i_{l-1} \leq k-1$ . This means that all the symbols in  $D$  appear in the same sequence in  $C$ , although not necessarily consecutively. In this assignment, you write a program to find the largest  $t$  for which  $B_t$  is a subsequence of  $A$ . Note that the only possible values of  $t$  are  $0, 1, 2, \dots, \text{floor}(n/m)$ .

Write a function `issubseq()` to check whether one string is a subsequence of another.

Write a function `genBt()` to generate  $B_t$  from  $B$  and  $t$ .

Write a function `findt()` to compute the largest desired  $t$  mentioned above. This function would call the above two functions and should have a running time of the order  $O(n \log(n/m))$ .

Write a `main()` function to do the following:

- Read two strings  $A$  and  $B$  of lengths  $n$  and  $m$ , respectively.
- Call the function `findt()` to get the desired value of  $t$ .
- If  $t > 0$ , then print the match of  $B_t$  in  $A$  in the format given below.

**Sample Output**

In the example below, we have taken  $\Sigma = \{a, b, c\}$ ,  $n = 75$ , and  $m = 5$ . In this example, the largest  $t$  is 6. Convince yourself that  $B_7$  is not a subsequence of  $A$ .

```
A = cbcacaccbcacccbacaccbcacccbcbbaaaabcabcaaaaaabaaccabbacbbbabcbacbaaaaacbac
B = cbaab
t = 6
cbcacaccbcacccbacaccbcacccbcbbaaaabcabcaaaaaabaaccabbacbbbabcbacbaaaaacbac
c c c cc c   b   b   bb bbaaaa a   aaaaa a   bbb   bbb
|-----|   |-----| |-----| |-----|   |-----|
```

Here is another example in which  $|\Sigma| = 6$ . Now, the largest computed  $t$  is 1.

```
A = ccdeefceedafadbfcccccfbbaeeafcacddabcadecbeafdffbcdadcfbfedfaabffbdaafcca
B = fffec
t = 1
ccdeefceedafadbfcccccfbbaeeafcacddabcadecbeafdffbcdadcfbfedfaabffbdaafcca
  f     f     f             e     c
  |     |     |             |     |
```