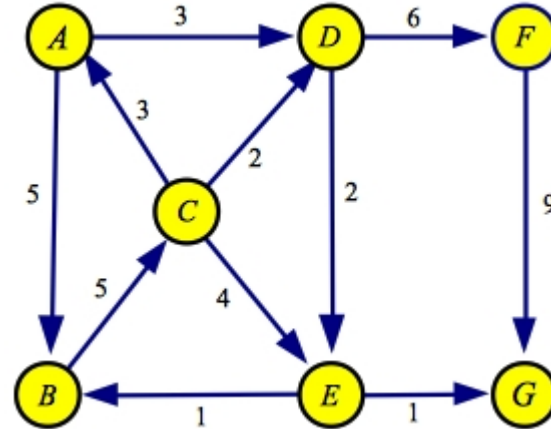
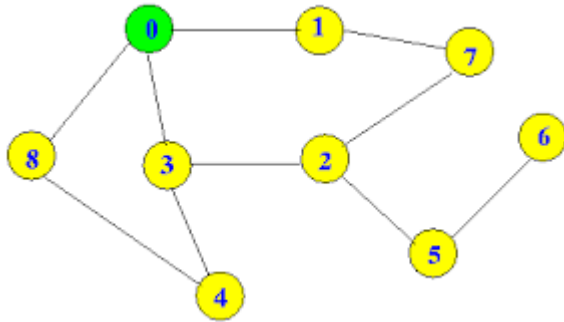


INTRODUCTION TO GRAPHS



Partha P Chakrabarti

Indian Institute of Technology Kharagpur

Graphs

A Graph $G = (V, E)$ consists of the following:

- A set of **Vertices** or **Nodes** V
 - Nodes may have one or more labels.
- A set of **Edges** E where each edge connects vertices of V
 - An edge usually defines a connection or relationship between vertices or nodes.
 - The edges can be undirected or **directed**.
 - Each edge can have one or more labels.
 - Usually there is at most one edge between vertices, there could be multiple edges between the same nodes.
 - Normally an edge connects two vertices, but in general we could have hyper-edges.

$(0,8)$

$e_i(0,8)$
 $(8,0)$

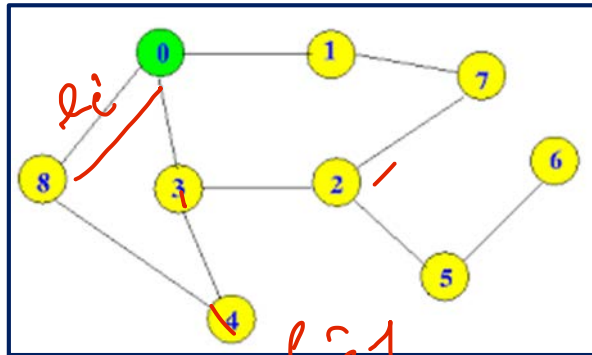


Fig 1

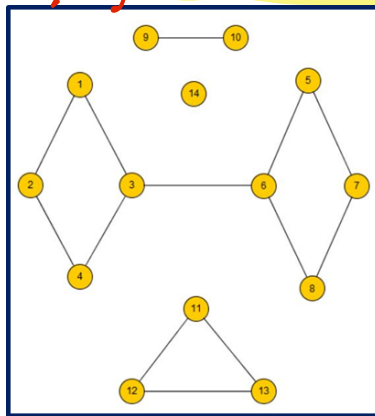


Fig 2

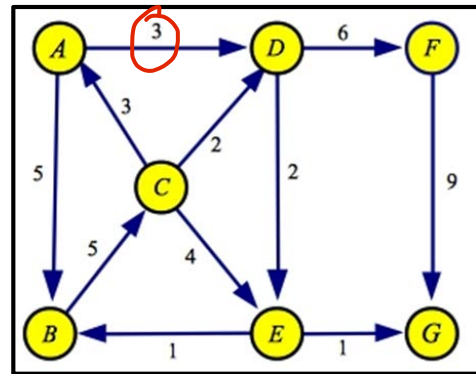


Fig 3

Graphs

A Graph $G = (V, E)$ consists of the following:

