Topic Models

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CSE, IITKGP

October 13-14, 2014

Why Topic Modeling?

Information Overload

As more information becomes available, it becomes more difficult to find and discover what we need.

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Topic Modeling

Provides methods for automatically organizing, understanding, searching and summarizing large electronic archives

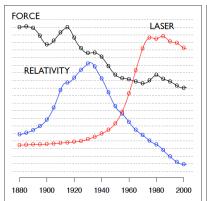
- Discover the hidden themes that pervade the collection
- Annotate the documents according to those themes
- Use annotations to organize, summarize, and search the texts

Applications: Discover Topics from a corpus

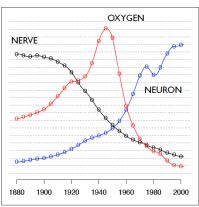
human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	$\operatorname{control}$	model
map	living	infectious	parallel
information	diversity	$_{ m malaria}$	methods
genetics	group	parasite	networks
mapping	new	parasites	software
$\operatorname{project}$	two	united	new
sequences	common	tuberculosis	simulations

Applications: Model the evolution of topics over time

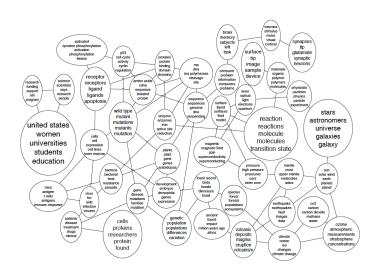




"Neuroscience"

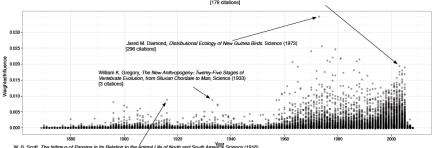


Applications: Model connections between topics



Applications: Discover influential articles



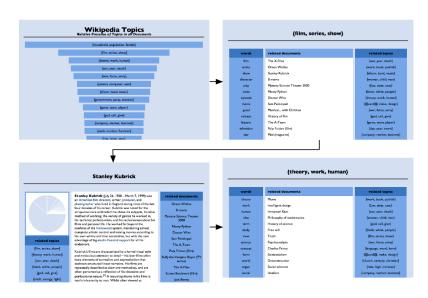


W. B. Scott, The Isthmus of Panama in Its Relation to the Animal Life of North and South America, Science (1916) [3 citations]

Link Prediction using Relational Topic Models

Markov chain Monte Carlo convergence diagnostics: A comparative review	
Minorization conditions and convergence rates for Markov chain Monte Carlo	
Rates of convergence of the Hastings and Metropolis algorithms	
Possible biases induced by MCMC convergence diagnostics	_ <u>R</u>
Bounding convergence time of the Gibbs sampler in Bayesian image restoration	
Self regenerative Markov chain Monte Carlo	RTM (ψ_e)
Auxiliary variable methods for Markov chain Monte Carlo with applications	
Rate of Convergence of the Gibbs Sampler by Gaussian Approximation	
Diagnosing convergence of Markov chain Monte Carlo algorithms	
Exact Bound for the Convergence of Metropolis Chains	
Self regenerative Markov chain Monte Carlo	LDA
Minorization conditions and convergence rates for Markov chain Monte Carlo	
Gibbs-markov models	+
Auxiliary variable methods for Markov chain Monte Carlo with applications	Re
Markov Chain Monte Carlo Model Determination for Hierarchical and Graphical Models	100
Mediating instrumental variables	Regression
A qualitative framework for probabilistic inference	ior
Adaptation for Self Regenerative MCMC	_

Applications: Organize and browse large corpora



Seeking Life's Bare (Genetic) Necessities

COLD SPRING HARBOR, NEW YORK-How many genes does an organism need to survive? Last week at the genome meeting here,* two genome researchers with radically different approaches presented complementary views of the basic genes needed for life. One research team, using computer analyses to compare known genomes, concluded that today's organisms can be sustained with just 250 genes, and that the earliest life forms required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job-but that anything short of 100 wouldn't be enough. Genes

Although the numbers don't match precisely, those predictions * Genome Mapping and Sequenc-

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May 8 to 12.

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Stripping down. Computer analysis yields an estimate of the minimum modern and ancient genomes

SCIENCE • VOL. 272 • 24 MAY 1996

This articles is about using data analysis to determine the number of genes an organism needs to survive

233 genes

[&]quot;are not all that far apart," especially in comparison to the 75,000 genes in the human genome, notes Siv Andersson of Uppsala University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely mapped and sequenced. "It may be a way of organizing any newly sequenced genome," explains Arcady Mushegian, a computational mo-

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Highlighted words: 'blue': data analysis, 'pink': evolutionary biology, 'yellow': aenetics

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The article blends genetics, data analysis and evolutionary biology in different proportions

Genes

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Knowing that this article blends those topics would help situate it in a collection of scientific articles

Genes

Topic Model: Basic Idea

A generative statistical model that captures this intuition.

