



2-d Arrays

Two Dimensional Arrays

- We have seen that an array variable can store a list of values
- Many applications require us to store a **table** of values

	Subject 1	Subject 2	Subject 3	Subject 4	Subject 5
Student 1	75	82	90	65	76
Student 2	68	75	80	70	72
Student 3	88	74	85	76	80
Student 4	50	65	68	40	70

Contd.

- The table contains a total of 20 values, five in each line
 - The table can be regarded as a **matrix** consisting of **four rows** and **five columns**
- C allows us to define such tables of items by using **two-dimensional** arrays

Declaring 2-D Arrays

- General form:

```
type array_name [row_size][column_size];
```

- Examples:

```
int marks[4][5];
```

```
float sales[12][25];
```

```
double matrix[100][100];
```


Initializing 2-d arrays

- `int a[2][3] = {1,2,3,4,5,6};`
- `int a[2][3] = {{1,2,3}, {4,5,6}};`
- `int a[][3] = {{1,2,3}, {4,5,6}};`

All of the above will give the 2x3 array

1	2	3
4	5	6

Accessing Elements of a 2-d Array

- Similar to that for 1-d array, but use two indices
 - First indicates row, second indicates column
 - Both the indices should be expressions which evaluate to integer values (within range of the sizes mentioned in the array declaration)
- Examples:
 - $x[m][n] = 0;$
 - $c[i][k] += a[i][j] * b[j][k];$
 - $a = \text{sqrt}(a[j*3][k]);$

Example

```
int a[3][5];
```

A two-dimensional array of 15 elements

Can be looked upon as a table of 3 rows and 5 columns

	col0	col1	col2	col3	col4
row0	a[0][0]	a[0][1]	a[0][2]	a[0][3]	a[0][4]
row1	a[1][0]	a[1][1]	a[1][2]	a[1][3]	a[1][4]
row2	a[2][0]	a[2][1]	a[2][2]	a[2][3]	a[2][4]

How is a 2-d array is stored in memory?

- Starting from a given memory location, the elements are stored **row-wise** in consecutive memory locations (**row-major** order)

- x: starting address of the array in memory
- c: number of columns
- k: number of bytes allocated per array element

□ $a[i][j]$ → is allocated memory location at
address $x + (i * c + j) * k$

$a[0][0]$	$a[0][1]$	$a[0][2]$	$a[0][3]$	$a[1][0]$	$a[1][1]$	$a[1][2]$	$a[1][3]$	$a[2][0]$	$a[2][1]$	$a[2][2]$	$a[2][3]$
Row 0				Row 1				Row 2			

Array Addresses

```
int main()
{
    int a[3][5];
    int i,j;

    for (i=0; i<3;i++)
    {
        for (j=0; j<5; j++) printf("%u\n", &a[i][j]);
        printf("\n");
    }
    return 0;
}
```

Output

```
3221224480
3221224484
3221224488
3221224492
3221224496

3221224500
3221224504
3221224508
3221224512
3221224516

3221224520
3221224524
3221224528
3221224532
3221224536
```


More on Array Addresses

```
int main()
{
    int a[3][5];
    printf("a = %u\n", a);
    printf("&a[0][0] = %u\n", &a[0][0]);
    printf("&a[2][3] = %u\n", &a[2][3]);
    printf("a[2]+3 = %u\n", a[2]+3);
    printf("*(a+2)+3 = %u\n", *(a+2)+3);
    printf("*(a+2) = %u\n", *(a+2));
    printf("a[2] = %u\n", a[2]);
    printf("&a[2][0] = %u\n", &a[2][0]);
    printf("(a+2) = %u\n", (a+2));
    printf("&a[2] = %u\n", &a[2]);
    return 0;
}
```

Output

```
a = 3221224480
&a[0][0] = 3221224480
&a[2][3] = 3221224532
a[2]+3 = 3221224532
*(a+2)+3 = 3221224532
*(a+2) = 3221224520
a[2] = 3221224520
&a[2][0] = 3221224520
(a+2) = 3221224520
&a[2] = 3221224520
```


How to read the elements of a 2-d array?

- By reading them one element at a time

```
for (i=0; i<nrow; i++)
```

```
    for (j=0; j<ncol; j++)
```

```
        scanf ("%f", &a[i][j]);
```

- The ampersand (&) is necessary
- The elements can be entered all in one line or in different lines

How to print the elements of a 2-d array?