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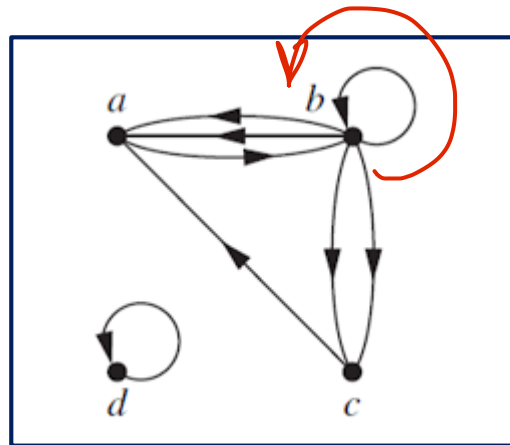
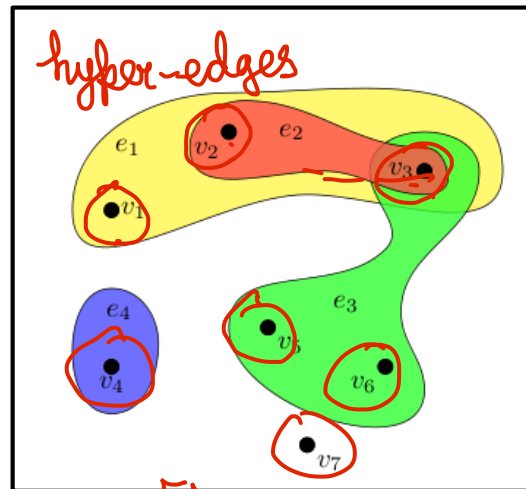


fig 4



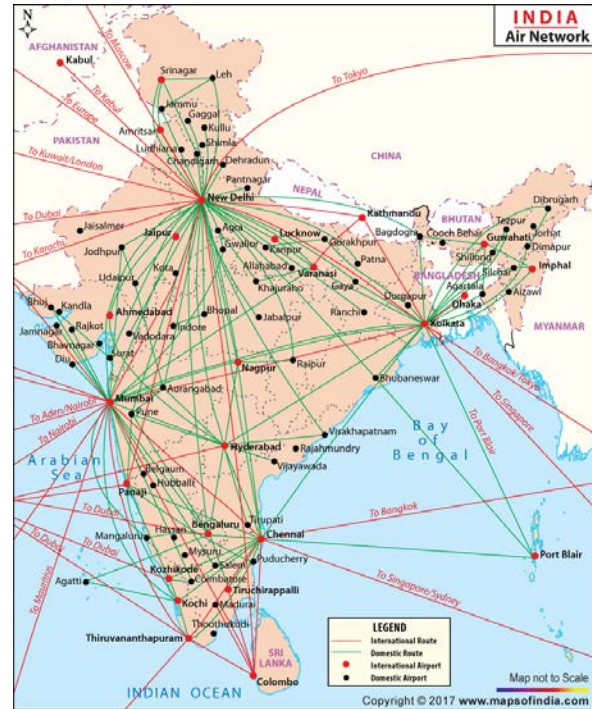
$$e = \{v_1, v_2, \dots, v_k\}$$

fig 5

Some Applications of Graphs

- Maps, Routes
- Layouts
- Circuits and Networks
- Relationships
- Constraints
- Dependencies
- Flow Charts
- State Machines