Generative Model

Documents are mixture of topics, where a topic is a probability distribution over words.

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genetics topic has words about genetics with high probability and the *evolutionary biology* topic has words about evolutionary biology with high probability.

Topic Model: Basic Idea

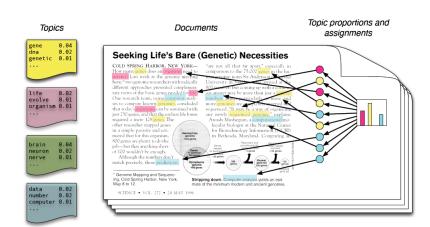
A generative statistical model that captures this intuition.

Generative Model

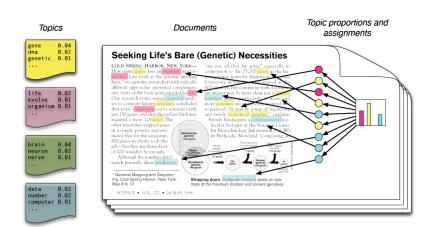
Documents are mixture of topics, where a topic is a probability distribution over words.

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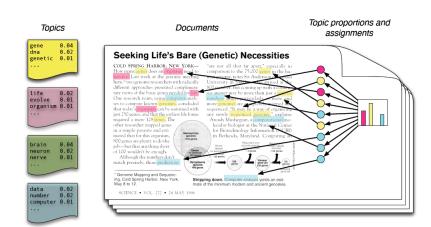
Technically, the generative model assumes that the topics are generated first, before the documents.



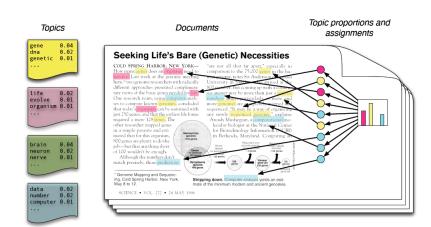
- Each topic is a distribution over words
- Each document is a mixture of corpus-wide topics
- Each word is drawn from one of those topics



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What does the statistical model reflect?

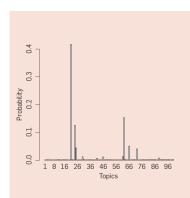
- All the document in the collection share the same set of topics, but each document exhibits those topics in different proportions
- Each word in each document is drawn from one of the topics, where the selected topic is chosen from the per-document distribution over topics

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- All the document in the collection share the same set of topics, but each document exhibits those topics in different proportions
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In the example article, the distribution over topics would place probability on *genetics*, *data analytics* and *evolutionary biology*, and each word is drawn from one of those three topics.

Real Inference with LDA for the example article



"Genetics" human genome dna aenetic genes sequence gene molecular sequencing map information genetics mapping project seauences

"Evolution"
evolution
evolutionary
species
organisms
life
origin
biology
groups
phylogenetic
living
diversity
group
new
two

common

"Disease"
disease
host
bacteria
diseases
resistance
bacterial
new
strains
control
infectious
malaria
parasite
parasites

united

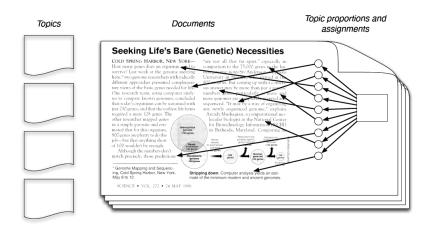
tuberculosis

"Computers" computer models information data computers system network systems model parallel methods networks software new simulations

Central Problem of LDA

- The documents themselves are observed, while the topic structure the topics, per-document topic distributions, and the per-document per-word topic assignments - is hidden structure.
- The central computational problem is to use the observed documents to infer the hidden topic structure, i.e. *reversing* the generative process.

Goal: The posterior distribution



Infer the hidden variables

Compute their distribution conditioned on the documents

37,000 text passages from educational materials (300 topics)

