### CS29003 Algorithms Laboratory Assignment 8: Application of Graph traversals

#### General instruction to be followed strictly

- 1. Do not use any global variable unless you are explicitly instructed so.
- 2. Do not use Standard Template Library (STL) of C++.
- 3. Use proper indentation in your code and comment.
- 4. Name your file as <roll\_no>\_<assignment\_no>. For example, if your roll number is 14CS10001 and you are submitting assignment 3, then name your file as 14CS10001\_3.c or 14CS10001\_3.cpp as applicable.
- 5. Write your name, roll number, and assignment number at the beginning of your program.
- 6. Make your program as efficient as possible. Follow best practices of programming.

Let  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$  be a **weighted**, **undirected**, **acyclic**, **connected** graph with weight function  $w : \mathcal{V} \longrightarrow \mathbb{Z}$ . Let n be the number of vertices in  $\mathcal{G}$ . Observe that such a graph has exactly n - 1 edges. We are also given a cost  $c : \mathcal{E} \longrightarrow \mathbb{Z}$  per edge. Since  $\mathcal{G}$  is connected and acyclic, if we remove any edge  $e \in \mathcal{E}$  from  $\mathcal{G}$ , we obtain two connected components, say  $\mathcal{H}_1^e, \mathcal{H}_2^e$ . We define the **vulnerability** ( $\gamma_e$ ) of any edge  $e \in \mathcal{E}$  as follows.

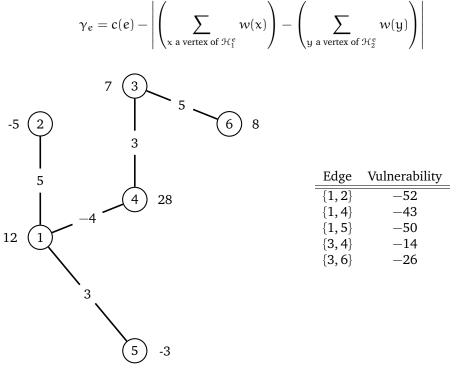


Figure 1: A graph and the vulnerability of its edges.

Vertices are labeled with  $\{1, 2, ..., n\}$ . Figure 1 exhibits an example of a graph and the vulnerabilities of its edges. In this assignment, you write a C/C++ function to find an edge having the highest

vulnerability. If there are more than one edge having the highest vulnerability, output any one of them. Represent the graph with an adjacency list.

# Part I: Brute-force $O(n^2)$ -Time Algorithm

In this part, you implement the following algorithm. For each edge  $e \in \mathcal{E}$ , you remove the edge from the graph, obtain the two connected components  $\mathcal{H}_1^e$  and  $\mathcal{H}_2^e$ , compute the sum of the weights of the vertices in each  $\mathcal{H}_1^e$  and  $\mathcal{H}_2^e$ , and compute  $\gamma(e)$ . Finally output an edge e with the smallest  $\gamma(e)$ .

### Part II: Linear Time Algorithm

Design an O(n)-time algorithm for this problem. *Hint: use DFS (you are welcome to use any other approach)!* 

## main()

- 1. Read n from the user.
- 2. Read the weights of these n vertices.
- 3. Read the edges along with its weight.
- 4. Dynamically allocate space to store the graph in the adjacency list format using malloc/calloc/new
- 5. Compute an edge with the smallest vulnerability using both the methods and output.

You assume that the given graph is weighted, undirected, acyclic, connected (no need to check this in your code). An edge is denoted by an unordered pair of vertices whose order does not matter. For example, when giving input, user can denote an edge as 2 3 or 3 2. You code should behave identically in both the cases. Submit a single .c or .cpp file. Your code should get compiled properly by gcc or g++ compiler.

#### Sample Output

```
Write n: 6
Write weights of vertices: 12 -5 7 28 -3 8
Write the edges and their weights
1 2 5
1 4 -4
1 5 3
3 4 3
3 6 5
Edge with the smallest vulnerability computed using first method: 3 4
Edge with the smallest vulnerability computed using second method: 3 4
```