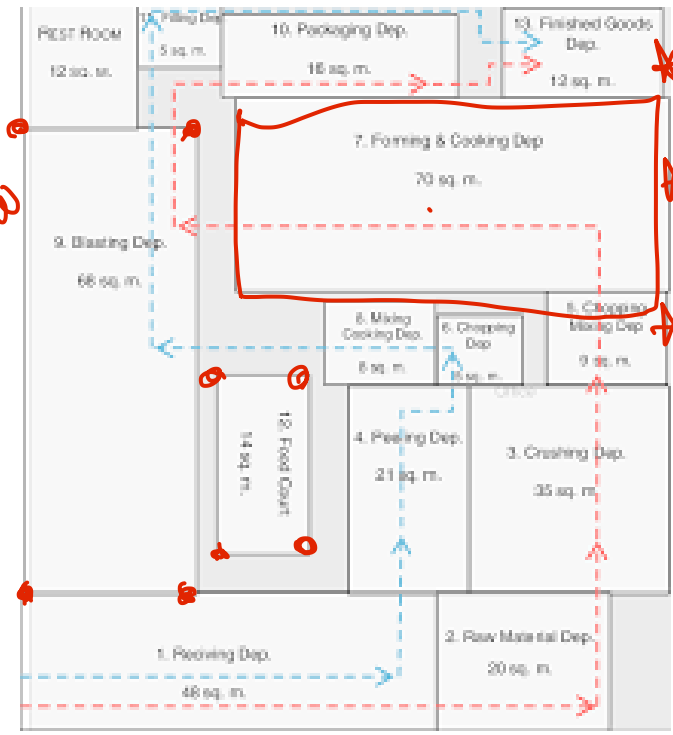
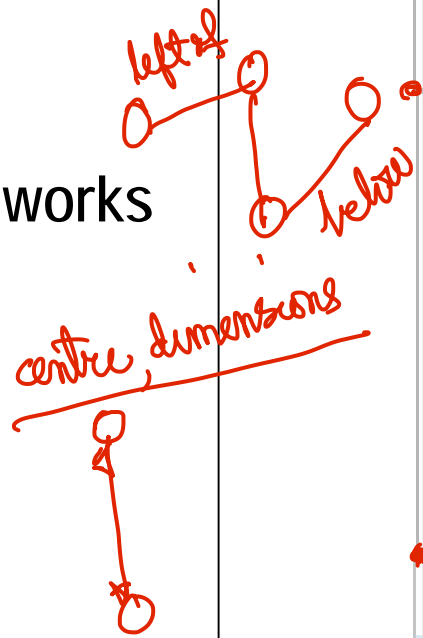
ETD ETA
airline
Flight No \rightarrow
 $V =$ cities
 $E =$ set of direct flights between cities



Appl Fig 1

Some Applications of Graphs $G_Z(V, E)$

- Maps, Routes
- **Layouts**
- Circuits and Networks
- Relationships
- Constraints
- Dependencies
- Flow Charts
- State Machines



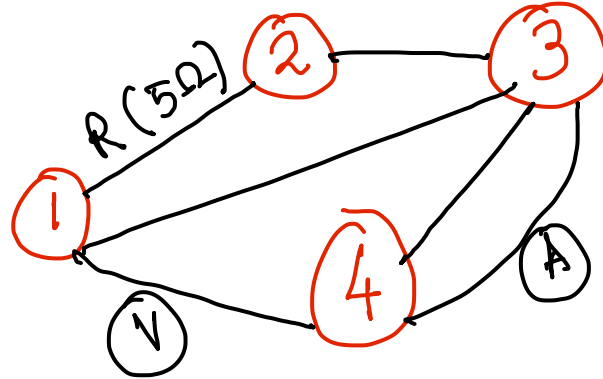
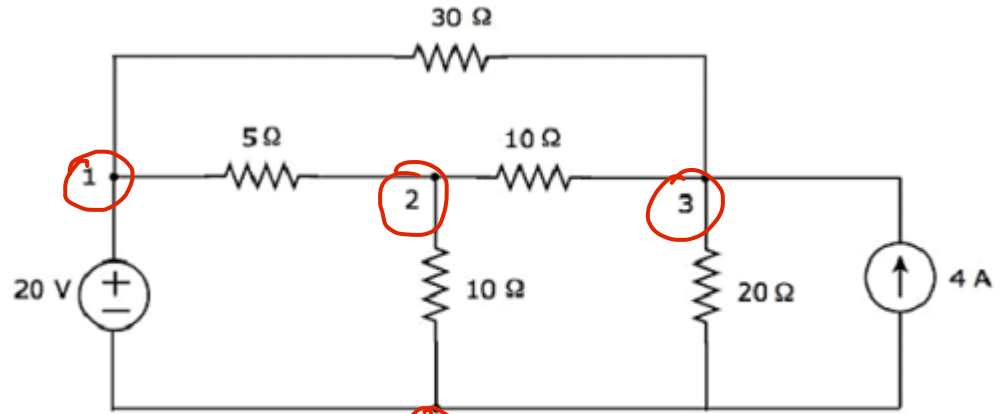
Physical