Topic 247

Topic 5

Topic 43

word	prob.
DRUGS	.069
DRUG	.060
MEDICINE	.027
EFFECTS	.026
BODY	.023
MEDICINES	.019
PAIN	.016
PERSON	.016
MARIJUANA	.014
LABEL	.012
ALCOHOL	.012
DANGEROUS	.011
ABUSE	.009
EFFECT	.009
KNOWN	.008
PILLS	.008

word	prob.
RED	.202
BLUE	.099
GREEN	.096
YELLOW	.073
WHITE	.048
COLOR	.048
BRIGHT	.030
COLORS	.029
ORANGE	.027
BROWN	.027
PINK	.017
LOOK	.017
BLACK	.016
PURPLE	.015
CROSS	.011
COLORED	.009
<u> </u>	

word	prob.
MIND	.081
THOUGHT	.066
REMEMBER	.064
MEMORY	.037
THINKING	.030
PROFESSOR	.028
FELT	.025
REMEMBERED	.022
THOUGHTS	.020
FORGOTTEN	.020
MOMENT	.020
THINK	.019
THING	.016
WONDER	.014
FORGET	.012
RECALL	.012

word	prob.
DOCTOR	.074
DR.	.063
PATIENT	.061
HOSPITAL	.049
CARE	.046
MEDICAL	.042
NURSE	.031
PATIENTS	.029
DOCTORS	.028
HEALTH	.025
MEDICINE	.017
NURSING	.017
DENTAL	.015
NURSES	.013
PHYSICIAN	.012
HOSPITALS	.011

Documents with different content can be generated by choosing different distributions over topics.

• Equal probability to first two topics:

Documents with different content can be generated by choosing different distributions over topics.

- Equal probability to first two topics: about a person who has taken too many drugs and how that affected color perceptions.
- Equal probability to the last two topics:

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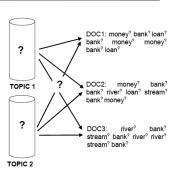
- Equal probability to first two topics: about a person who has taken too many drugs and how that affected color perceptions.
- Equal probability to the last two topics: about a person who experienced a loss of memory, which required a visit to the doctor.

Generative model and statistical inference

PROBABILISTIC GENERATIVE PROCESS

TOPIC 1 DOC1: money¹ bank¹ loan¹ bank¹ loan¹ bank¹ loan¹ bank¹ loan¹ DOC2: money¹ bank¹ DOC2: money¹ bank¹ DOC2: money¹ bank¹ bank² river² loan¹ stream² bank¹ money¹ DOC3: river² bank² stream² bank² river² river² stream² bank² river² bank²

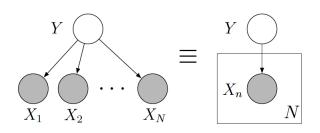
STATISTICAL INFERENCE



Important points

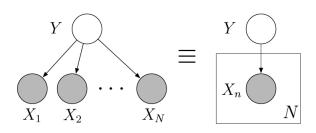
- bag-of-words assumption: The generative process does not make any assumptions about the order of words in the documents.
- capturing polysemy: The way that the model is defined, there is no notion
 of mutual exclusivity that restricts words to be part of one topic only. Ex:
 both 'money' and 'river' topics can give high probability to the word 'bank'.

Graphical Model (Notation)



- Nodes are random variables
- Edges denote possible dependence
- Observed variables are shaded
- Plates denote replicated structure

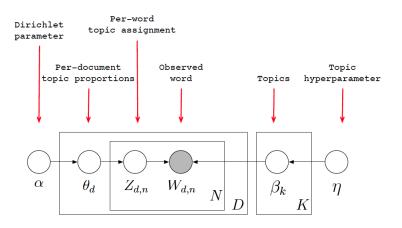
Graphical Model (Notation)



- Structure of the graph defines the pattern of conditional dependence between the ensemble of random variables
- E.g., this graph corresponds to

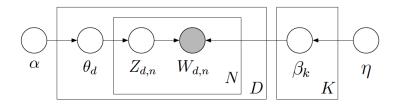
$$p(y,x_1,...,x_N) = p(y) \prod_{n=1}^{N} p(x_n|y)$$

LDA: Graphical Model



Each piece of the structure is a random variable.

Latent Dirichlet Allocation: Generative Model



- 1 Draw each topic $\beta_i \sim \text{Dir}(\eta)$, for $i \in \{1, ..., K\}$.
- 2 For each document:
 - **1** Draw topic proportions $\theta_d \sim \text{Dir}(\alpha)$.
 - 2 For each word:
 - **1** Draw $Z_{d,n} \sim \text{Mult}(\theta_d)$.
 - 2 Draw $W_{d,n} \sim \text{Mult}(\beta_{Z_{d,n}})$.

What is Latent Dirichlet Allocation (LDA)?

- 'Latent' has the same sense in LDA as in Latent semantic indexing, i.e. capturing topics as latent variables
- The distribution that is used to draw the per-document topic distributions is called a *Dirichlet distribution*. This result is used to allocate the words of the documents to different topics.

What is Latent Dirichlet Allocation (LDA)?

