

# Assignment 3: CS21003 Algorithms 1

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1. Design an efficient data structure where the key elements are lower-case alphabetic strings and the ordering is lexicographic. Each string can be of maximum size  $m$ . The operations are insert, delete, find, max, and min. Clearly explain how you will
  - (a) implement this data structure,
  - (b) provide an example representation,
  - (c) present algorithms for each operations,
  - (d) analyze the time complexity of each operation,
  - (e) space complexity for storing  $n$  elements to efficiently manage the structure.

Do NOT assume that  $m$  is a constant.

**[10 Marks]**

2. Suppose you are given a black box access to a sorting algorithm which takes an array containing distinct integers as input and outputs the sorted array. Use this algorithm in a black box fashion to design an algorithm to remove all duplicates from an integer array. You are allowed to perform  $\mathcal{O}(n)$  comparisons other than the comparisons done inside the black box of the sorting algorithm. You are free to perform all other kind of computations of any time complexity.

**[10 Marks]**

3. Suppose you are given a gray box access to a comparison-based algorithm for removing all duplicates from an integer array — you can observe the sequence of comparisons that the algorithm performs on any input and nothing else. Use this gray box to design a comparison-based algorithm to sort an integer array. You are allowed to perform  $\mathcal{O}(n)$  comparisons other than the comparisons made by the gray box algorithm. You are free to perform all other kind of computations of any time complexity. Can you now see that  $\Omega(n \log n)$  is also a lower bound on the number of comparisons that any comparison-based algorithm must perform to remove all duplicates? (You do not need to write in your answer script that yes I see! The last sentence is for your own understanding.)

**[10 Marks]**