Logical

line drawing

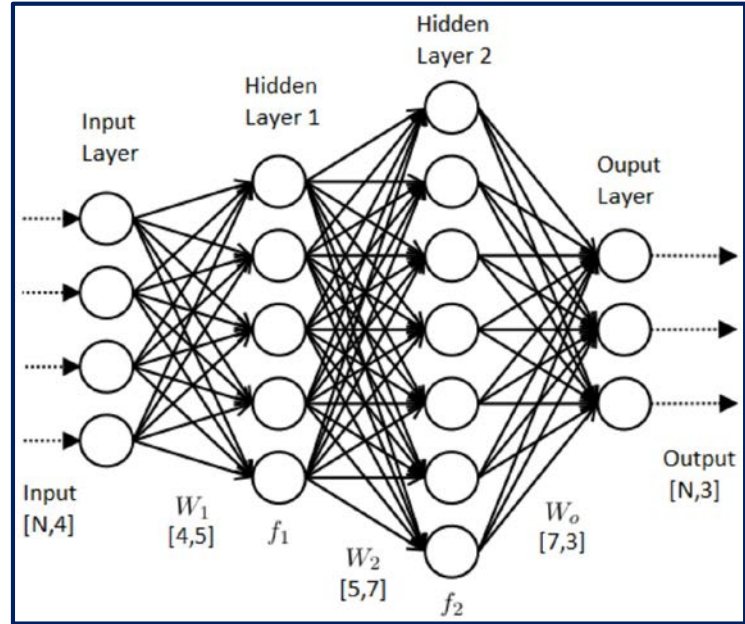
Some Applications of Graphs

- Maps, Routes
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- **Circuits and Networks**
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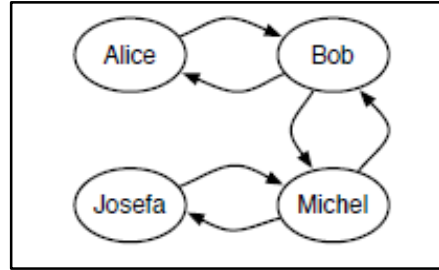
Some Applications of Graphs

- Maps, Routes
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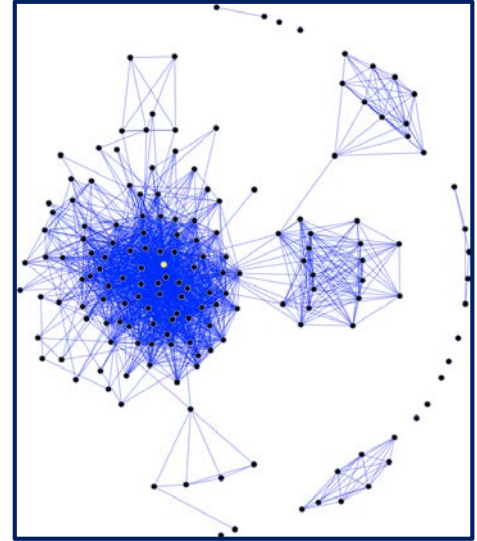
Some Applications of Graphs

- Maps, Routes
- Layouts
- Circuits and Networks
- **Relationships**
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- Dependencies
- Flow Charts
- State Machines



Friendship (likes)