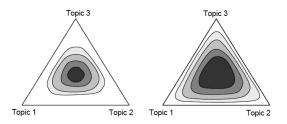
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Dirichlet Distribution

The Dirichlet distribution is an exponential family distribution over the simplex, i.e. positive vectors that sum to one

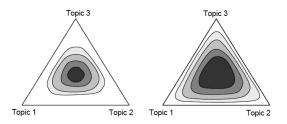
$$p(\theta \mid \vec{\alpha}) = \frac{\Gamma(\sum_{i} \alpha_{i})}{\prod_{i} \Gamma(\alpha_{i})} \prod_{i} \theta_{i}^{\alpha_{i}-1}$$

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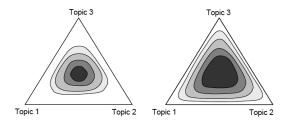
 α_i s: hyper-parameters of the model which can be interpreted as: α_j can be interpreted as an observation count for the number of times topic j is sampled in a document

$$p(\theta \mid \vec{\alpha}) = \frac{\Gamma(\sum_{i} \alpha_{i})}{\prod_{i} \Gamma(\alpha_{i})} \prod_{i} \theta_{i}^{\alpha_{i}-1}$$



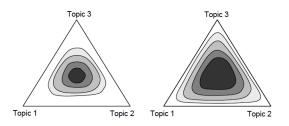
 α_i s: hyper-parameters of the model which can be interpreted as: These priors can be interpreted as forces in the topic distributions with higher α moving the topics away from the corners of the simplex

$$p(\theta \mid \vec{\alpha}) = \frac{\Gamma(\sum_{i} \alpha_{i})}{\prod_{i} \Gamma(\alpha_{i})} \prod_{i} \theta_{i}^{\alpha_{i} - 1}$$

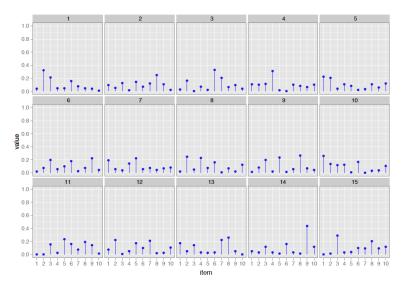


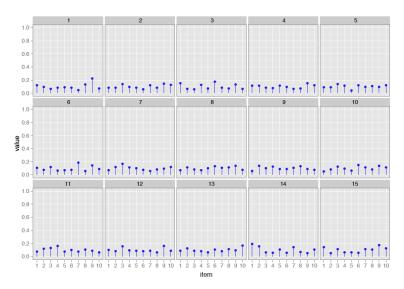
 α_i s: hyper-parameters of the model which can be interpreted as: When $\alpha < 1$, there is a bias to pick topic distributions favoring just a few topics

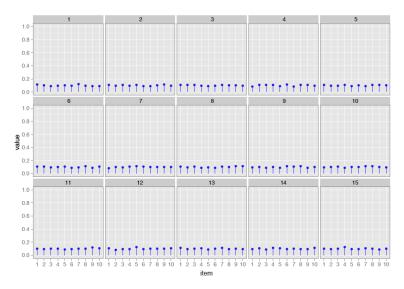
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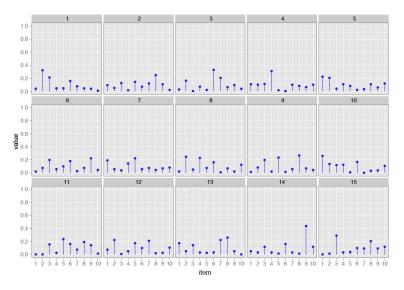


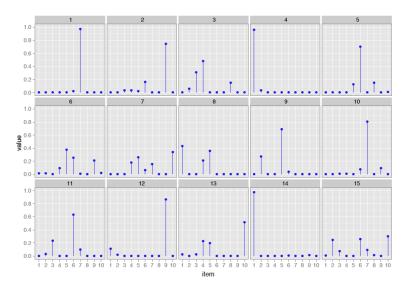
 α_i s: hyper-parameters of the model which can be interpreted as: It is convenient to use a symmetirc Dirichlet distribution with a single hyper-parameter $\alpha_1=\alpha_2\ldots=\alpha$

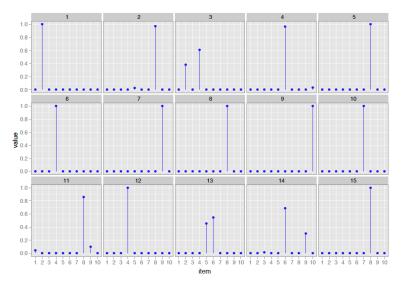


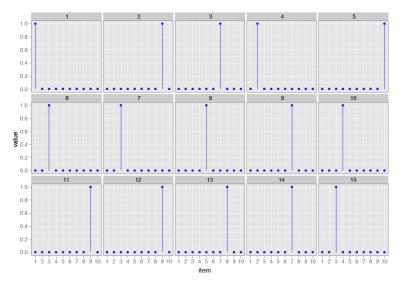












Online Implementations

LDA-C* A C implementation of LDA

HDP* A C implementation of the HDP ("infinite LDA") **Online LDA*** A python package for LDA on massive data