- By printing them one element at a time

```
for (i=0; i<nrow; i++)  
    for (j=0; j<ncol; j++)  
        printf ("\n %f", a[i][j]);
```

- The elements are printed one per line

```
for (i=0; i<nrow; i++)  
    for (j=0; j<ncol; j++)  
        printf ("%f", a[i][j]);
```

- The elements are all printed on the same line₁₂

Contd.

```
for (i=0; i<nrow; i++)  
{  
    printf (“\n”);  
    for (j=0; j<ncol; j++)  
        printf (“%f  ”, a[i][j]);  
}
```

- The elements are printed nicely in matrix form

Example: Matrix Addition

```
int main()
{
    int a[100][100], b[100][100],
        c[100][100], p, q, m, n;

    scanf ("%d %d", &m, &n);

    for (p=0; p<m; p++)
        for (q=0; q<n; q++)
            scanf ("%d", &a[p][q]);

    for (p=0; p<m; p++)
        for (q=0; q<n; q++)
            scanf ("%d", &b[p][q]);
```

```
    for (p=0; p<m; p++)
        for (q=0; q<n; q++)
            c[p][q] = a[p][q] + b[p][q];

    for (p=0; p<m; p++)
    {
        printf ("\n");
        for (q=0; q<n; q++)
            printf ("%d  ", c[p][q]);
    }
    return 0;
}
```

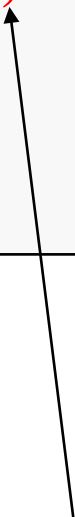

Passing 2-d Arrays as Parameters

- Similar to that for 1-D arrays
 - The array contents are not copied into the function
 - Rather, the address of the first element is passed
- For calculating the address of an element in a 2-d array, we need:
 - The starting address of the array in memory
 - Number of bytes per element
 - Number of columns in the array
- The above three pieces of information must be known to the function

Example Usage

```
int main()
{
    int a[15][25], b[15][25];
    :
    :
    add (a, b, 15, 25);
    :
}
```

```
void add (int x[][25], int
y[][25], int rows, int cols)
{
    :
}
```



We can also write

```
int x[15][25], y[15][25];
```

**But at least 2nd dimension
must be given**

Dynamic Allocation of 2-d Arrays

- Recall that address of $[i][j]$ -th element is found by first finding the address of first element of i -th row, then adding j to it
- Now think of a 2-d array of dimension $[M][N]$ as M 1-d arrays, each with N elements, such that the starting address of the M arrays are contiguous (so the starting address of k -th row can be found by adding 1 to the starting address of $(k-1)$ -th row)
- This is done by allocating an array p of M pointers, the pointer $p[k]$ to store the starting address of the k -th row

Contd.

- Now, allocate the M arrays, each of N elements, with $p[k]$ holding the pointer for the k-th row array
- Now p can be subscripted and used as a 2-d array
- Address of $p[i][j] = *(p+i) + j$ (note that $*(p+i)$ is a pointer itself, and p is a pointer to a pointer)

Dynamic Allocation of 2-d Arrays

```
int **allocate (int h, int w)
```

```
{
```

```
    int **p;
```

```
    int i, j;
```

**Allocate array
of pointers**



```
    p = (int **) malloc(h * sizeof (int *));
```

```
    for (i=0; i<h; i++)
```

```
        p[i] = (int *) malloc(w * sizeof (int));
```

```
    return(p);
```

```
}
```

**Allocate array of
integers for each
row**

```
void read_data (int **p, int h, int w)
```

```
{
```

```
    int i, j;
```

```
    for (i=0; i<h; i++)
```

```
        for (j=0; j<w; j++)
```

```
            scanf ("%d", &p[i][j]);
```

```
}
```

**Elements accessed
like 2-D array elements.**

Contd.

```
void print_data (int **p, int h, int w)
{
    int i, j;
    for (i=0;i<h;i++)
    {
        for (j=0;j<w;j++)
            printf ("%5d ", p[i][j]);
        printf ("\n");
    }
}
```

```
int main()
{
    int **p;
    int M, N;
    printf ("Give M and N \n");
    scanf ("%d%d", &M, &N);
    p = allocate (M, N);
    read_data (p, M, N);
    printf ("\nThe array read as \n");
    print_data (p, M, N);
    return 0;
}
```


Contd.

```
void print_data (int **p, int h, int w)
{
    int i, j;
    for (i=0;i<h;i++)
    {
        for (j=0;j<w;j++)
            printf ("%5d ", p[i][j]);
        printf ("\n");
    }
}
```

```
int main()
{
    int **p;
    int M, N;
    printf ("Give M and N \n");
    scanf ("%d%d", &M, &N);
    p = allocate (M, N);
    read_data (p, M, N);
    printf ("\nThe array read as \n");
    print_data (p, M, N);
    return 0;
}
```

Give M and N

3 3

1 2 3

4 5 6

7 8 9

The array read as

1 2 3

4 5 6

7 8 9

Memory Layout in Dynamic Allocation

```
int main()
{
    int **p;
    int M, N;
    printf ("Give M and N \n");
    scanf ("%d%d", &M, &N);
    p = allocate (M, N);
    for (i=0;i<M;i++) {
        for (j=0;j<N;j++)
            printf ("%10d", &p[i][j]);
        printf("\n");
    }
    return 0;
}
```

```
int **allocate (int h, int w)
{
    int **p;
    int i, j;

    p = (int **)malloc(h*sizeof (int *));
    for (i=0; i<h; i++)
        printf ("%10d", &p[i]);
    printf("\n\n");
    for (i=0; i<h; i++)
        p[i] = (int *)malloc(w*sizeof(int));
    return(p);
}
```


Output

3 3

31535120 31535128 31535136

31535152 31535156 31535160

31535184 31535188 31535192

31535216 31535220 31535224

Starting address of each row, contiguous (pointers are 8 bytes long)

Elements in each row are contiguous