→ citation graphs



Some Applications of Graphs

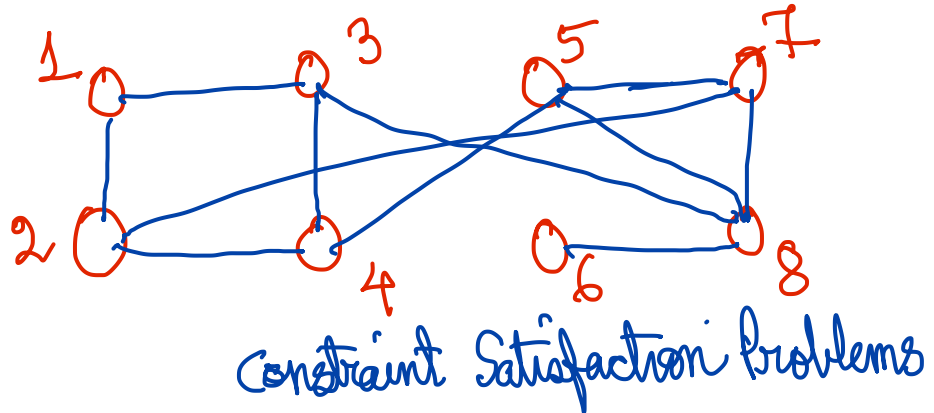
- Maps, Routes
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Instructions

- fill in words from the list

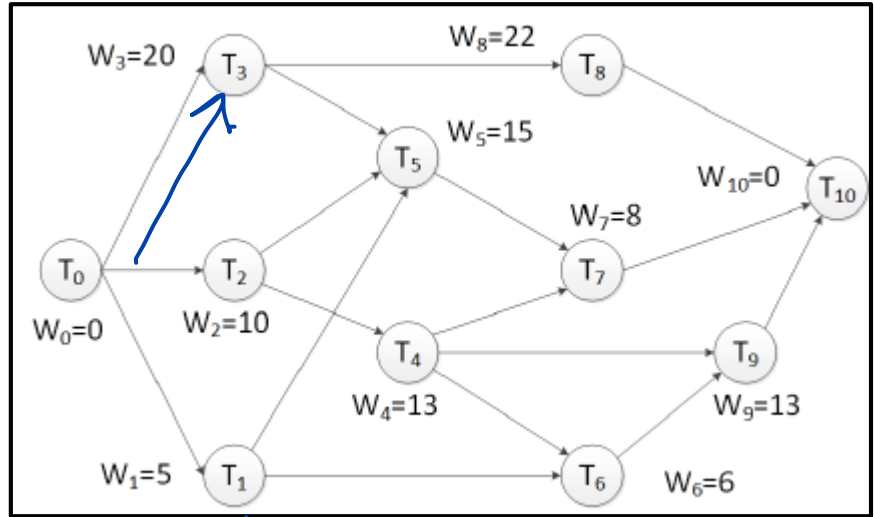
List of Words

- All
- Ale
- Eel
- Hike
- Hoses
- Keel
- Knot
- Laser
- Lee
- Line
- Sails
- Sheet
- Steer
- Tie