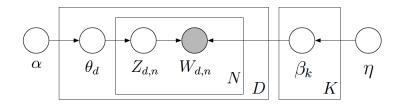
LDA in R* Package in R for many topic models

LingPipe Java toolkit for NLP and computational linguistics

Mallet Java toolkit for statistical NLP

TMVE* A python package to build browsers from topic models

Latent Dirichlet Allocation: Statistical Inference



- From a collection of documents, infer
 - Per-word topic assignment z_{d,n}
 - Per-document topic proportions θ_d
 - Per-corpus topic distributions β_k
- Use posterior expectations to perform the task at hand, e.g., information retrieval, document similarity, etc.

LDA: computing posterior

Joint distribution of the hidden and observed variables

$$p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})$$

$$= \prod_{i=1}^{K} p(\beta_i) \prod_{d=1}^{D} p(\theta_d)$$

$$\left(\prod_{n=1}^{N} p(z_{d,n} | \theta_d) p(w_{d,n} | \beta_{1:K}, z_{d,n}) \right)$$

LDA: computing posterior

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$$\left(\prod_{n=1}^{N} p(z_{d,n} | \theta_d) p(w_{d,n} | \beta_{1:K}, z_{d,n}) \right)$$

What is posterior?

Conditional distribution of the hidden variables given the observed variables

$$p(\beta_{1:K}, \theta_{1:D}, z_{1:D} | w_{1:D}) = \frac{p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})}{p(w_{1:D})}$$

Computing Posterior

$$p(\beta_{1:K}, \theta_{1:D}, z_{1:D} | w_{1:D}) = \frac{p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})}{p(w_{1:D})}$$

- Numerator is the joint distribution of all the random variables, which can be easily computed for any settings of the hidden variables
- Denominator is the marginal probability of the observations, probability of seeing the observed corpus under any topic model

Computing Posterior

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This marginal is intractable to compute!

The sum is over all possible ways of assigning each observed word of the collection to one of the topics. Number of words can be of the order of millions!!

Can we approximate it?

Algorithms to approximate it fall in two categories:

Sampling-based Algorithms

Collect samples from the posterior to approximate it with an empirical distribution

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Variational Methods

- Deterministic alternative to sampling-based algorithms
- The inference problem is transformed to an optimization problem

- A form of Markov chain Monte Carlo (MCMC), which simulates a high-dimensional distribution by sampling on lower-dimensional subset of variables where each subset is conditioned on the value of all others
- Sampling is done sequentially and proceeds until the sampled values approximate the target distribution
- It directly estimates the posterior distribution over z , and uses this to provide estimates for β and θ

- Suppose we have a word token i for which we want to find the topic assignment probability : $p(z_i = j)$
- Represent the collection of documents by a set of word indices w_i and document indices d_i for this token i
- Gibbs sampling considers each word token in turn and estimates the probability of assigning the current word token to each topic, conditioned on the topic assignment to all other word tokens
- From this conditional distribution, a topic is sampled and stored as the new topic assignment for this word token
- This conditional is written as $P(z_i = j | z_{-i}, w_i, d_i, .)$

- Let us define two matrices C^{WT} and C^{DT} of dimensions $W \times T$ and $D \times T$ respectively.
- C_{wj}^{WT} contains the number of times word w is assigned to topic j, not including the current instance
- C_{dj}^{WT} contains the number of times topic j is assigned to some word token in document d, not including the current instance

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- C_{wj}^{WT} contains the number of times word w is assigned to topic j, not including the current instance
- C_{dj}^{WT} contains the number of times topic j is assigned to some word token in document d, not including the current instance

$$P(z_{i} = j | z_{-i}, w_{i}, d_{i}, .) \propto \frac{C_{w,j}^{WT} + \eta}{\sum_{w=1}^{W} C_{w,j}^{WT} + W\eta} \frac{C_{d,j}^{DT} + \alpha}{\sum_{t=1}^{T} C_{d,j}^{DT} + T\alpha}$$

- The left part is the probability of word w under topic j (How likely a word is for a topic) whereas
- the right part is the probability of topic *j* under the current topic distribution for document *d* (How dominant a topic is in a document)

Algorithm

- Start: Each word token is assigned to a random topic in $[1 \dots T]$
- For each word token, a new topic is sampled as per $P(z_i = j | z_{-i}, w_i, d_i, .)$, adjusting the matrices C^{WT} and C^{DT}
- A single pass through all word tokens in the document is one Gibbs sample
- After the burnin period, these samples are saved at regularly spaced intervals, to prevent correlations between samples

Estimating θ and β

$$\beta_i^{(j)} = \frac{C_{ij}^{WT} + \eta}{\sum_{k=1}^{W} C_{kj}^{WT} + W\eta}$$

$$\theta_{j}^{(d)} = \frac{C_{dj}^{DT} + \alpha}{\displaystyle\sum_{k=1}^{T} C_{dk}^{DT} + T\alpha}$$

These values correspond to predictive distributions of

- \bullet sampling a new token of word i from topic j, and
- samping a new token in document d from topic j

An Example

The algorithm can be illustrated by generating artificial data from a known topic model and applying the algorithm to check whether it is able to infer the original genrative structure.

