CS13002 Programming and Data Structures, Spring 2006

Class test 2

1.

Total points: 30		March 30, 2006		Total time: 1 hour
Roll no: _	05FB1331	Name:	Foolan Barik	Section:@
-	rs must fit in the	respective spaces [self. You may use extra blank shorovided. Not all blanks carry equations of your solutions. Answer	qual marks. Evaluation will
Let $\omega = \sqrt[3]{2}$	3/2 be the real cu	be root of 2. Cons	ider the set	
A =	$= \{a + b\omega + c\omega^2\}$	$\mid a,b,c$ are intege	rs}	
the sum, c	lifference and pr	coduct of $a_1 + b_1 \omega$	is closed under addition, subtraction $c_1 + c_1\omega^2$, $a_2 + b_2\omega + c_2\omega^2 \in A$ $c_1(a_2 + b_2\omega + c_2\omega^2) = (a_1 \pm a_2)$	can be expressed in the form
ω of degre	e 4. Then use th		$+b_1\omega + c_1\omega^2$ and $a_2 + b_2\omega + c_2$ d $\omega^4 = 2\omega$ in order to reduce this	
=	$(a_1a_2) + (a_1b_1)$ $(a_1a_2) + (a_1b_1)$	$b_2 + a_2 b_1)\omega + (a_1$	$c_{2}\omega^{2})$ $c_{2} + b_{1}b_{2} + a_{2}c_{1})\omega^{2} + (b_{1}c_{2} + c_{2} + b_{1}b_{2} + a_{2}c_{1})\omega^{2} + (b_{1}c_{2} + c_{2} + a_{2}b_{1} + 2c_{1}c_{2})\omega + (a_{1}c_{2} + b_{2} + a_{2}b_{1} + 2c_{1}c_{2})\omega + (a_{1}c_{2} + b_{2} + a_{2}b_{1} + a_{2}$	$b_2c_1)\times 2+(c_1c_2)\times (2\omega)$
Represent	an element of A	by a structure of t	hree integers:	
i	def struct { .nt a,b,c; /* bicNumber;	•	$+b\omega+c\omega^2\in A$ */	
Complete	the following fur	nction that takes tw	o cubic numbers x1 , x2 as argun	nents and returns their product. (8)
cubi {	cNumber cubi	icProd (cubio	cNumber x1, cubicNumber	x2)
_	cu	nbicNumber x;	/* local var	iable */
_	<u>x.a</u> = <u>(x</u>	:1.a) * (x2.a)	+ 2 * (x1.b) * (x2.c) +	+ 2 * (x2.b) * (x1.c);
_	x.b =	(x1.a) * (x2.	b) + (x2.a) * (x1.b) + 2	2 * (x1.c) * (x2.c) ;
_	x.c =	(x1.a) * (x	2.c) + (x1.b) * (x2.b) +	+ (x2.a) * (x1.c) ;
}		return x;		
J				

2. A house has n rooms numbered $0, 1, \ldots, n-1$. Consider the $n \times n$ matrix M. The i, j-th entry of M is 1 if there is a door between room i and room j; it is 0 otherwise. Given two rooms u, v, the following function finds out whether there exists a way to go from room u to room v using the doors. The function works as follows. It maintains two arrays visited[] and toExplore[]. To start with, room u is marked as visited and is also inserted in the array toExplore[]. Then we enter a loop. We first check if there are some more rooms to explore. Let i be one such room. We find out all unvisited rooms j sharing doors with room i. We mark all these rooms j as visited and also insert them in the array toExplore[]. A good way to handle elements of the array toExplore[] is to insert elements at the end (of the current list of rooms to explore) and consider the rooms from beginning to end for further exploration. We maintain two indices start and end. The rooms yet to be explored lie in the indices start, ..., end in toExplore[]. Complete the following function to solve this connectivity problem.

```
int connected ( int M[MAXDIM][MAXDIM], int n, int u, int v )
{
  int *visited, *toExplore, i, j, start, end;
   /* Allocate memory for n integers to each of visited and toExphe */
  visited
                 (int *)malloc(n * sizeof(int))
  toExplore = (int *)malloc(n * sizeof(int))
   for (i=0; i<n; ++i) visited[i] = 0; # Initialize the array visited*/
                            _____; /* Mark room u as visited*/
  visited[u] = _____
                        1
   /* Insert room u in the array toExplore*/
  toExplore[0] = u; start = end = 0;
   /* As long as there are more rooms to explore*/
  while ( _____start <= end
     i = toExplore[start]; ++start;
     /* if i is the destination room v, return true*/
     if ( i == v ) return 1;
     /* Check all rooms j sharing doors with room i*/
     for (j=0; j<n; ++j) {
        /* if there is a door between i and j, and j is not visited*/
                 /* Mark j as visited */
                               visited[j] = 1;
           /* Insert j in toExplore[] and adjust the insertion index/
                            toExplore[++end] = j;
        }
     }
   /* Loop ends. Room v could not be reached from room u.*/
   /* Free allocated memory*/
             visited ____); free( toExplore );
   free(
   /* Return failure */
              return 0;
}
```