Some Applications of Graphs

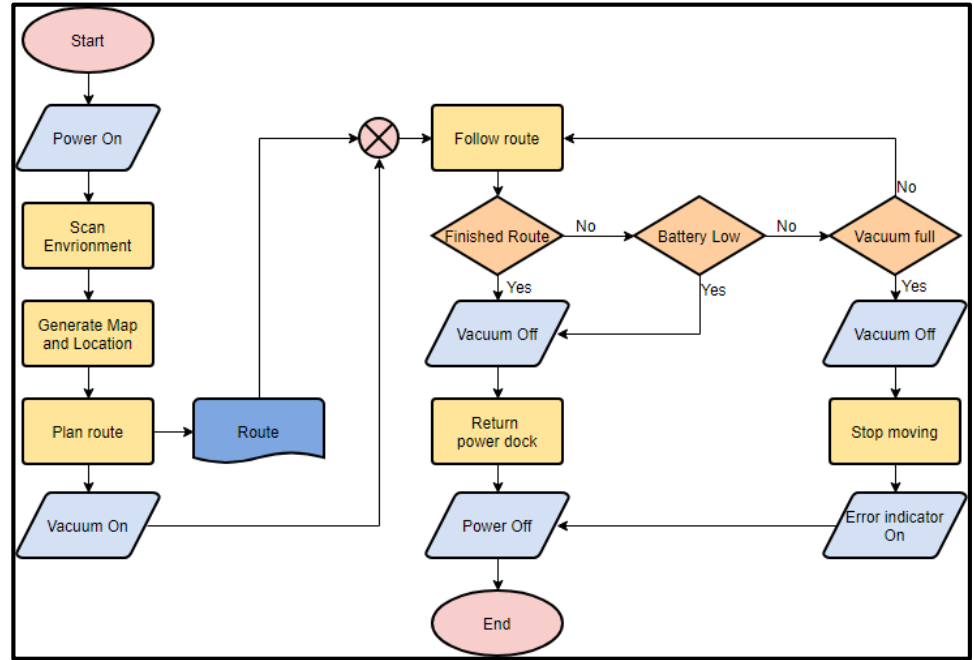
- Maps, Routes
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Acyclic Graphs

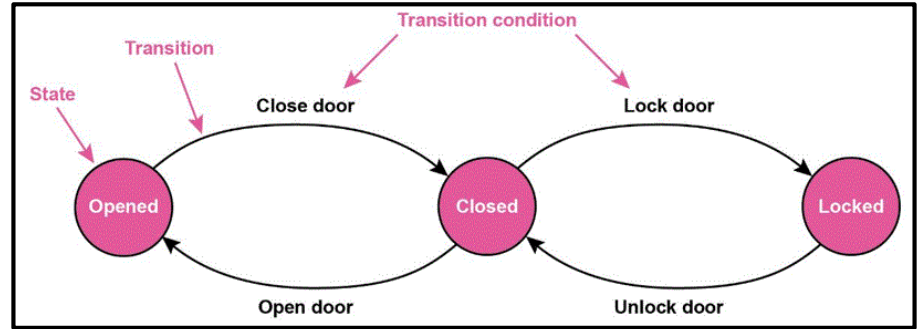
Some Applications of Graphs

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Some Applications of Graphs

- Maps, Routes
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State = Node
Transition = edge

Graph Representation

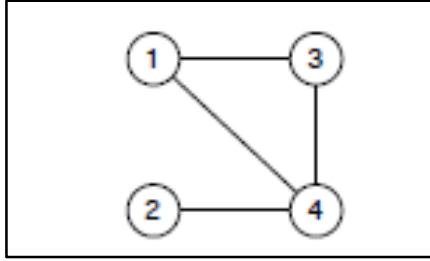


Fig 1

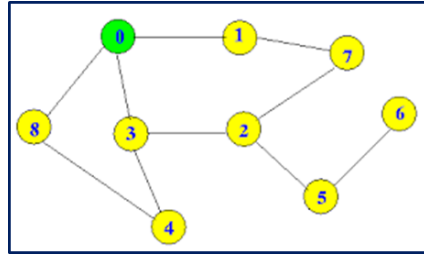
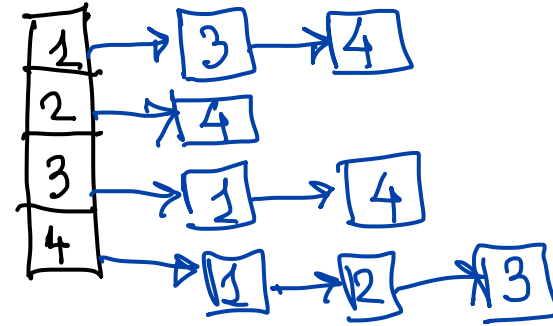