Example

 Let topic 1 give equal probability to MONEY, LOAN, BANK and topic 2 give equal probability to words RIVER, STREAM, and BANK

$$\beta_{MONEY}^{(1)} = \beta_{LOAN}^{(1)} = \beta_{BANK}^{(1)} = 1/3$$

$$\beta_{RIVER}^{(2)} = \beta_{STREAM}^{(2)} = \beta_{BANK}^{(2)} = 1/3$$

We generate 16 documents by arbitrarily mixing two topics.

Initial Structure

	River	Stream	Bank	Money	Loan
8 9 10 11 12 13	○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○ ○	Stream	OCO OCO	000000000000000000000000000000000000	Company Comp

Colors reflect initial random assignment, black = topic 1, while = topic 2

After 64 iterations of Gibbs Sampling

	River	Stream	Bank	Money	Loan
12345678901123	0 0 0 0 00 00 00 000	00 000 000 000 000 000000	00000 00000 000000 000000 000000 00000 0000	Money	Loan
14 15	0000	0000000	000000	 	:
16	00000	0000000	0000	 	į l

$$\beta_{MONEY}^{(1)} = 0.32, \beta_{LOAN}^{(1)} = 0.29, \beta_{BANK}^{(1)} = 0.39$$

$$\beta_{RIVER}^{(2)} = 0.25, \beta_{STREAM}^{(2)} = 0.4, \beta_{BANK}^{(2)} = 0.35$$

Computing Similarities

Document Similarity

Similarity between documents d_i and d_2 can be measured by the similarity between their topic distributions $\theta^{(d_1)}$ and $\theta^{(d_2)}$

KL divergence :
$$D(p,q) = \sum_{j=1}^{T} p_j log_2 \frac{p_j}{q_j}$$

Symmetrized KL divergence: $\frac{1}{2}[D(p,q)+D(q,p)]$ seems to work well

Similarity with respect to query q

Maximize the conditional probability of query given the document:

$$p(q|d_i) = \prod_{w_k \in q} p(w_k|d_i)$$

$$= \prod_{w_k \in q} \sum_{i=1}^{T} P(w_k | z = j) P(z = j | d_i)$$

Computing Similarities

Similarity between two words

Having observed a single word in a new context, what are the other words that might appear in the same context, based on the topic interpretation for the observed word?

$$p(w_2|w_1) = \sum_{j=1}^{T} p(w_2|z=j)p(z=j|w_i)$$

Example

Observed and predicted responses for the word 'PLAY'

.036 .024 .016 .011 .010 .009 .009 .008 .008 .007 .007

HUMANS	TOPIC

HUMANS		TOFICS
FUN	.141	BAL
BALL	.134	GAM
GAME	.074	CHILDRE
WORK	.067	TEAN
GROUND	.060	WAN
MATE	.027	MUSI
CHILD	.020	SHOV
ENJOY	.020	HI
WIN	.020	CHILI
ACTOR	.013	BASEBAL
FIGHT	.013	GAME
HORSE	.013	FUI
KID	.013	STAG
MUSIC	.013	FIELI

Modeling Science

Data

The OCR'ed collection of Science from 1990-2000

- 17K documents
- 11M words
- 20K unique terms (stop words and rare words removed)

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Model

100-topic model using variational inference

Example Inference

Seeking Life's Bare (Genetic) Necessities

COLD SPRING HARBOR, NEW YORK—
How many gene soles an organism need to
survive? List week at the genome meeting
here, "two genome researchers with radically
different approaches presented complementary views of the basic genes needed for life.
One research team, using computer analyses to compare known genomes, concluded
that today's organisms can be sustained with
put 252 genes, and that the earliest life forms
required a mere 128 genes. The
other researcher mapped genes

other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough.

of 100 wouldn't be enough.
Although the numbers don't
match precisely, those predictions
*Genome Mapping and Sequenc-

ing, Cold Spring Harbor, New York,

May 8 to 12

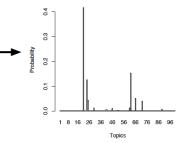
"are not all that far apart," especially un comparison to the 75,002 genes in the human genome, notes Six Andersson of Urgisals University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely unapped and sequenced. "It may be a way of organizing up newly sequenced genome," explains

Arcady Mushegian, a computational molecular biologist at the National Center for Biotechnology Information (NCBI) in Bethesda, Maryland, Comparing an

in Bethesda, Maryland. Comparing an order of the comparing and order of the

Stripping down. Computer analysis yields an estimate of the minimum modern and ancient genomes.

SCIENCE • VOL. 272 • 24 MAY 1996



Example Topics

human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	$\operatorname{control}$	model
$_{\mathrm{map}}$	living	infectious	parallel
information	diversity	$_{ m malaria}$	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations

Modeling Richer Assumptions in Topic Models

- Correlated topic models
- Dynamic topic models
- Measuring scholarly impact

Correlated Topic Models

- The Dirichlet is an exponential family distribution on the simplex, positive vectors that sum to one
- However, the near independence of components makes it a poor choice for modeling topic proportions
- An article about fossil fuels is more likely to also be about geology than about genetics

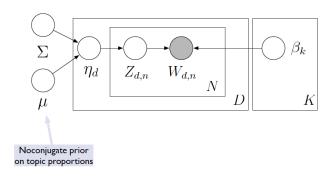
Using logistic normal distribution

A multivariate normal distribution of a k-dimensional vector $x = [X_1, X_2, \dots, X_k]$ can be written as

$$x \sim N_k(\mu, \Sigma)$$

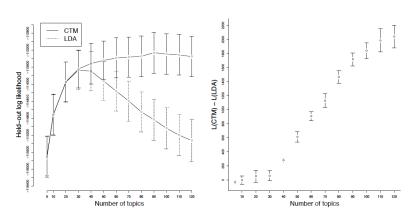
with k-dimensional mean vector μ and $k \times k$ covariance matrix Σ

Correlated Topic Model (CTM)



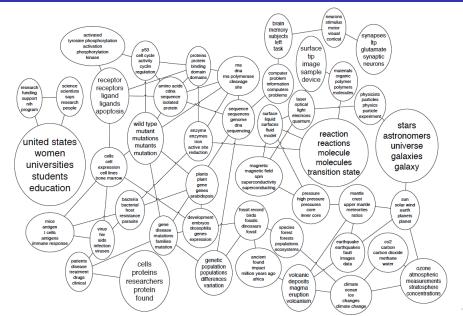
- Draw topic proportions from a logistic normal, where topic occurrences can exhibit correlation.
- Use for:
 - Providing a "map" of topics and how they are related
 - Better prediction via correlated topics

CTM supports more topics and provides a better fit than LDA



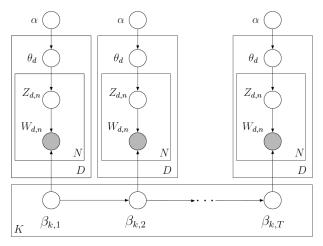
Held-out log probability on Science

Correlated Topics



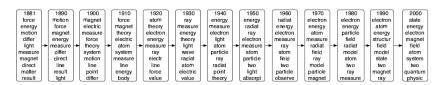
LDA assumption

- LDA assumes that the order of documents does not matter
- Not appropriate for corpora that span hundreds of years
- We might want to track how language changes over time

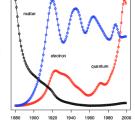


Topics drifting in time

$$\beta_{k,t}|\beta_{k,t-1} \sim N(\beta_{k,t-1},\sigma^2 I)$$



"Atomic Physics"



1881 On Matter as a form of Energy

1892 Non-Euclidean Geometry

1900 On Kathode Rays and Some Related Phenomena

1917 "Keep Your Eye on the Ball"

1920 The Arrangement of Atoms in Some Common Metals

1933 Studies in Nuclear Physics 1943 Aristotle, Newton, Einstein, II

1943 Anstolie, Newton, Einstein. II

1950 Instrumentation for Radioactivity

1965 Lasers

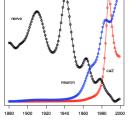
1975 Particle Physics: Evidence for Magnetic Monopole Obtained

1985 Fermilab Tests its Antiproton Factory

1999 Quantum Computing with Electrons Floating on Liquid Helium



"Neuroscience"



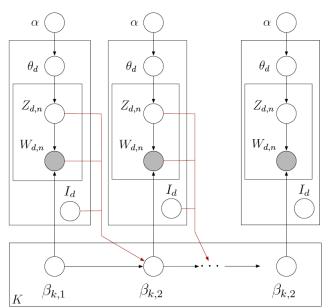
- 1887 Mental Science
- 1900 Hemianopsia in Migraine
- 1912 A Defence of the "New Phrenology"
- 1921 The Synchronal Flashing of Fireflies
- 1932 Myoesthesis and Imageless Thought
- 1943 Acetylcholine and the Physiology of the Nervous System
- 1952 Brain Waves and Unit Discharge in Cerebral Cortex
- 1963 Errorless Discrimination Learning in the Pigeon
- 1974 Temporal Summation of Light by a Vertebrate Visual Receptor
- 1983 Hysteresis in the Force-Calcium Relation in Muscle
- 1993 GABA-Activated Chloride Channels in Secretory Nerve Endings

Measuring Scholarly Impact

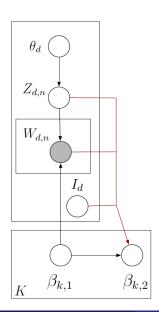
How to model influence?