Fig 2

Adjacency Matrix

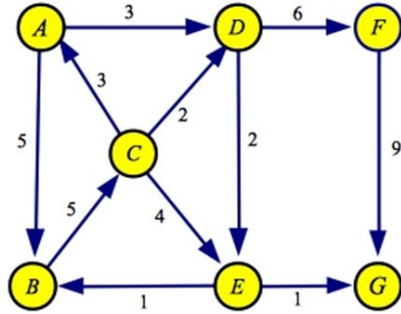
	1	2	3	4
1	0	0	1	1
2	0	0	0	1
3	1	0	0	1
4	1	1	1	0

Adjacency List



1	2	3	4	
2	1	4		
3	2	1	4	
4	3	1	2	3

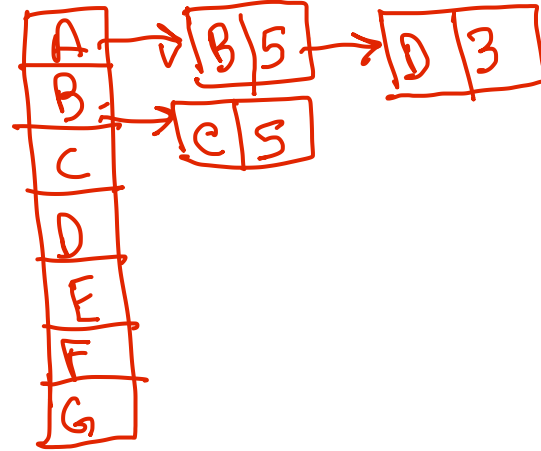
Graph Representation



Adjacency Matrix

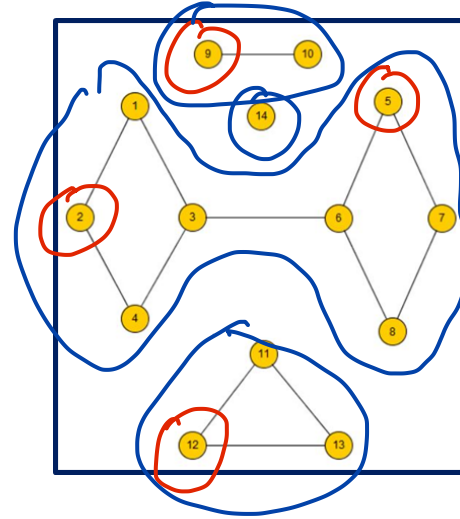
	A	B	C	D	E	F	G
A				3			
B	3						
C							
D						6	
E							
F							
G							

Adjacency List



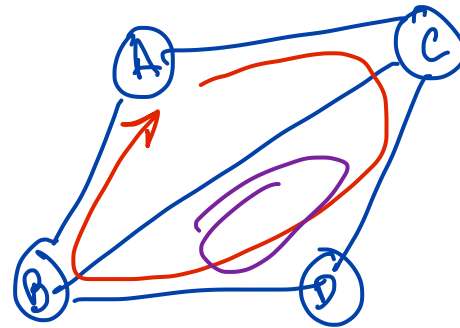
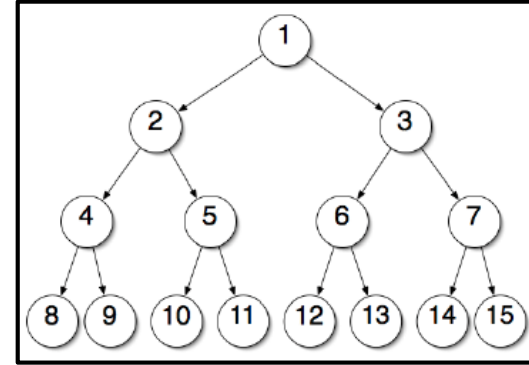
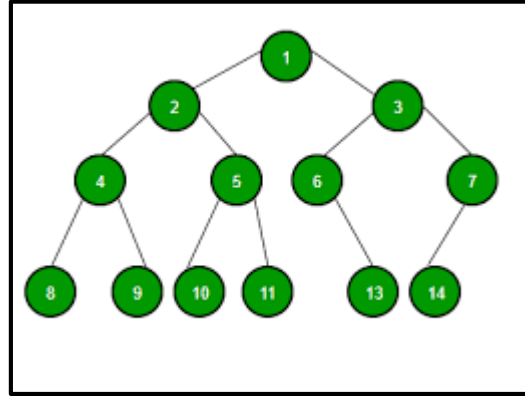
Some Algorithms on Graphs