- Idea from Dynamic Topic Models, influential articles reflect future changes in language use
- The influence of an article is a latent variable
- Inflential articles affect the drift of the topics that they discuss
- The posterior gives a retrospective estimate of influential article

Measuring Scholarly Impact

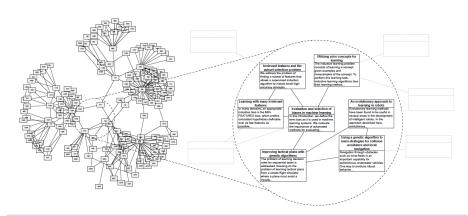


Measuring Scholarly Impact



- Each document has an influence score I_d.
- Each topic drifts in a way that is biased towards the documents with high influence.
- The posterior of I_{1:D} can be examined to retrospectively find articles that best explain future changes in language.

Relational Topic Models



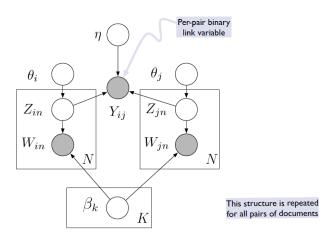
Connected Observations

- Citation networks of documents
- Hyperlinked networks of web-pages
- Friend-connected social network profiles

Relational Topic Models

- LDA needs to be adapted to a model of content and connection
- RTMs find hidden structure in both types of data

Relational Topic Models



Works in a supervised framework, allowing predictions about new and unlinked data

Link Prediction Task using RTM

Given a new document, which documents is it likely to link to?

Markov chain Monte Carlo convergence diagnostics: A comparative review

Minorization conditions and convergence rates for Markov chain Monte Carlo Rates of convergence of the Hastings and Metropolis algorithms

Possible biases induced by MCMC convergence diagnostics

Bounding convergence time of the Gibbs sampler in Bayesian image restoration Self regenerative Markov chain Monte Carlo

Auxiliary variable methods for Markov chain Monte Carlo with applications

Rate of Convergence of the Gibbs Sampler by Gaussian Approximation

Diagnosing convergence of Markov chain Monte Carlo algorithms

RTM allows for such predictions

- links given the new words of a document
- words given the links of a new document

Supervised settings of LDA

Use data points paired with response variables

- User reviews paired with a number of stars
- Web pages paired with a number of likes
- Documents paired with links to other documents
- Images paired with a category

Supervised settings of LDA

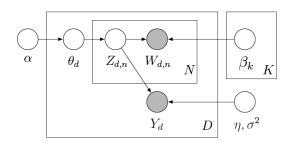
Use data points paired with response variables

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Supervised topic modes

are topic models of documents and responses, fit to find topics predictive of the response

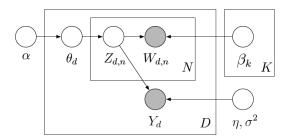
Supervised LDA



- **1** Draw topic proportions $\theta \mid \alpha \sim \text{Dir}(\alpha)$.
- For each word
 - Draw topic assignment $z_n \mid \theta \sim \text{Mult}(\theta)$.
 - Draw word $w_n \mid z_n, \beta_{1:K} \sim \text{Mult}(\beta_{z_n})$.
- ③ Draw response variable $y \mid z_{1:N}, \eta, \sigma^2 \sim N(\eta^T \bar{z}, \sigma^2)$, where

$$\bar{z} = (1/N) \sum_{n=1}^{N} z_n.$$

Supervised LDA



- The response variable y is drawn after the document because it depends on z_{1:N}, an assumption of partial exchangeability.
- Consequently, y is necessarily conditioned on the words.

Prediction

- Fit sLDA parameters to documents and responses. This gives:
 - topics $\beta_{1:K}$
 - coefficients $\eta_{1:K}$
- We have a new document $w_{1:N}$ with unknown response value.
- We predict y using the SLDA expected value:

$$\mathbf{E}\left[\mathbf{Y} \,|\, \mathbf{w}_{1:N}, \alpha, \beta_{1:K}, \eta, \sigma^2\right] = \eta^\top \mathbf{E}\big[\bar{\mathbf{Z}} \,|\, \mathbf{w}_{1:N}\big]$$