- Paths
- Reachability
- Connected Components
- Trees, Cycles, ordering
- Costs & Distances
- Spanning Trees
- Shortest Paths
- Flows



Some Algorithms on Graphs

- Paths
- Reachability
- **Trees, Cycles, ordering**
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Some Algorithms on Graphs

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- Reachability
- **Cycles, ordering**
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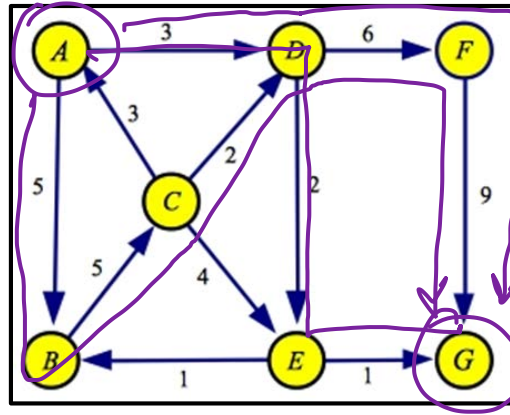


Fig 1

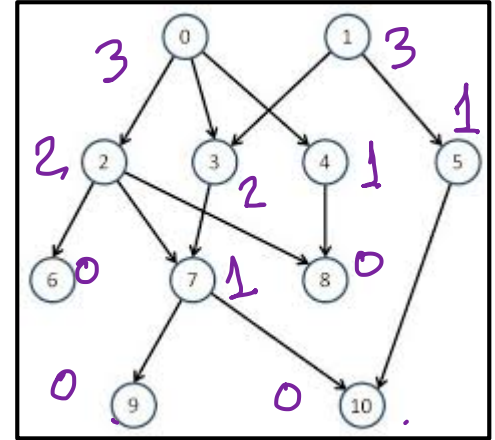
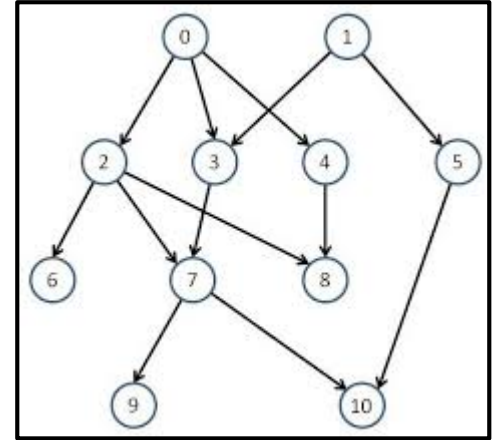
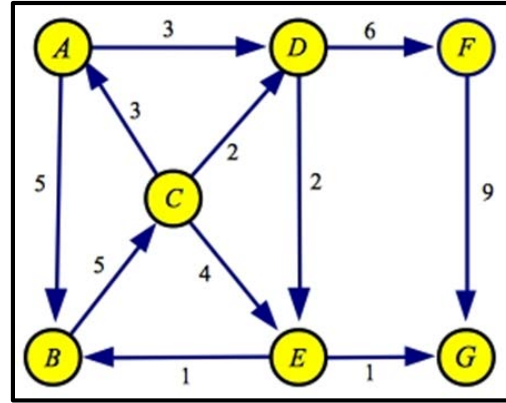


Fig 2

Some Algorithms on Graphs

- Paths
- Reachability
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- **Spanning Trees**
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Some Algorithms on Graphs

- Paths
- Reachability
- Cycles, ordering
- Connected Components
- Costs & Distances
- Spanning Trees
- Shortest Paths
- Flows

$$G = (V, E)$$

V = set of vertices

E = set of edges

undirected / directed

weights / labels

cycles / acyclic

TRAVERSAL OF GRAPHS
Algorithms for Graphs

Thank you